



**THE AERODYNAMIC PERFORMANCE OF THE HOUCK CONFIGURATION
FLOW GUIDES**

THESIS

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AFIT/GAE/ENY/07-J09

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AFIT/GAE/ENY/07-J09

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GUIDES**

THESIS

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Department of Aeronautical and Astronautical Engineering

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In Partial Fulfillment of the Requirements for the
Degree of Master of Science in Aeronautical Engineering

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FLOW GUIDES**

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Abstract

In an effort to explore efficient wing designs for UAV's, the Air Force is investigating the patented Houck Aircraft Configuration, which is a joined-wing aircraft with curved flow guides of varying camber connecting the upper and lower wingtips. Models were drawn in three-dimensions using Solidworks® with upper and lower wings drawn as identical NACA 2412 airfoil sections for all models. A variety of airfoil sections between the upper and lower wingtips were drawn and rotated to achieve a combination of cant and angle of attack variation. Subsequently, a solid part was lofted through these sections and merged with the upper and lower wings. Each model was built by a rapid prototype machine. A six-component balance in the AFIT low-speed wind tunnel provided measurements yielding the aerodynamic data of each model. Comparisons are made to the same basic planform area without flow guides and to a case where the wingtips are joined with a flat plate. At a Reynolds number of 38K, the increase in skin friction drag outweighed any possible reduction of induced drag. However for Reynolds numbers in the 57K to 120K range, improvements in L/D_{\max} of about 2-5% over the no flow guide case were measured.

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Dermot N. Killian II

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List of Symbols

| | | |
|----------------------|-----------------------------|--------------------|
| A | axial load force | (lb _f) |
| AR | aspect ratio | (-) |
| α | angle of attack | (°) |
| b | wing span | (in) |
| \bar{c} | average chord | (in) |
| C_D | total drag coefficient | (-) |
| C_{Di} | induced drag coefficient | (-) |
| C_{Do} | minimum coefficient of drag | (-) |
| C_L | lift coefficient | (-) |
| C_{Lmax} | maximum coefficient of lift | (-) |
| C_m | pitch moment coefficient | (-) |
| D | drag | (lbs) |
| D_{form} | form drag | (lbs) |
| $D_{induced}$ | induced drag | (lbs) |
| $D_{interference}$ | interference drag | (lbs) |
| $D_{parasite}$ | parasite drag | (lbs) |
| $D_{skin\ friction}$ | skin friction drag | (lbs) |
| D_{total} | total drag | (lbs) |
| δ_b | blockage correction factor | (-) |
| e | span efficiency factor | (-) |

| | | |
|-------------------|--------------------------------------|-------------------------|
| $e AR$ | effective aspect ratio | (-) |
| Γ | circulation | (in ² /s) |
| k | ratio of span to tunnel height | (-) |
| Ke | normalized turbulent kinetic energy | (-) |
| L/D | lift-to-drag ratio | (-) |
| L/D_{\max} | maximum lift-to-drag ratio | (-) |
| λ | wind tunnel aspect ratio | (-) |
| N | normal load force | (lb _f) |
| P_{baro} | barometric pressure in test room | (psi) |
| q | dynamic pressure | (in Hg) |
| ρ | air density | (slug/ft ³) |
| Re | Reynolds number | (-) |
| S | planform area of wing | (in ²) |
| T_{room} | temperature in test room | (°F) |
| u | u-component of velocity in wind axis | (mph, m/s) |
| u_{rms} | root mean squared of u measurements | (mph, m/s) |
| v | v-component of velocity in wind axis | (mph, m/s) |
| v_{rms} | root mean squared of v measurements | (mph, m/s) |
| V | average wind tunnel velocity | (mph, m/s) |
| w | w-component of velocity in wind axis | (mph, m/s) |
| w_{rms} | root mean squared of w measurements | (mph, m/s) |
| W | aircraft weight | (lbs) |

| | | |
|------------|--|------------|
| x | x-component of velocity in hot-wire axis | (mph, m/s) |
| X_{cg} | x location of center of gravity from aircraft nose | (in) |
| X_{cmb} | x distance from balance moment center to $\frac{1}{4}$ chord | (in) |
| y | y-component of velocity in hot-wire axis | (mph, m/s) |
| z | z-component of velocity in hot-wire axis | (mph, m/s) |
| Z_{cmb} | z distance from balance moment center to $\frac{1}{4}$ chord | (in) |
| ω_x | curl or vorticity about x axis | (rad/s) |

THE AERODYNAMIC PERFORMANCE OF THE HOUCK CONFIGURATION FLOW GUIDES

I. Introduction

1.1 Background

As previously summarized by Michael Walker's Thesis (31), The Air Force Research Lab (AFRL) has been investigating the claims of a patent for a new aircraft wing design known as the Houck Lifting Foil (see Figure 1). The purpose of the Houck Lifting Foil is to provide an aerodynamically efficient design for a joined-wing aircraft. A description of the Houck Lifting Foil, as described by the patent's abstract, is as follows:

A lifting foil for an aircraft, a hydrofoil or the like having a pair of courses or wings. Vortex losses due to spanwise fluid flow are substantially reduced by joining the tips of the courses with flow guides configured for jointly terminating the undesired flows. Termination is effected by providing the flow guides with crosssections cambered for reducing the dynamic pressure of fluid flowing in a spanwise direction across the flow guide surfaces (16).

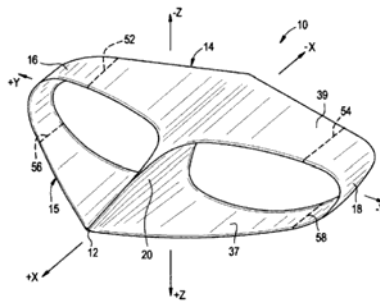
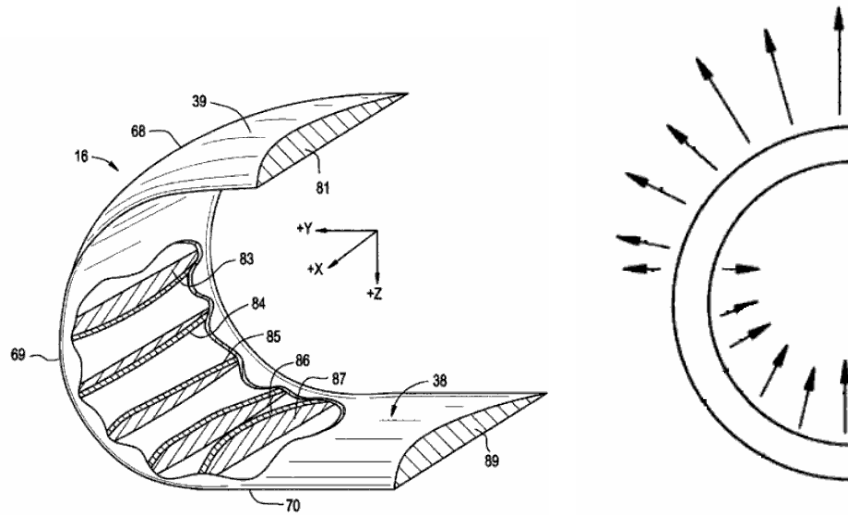


Figure 1: Isometric View of the Houck Lifting Foil (reproduced from Reference 16)

The upper and lower wings of the Houck Lifting Foil are connected by flow guides that are specially cambered and curved to direct airflow along a specified path (see

Figure 2). The cambered airfoil sections are placed at precise locations to control the pressure distribution along the surface of the curved flow guide.

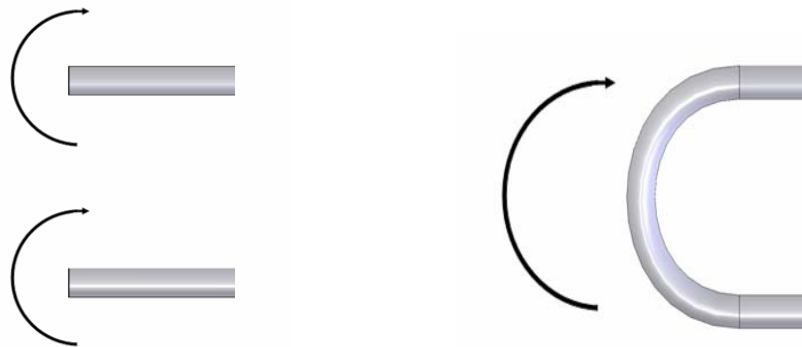


Varying Camber throughout Flow Guide

Pressure Distribution along Surface

Figure 2: Flow Guide Structure and Pressure Distribution (reproduced from Reference 16)

The purpose of the curved flow guide connection between the upper and lower wings is to combine the individual wing-tip vortices (without the flow guide) into a single vortex that is more spread out (see Figure 3), thus reducing induced drag.

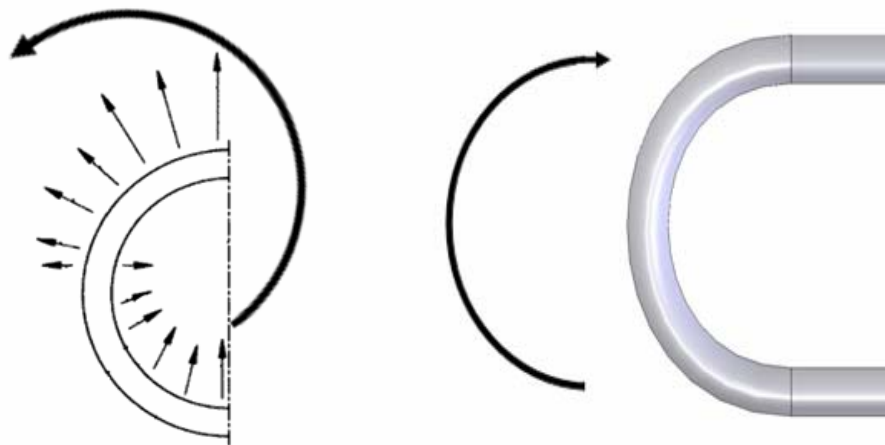


Individual Wing-Tip Vortices on Upper and Lower Wing

Combined Wing-Tip Vortex due to Flow Guide

Figure 3: Flow Guide Combining Wing-Tip Vortices

The flow guides are also progressively cambered along the curve in order to manipulate the flow near the wing-tips. From the lower wing the airfoil sections become progressively less cambered until the mid-point of the flow guide. At this point the airfoil is symmetric and does not provide any pressure difference (hence vortex). The process of progressive camber continues in the opposite direction until the camber of the flow guide matches the camber of the upper wing. The purpose of this variable camber flow guide design is to produce an aerodynamic force that opposes the aerodynamic force created by the wing-tip vortex of the flow guide (see Figure 4).



Resultant Force from the Progressive Camber Changes Resultant Force from Flow Guide Vortex
Figure 4: Resultant Force of Progressive Camber Opposing Resultant Force of Flow Guide Vortex

The designer of the Houck Lifting Foil claims that the use of the flow guides increases the aerodynamic efficiency by reducing the span-wise fluid flow over the wings, the cause of wing-tip vortices (16). The reduction of the wing-tip vortices strength would result in a reduction of induced drag (drag due to lift). If the reduction of induced drag is greater than the increase in parasite drag (profile drag, skin friction drag, and

interference drag) then the total drag will be reduced. Profile or form drag is related to the size of the aircraft whereby the flow guides would increase size. Skin friction is related to the friction of the fluid flow over the surface area of the aircraft whereby flow guides would increase surface area. Interference drag is caused the interference of boundary layers caused by other portions of the aircraft whereby the flow guides would increase interference. Hence, if this design is able to produce the aforementioned results, then it can be applied to various applications where aerodynamic efficiency is desired. These applications include, but are not limited to: fixed wing aircraft, rotary wing aircraft, submarines, and hydrofoils (16).

1.2 Problem Statement

The root question that is to be answered at the conclusion of this report is to determine whether or not the flow guides are able to perform as designed and stated in the patent. Does the progressive and variable camber along the flow guide create a resultant force that opposes the wing-tip vortex of the flow guide? Further more does this reduction in wing-tip vortices lower the induced drag as to the opposed increase in parasite drag due to the extra flow guide surface area? These questions will be attempted to be answered at the conclusion of this report.

1.3 Research Focus

The purpose of this report is to further investigate the aerodynamic performance of the Houck Lifting Foil. The primary investigative focus is on the aerodynamic properties associated with the variable camber flow guides. As prescribed by Patent

Number 7,100,867's 14th and 17th claims, models were constructed using *SolidWorks* that employ the variable camber flow guides (16). Figure 5 shows the Original Configuration Model that was constructed for testing.

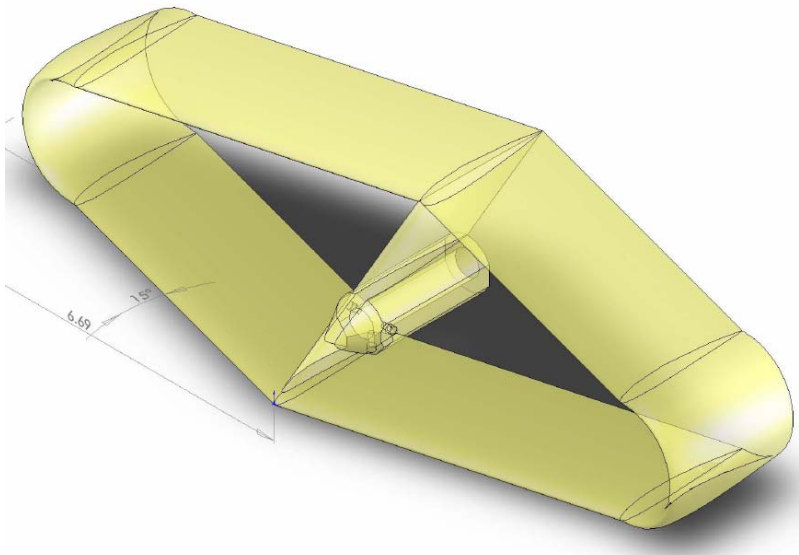


Figure 5: Original Configuration Model Utilizing the Flow Guides as prescribed by the Houck Lifting Foil Patent

The model has an average chord (\bar{c}) of 2.55", a wingspan (b) of 13.808", and a length of 5.59". The wing is based on a NACA 2412 airfoil section. It has a planform area (S) of 72.58 in². Further discussion of parameters is located in Section 3.3.

The models were built using the AFIT Objet 3D printer. In order to achieve aerodynamic analyses of the models, numerous tests were run in the AFIT low-speed wind tunnel. In addition to the aerodynamic analyses of the models, there was further examination of the Hot-Wire Anemometry data from the previous thesis investigation by Michael Walker (31). The model used for Hot-Wire Anemometry data is located in Figure 6.

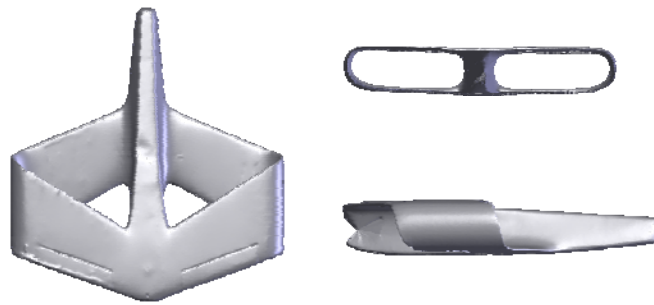


Figure 6: Three-View Representation of 24" Houck Configuration (reproduced from Reference 31)

The combination of these results in this report will be used in conjunction with other studies carried out by the Air Force Research Lab, Air Vehicles Directorate, Wright Patterson AFB, Ohio to determine the viability of the Houck Lifting Foil for the United States Air Force (6).

II. Literature Review

2.1 Overview

Since the dawn of manned flight there has been a constant effort to improve and refine aircraft aerodynamics. Before improvements can be made, the fundamentals of flight must first be understood. Therefore the beginning of this chapter begins with a few of the fundamentals of flight that will be the basis of discussion throughout the paper. This includes camber, drag, and wing-tip vortices. Next the chapter will progress into a discussion of devices and aircraft configurations that are the primary designs associated with the Houck configuration. This includes winglets, biplanes, and joined-wing aircraft. After that the chapter will discuss the evolution of aircraft efficiency which is primarily measured by lift-to-drag ratio. Finally the chapter will end with a discussion of measurement and building methods that were used to find the data for this paper.

2.2 Camber

Typical airfoil shape is determined by six elements: the leading edge, the trailing edge, the chord line, the camber line, the upper surface, and the lower surface. Camber is defined as the curvature of the mean camber line. The mean camber line is the line midway between upper and lower surfaces, extending from leading to the trailing edge (9). Figure 7 shows a positively cambered airfoil with the placement of the elements aforementioned.

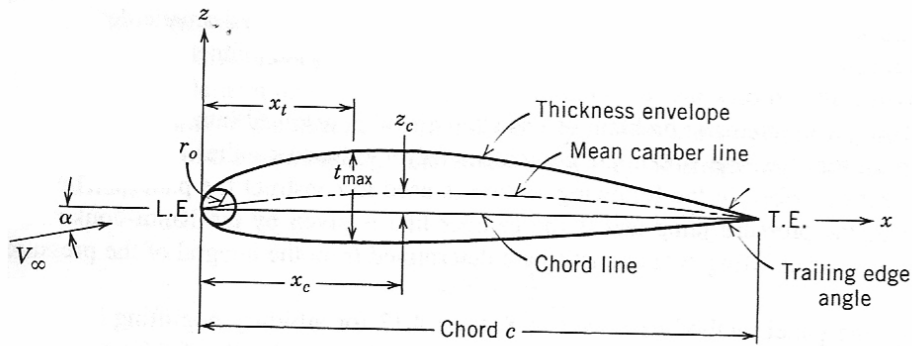


Figure 7: Airfoil geometrical elements (reproduced from Reference 17)

Camber contributes to the lift produced by the airfoil. At an angle of attack of zero, an airfoil with zero camber produces zero lift, an airfoil with positive camber produces positive lift, and an airfoil with negative camber produces negative lift. Figure 8 demonstrates how camber can affect lift.

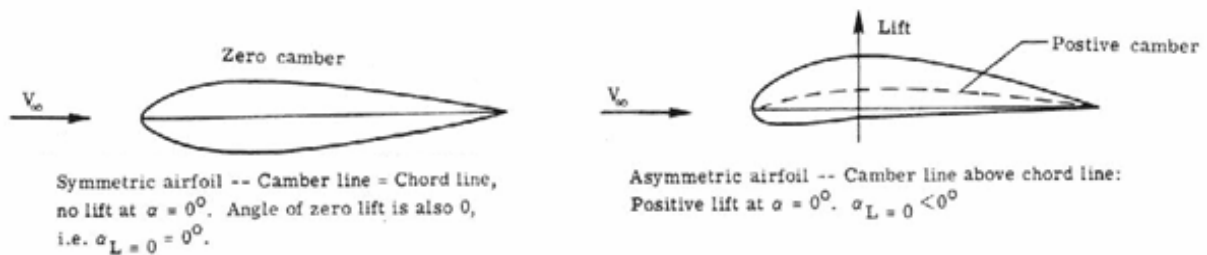


Figure 8: Effects of Zero and Positive Camber (reproduced from Reference 28)

2.3 Drag

“Drag is the component of the aerodynamic force that is parallel to the relative wind and retards the forward motion of the aircraft. At subsonic speeds, there are two kinds of drag: parasite drag and induced drag” (11). There is a third type of drag, compressibility drag; however this occurs at speeds higher than those considered in this study. The basic drag equation follows:

$$D = C_D q S \quad (1)$$

Where D (lbs) is drag, C_D is coefficient of drag, q is dynamic pressure (in Hg), and S is planform area of the wing (in²). The coefficient of drag, C_D , is the ratio of drag pressure to the dynamic pressure and is shown in the following equation:

$$C_D = \frac{D / S}{q} \quad (2)$$

These values of C_D are usually obtained experimentally.

Parasite drag, $D_{parasite}$, is made up of three different components: skin friction drag ($D_{skinfriction}$), form drag (D_{form}), and interference drag ($D_{interference}$). Skin friction drag is caused by the viscous friction within the boundary layer. The total area of the aircraft skin that is exposed to the airstream and its smoothness affects this type of drag. The major way to reduce the skin friction drag is to maintain the laminar airflow over the skin surface by maintaining a smooth surface by waxing and polishing the surfaces. Another method is to use laminar flow airfoils to delay boundary layer transition. Form drag, also known as pressure drag, is caused by the form of the aircraft. This drag occurs due to the turbulent wake behind the aircraft created by the pressure differences of flight.

Streamlining the fuselage and various other aircraft extremities reduces form drag.

Interference drag is caused by the interference of boundary layers from different parts of the aircraft (e.g. wing and fuselage). The total drag of the assembled components is

higher than the sum of the individual drag of the components unassembled. Smooth fairings at surface junctions reduce interference drag by creating fillets where sharp angles would otherwise occur. The breakdown of parasite drag in equation form is as follows:

$$D_{\text{parasite}} = D_{\text{skinfriction}} + D_{\text{form}} + D_{\text{interference}} \quad (3)$$

Where D_{parasite} is parasite drag (lbs), $D_{\text{skinfriction}}$ is skin friction drag (lbs), D_{form} is form drag (lbs), and $D_{\text{interference}}$ is interference drag (lbs).

Induced drag, D_{induced} , is the “least understood type of drag, but it is the most important, especially in the low-speed region of flight” (11). Induced drag, also known as drag to lift, is primarily caused by wing-tip vortices that form as the aircraft produces lift. Induced drag also includes the incremental change in pressure drag due to lift (due to the change in the angle of attack). Figure 9 shows the effect of induced drag on a finite wing.

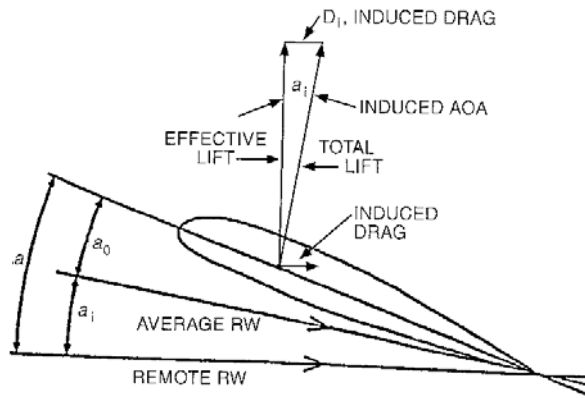


Figure 9: Effect of Induced Drag on Finite Wing (reproduced from Reference 11)

Total Drag, D_{total} (lbs), is the drag that is sum of induced drag, $D_{induced}$ (lbs), and parasite drag, $D_{parasite}$ (lbs). The total drag equation follows:

$$D_{total} = D_{induced} + D_{parasite} \quad (4)$$

For an aircraft in steady unaccelerated level flight with constant weight, the drag vs. velocity curve helps to approximate the speeds necessary for maximizing range and endurance. Additionally, the maximum endurance and range are factors determined by engine type for an aircraft. A turbojet/turbofan aircraft has a different method of measurement than a propeller-driven aircraft. Figure 10 shows the drag vs velocity curve for a turbofan/turbojet aircraft in steady unaccelerated flight with constant weight.

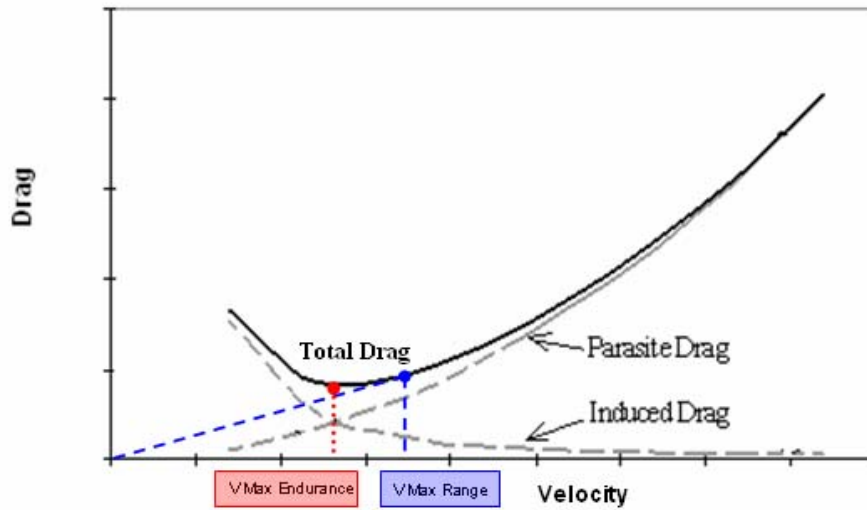


Figure 10: Drag vs Velocity for Turbofan/Turbojet Aircraft in Level Flight (reproduced from Reference 5)

The velocity that will allow the aircraft to maximize its endurance is the velocity where the total drag is minimized. At this velocity, the lift-to-drag ratio, L/D , is maximized and $D_{induced}$ is equal to $D_{parasite}$ (5). The velocity for maximum range is found by finding the values of drag, D , and velocity, V , which minimizes the ratio of D/V . This is achieved by drawing a line tangent to the Total Drag curve from the origin. At maximum range velocity, the ratio of $C_L^{1/2}/C_D$ is maximized (5). According to Brandt (5), usually the ratio $C_L^{1/2}/C_D$ is not used in a biplane analysis due the atypical use of turbofan/turbojet engines in the airframe. Figure 11 shows the drag vs. velocity curve for a propeller-driven aircraft in steady unaccelerated flight with constant weight.

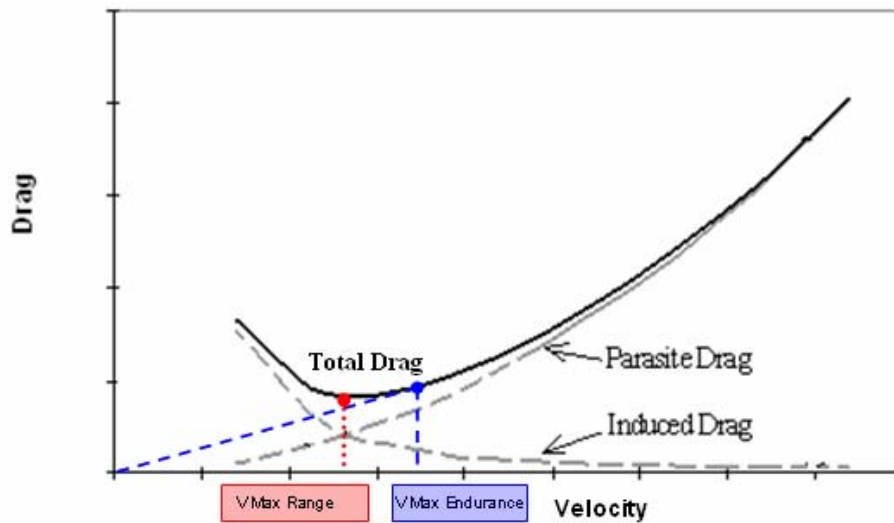


Figure 11: Drag vs Velocity for Propeller-Driven Aircraft in Level Flight (reproduced from Reference 5)

Unlike the Turbojet/Turbofan aircraft example, the velocity that will allow the propeller-driven aircraft to maximize its range is the velocity where the total drag is minimized. At this velocity, the lift-to-drag ratio, L/D , is maximized and $D_{induced}$ is equal to $D_{parasite}$ (5).

The velocity for maximum endurance is found by finding the values of drag, D , and velocity, V , which minimizes the ratio of D/V . This is achieved by drawing a line tangent to the Total Drag curve from the origin. At maximum-endurance velocity, the ratio of $C_L^{3/2}/C_D$ is maximized and the induced drag is equal to three times the parasite drag (34). The following equations summarize the relationship of parasite drag, C_{D_o} , to induced drag, C_{D_i} :

$$C_{D_o} = C_{D_i} \text{ at } \frac{L}{D_{\max}} \quad (5)$$

$$3C_{D_o} = C_{D_i} \text{ at } \frac{C_L^{\frac{3}{2}}}{C_{D_{\max}}} \quad (6)$$

Where C_{D_o} and C_{D_i} are dimensionless.

2.4 Wing-Tip Vortices

The flow phenomena at the wingtips of finite wings, known as wing-tip vortices, account for the major difference between a two-dimensional (infinite span) and three-dimensional (finite span) representation of wings. This difference between finite and infinite spans results from the formation of span-wise fluid flow that occurs in the three-dimensional case (5) and the assumption that in the two-dimensional case “the upflow in front of the wing exactly balances the downflow at the rear of the wing, so that there exists no net downward movement of air past wing caused by the circulation, Γ (in^2/s)” (28).

The primary cause for the formation of wing-tip vortices is lift. Lift, generated by a wing, results when there is a net pressure difference between the upper and lower surfaces of the wing. When the higher pressure exists on the lower surface of the wing, then positive lift is created. Due to the fact that wings are finite in length, the flow over the wing acts in a three-dimensional manner and has the tendency to equilibrate at the wing-tip (28). This phenomenon is seen in Figure 12.

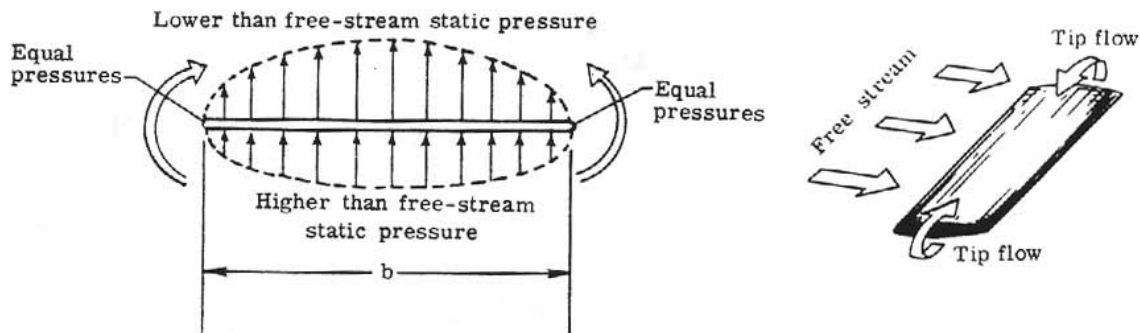


Figure 12: Equalizing Pressure at the Wing-Tips (reproduced from Reference 28)

Vortices form when the high pressure below the wing induces a circular velocity from below the wing that continues around the wing-tip to the lower pressure area on the upper surface of the wing. This movement in combination with the free stream flow of air, creates “very strong tornado-like swirling flows” also known as wing-tip vortices or trailing vortices that flow downstream (5). Wing-tip vortices are located above the wing-tips and have the tendency to sink and roll towards each other downstream of the wing (28). The tangential velocity at the core of the vortices can approach 70% of the aircraft’s forward velocity (18:304). Figure 13 demonstrates the formation of wing-tip vortices.

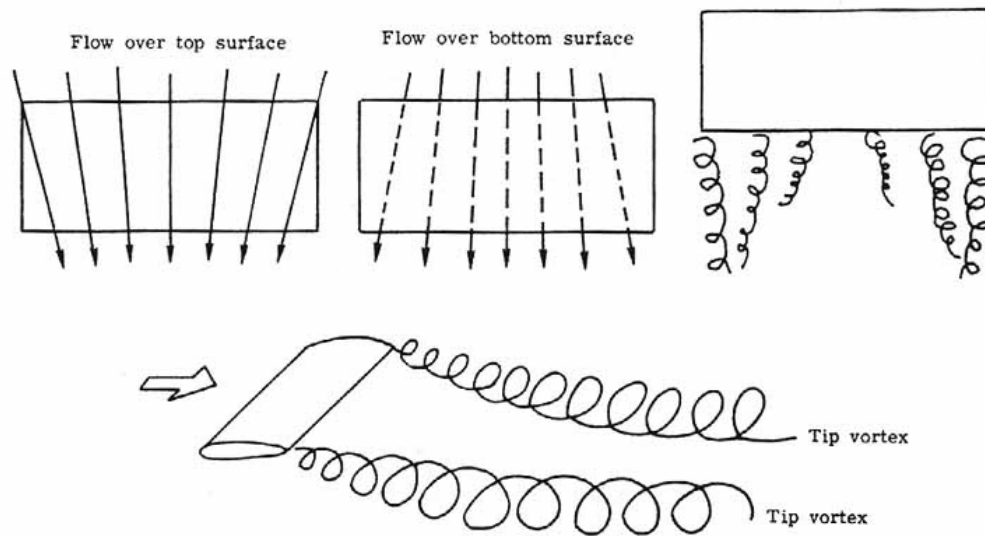


Figure 13: Formation of Wing-Tip Vortices (reproduced from Reference 28)

The circular flow pattern of the wing-tip vortices results in a downward component of the flow over the wing. This downward flow component is called downwash (see Figure 14). Downwash acts most strongly at the wingtips and loses strength toward the mid-span where its value is the least.

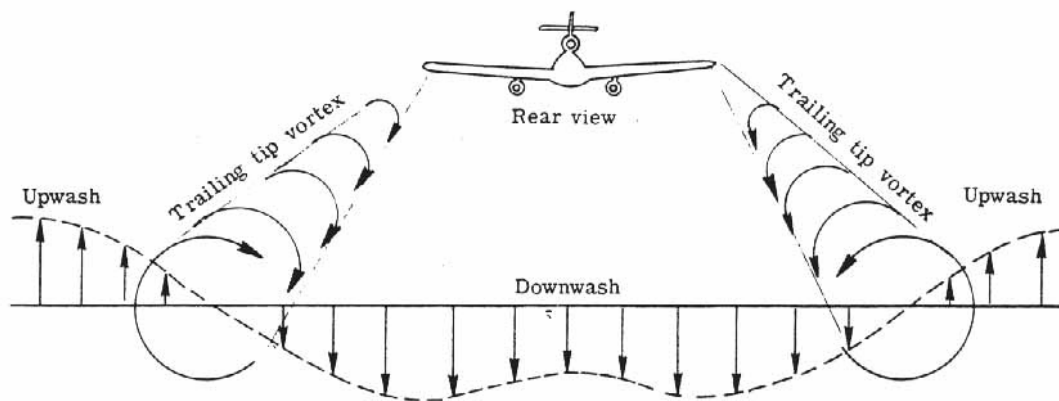


Figure 14: Creation of Downwash (reproduced from Reference 28)

Downwash produces two negative effects on the performance of a finite wing. First, it reduces the angle of attack that each section effectively sees, effective angle of attack.

Second, it creates a component of drag. This component of drag is known as induced drag and results from the kinetic energy associated with the rotation of the wing-tip vortices (2:355).

Wing-tip vortices “can significantly diminish the aerodynamic performance of a finite wing as opposed to an airfoil” (18:304). For a two-dimensional case (infinite span wing), the induced drag is equal to zero (13:2; 31). For a three-dimensional case (finite span wing) induced drag is a factor and contributes to total drag. Induced drag portion of total drag varies for various portions of flight. Induced drag becomes more prevalent at lower airspeeds for aircraft. At slow speeds, such as landing or takeoff, “wing-tip vortices may contribute about 75% of the total drag” of an aircraft. At higher speeds, such as cruise speed, wing-tip vortices contribute “about 25% of total drag” (18:304; 31).

To reduce induced drag, an aircraft can increase its aspect ratio, AR . The aspect ratio effect on induced drag is shown in Equation 7.

$$AR = \frac{C_L^2}{\pi \cdot e \cdot C_{Di}} \quad (7)$$

where AR is the aspect ratio (-), C_{Di} is the induced drag coefficient (-), C_L is the lift coefficient (-), and e is the span efficiency factor ($e = 1$ for elliptical wing).

2.5 Winglets

A winglet is best described by Jean Chattot’s quote: “Winglets are aerodynamic components placed at the tip of a wing to improve its efficiency in cruise” (7:386; 31:10). For over a century it has been known that an endplate at the tip of a finite wing reduces the spanwise flow and thereby can reduce the induced drag. However, for the endplate to

be effective, it must be “so large that the increase in wetted area drag far outweighs any drag reduction” (22:3). Unlike an endplate, a winglet does not just act as a fence against spanwise flow. “The winglet diffuses or spreads out the influence of the tip vortex such that the downwash and, in turn, the induced drag, are reduced” (22:3). A properly designed winglet can also “reduce total drag, increase lift, provide added stability, increase safety, and improve roll performance” (31:10). “Concepts for reducing wing-tip vortices have been developed and demonstrated throughout the history of aviation by individuals and companies and by the government agencies including NASA and the Air Force” (18:305; 31:11). The addition of winglets and their reduction in induced drag has been researched since the mid-1970’s when Dr. Richard Whitcomb, working at NASA Langley, first proposed them (20; 31:11). The use of winglets is widely used on many different aircraft platforms both commercially and militarily. The use of winglets has significantly reduced the amount of fuel needed for flight. “Data available for the Boeing 747-400 indicate that without winglets the aircraft suffers about 2.5 % drag losses, which corresponds to +9.5 tons at take-off” (12; 31:11).

With this reduction of induced drag there is a small cost in weight, viscous drag, and compressibility drag (17:201). These small costs are associated with the design of the winglet. The disadvantages to the use of the winglet are caused by the increase in wetted and cross-sectional area, which both cause an increase in profile drag. “The effect of the increased area is felt primarily at higher speeds, as the profile coefficient remains relatively constant while the drag increases with the square of velocity” (22:3). Optimizing winglet geometry becomes complicated due to requirement that the winglet

must maximize efficiency during the entire flight envelope (22:3). Usually when an improvement in one area of performance is made, there is a lack of consideration for its effects on other areas of aerodynamics. “An evaluation of effectiveness of various devices for the attenuation of trailing vortices was performed by Kirkman et al. It was found that while many devices show reduction of the maximum swirling velocity in the wake effects are typically accompanied by high drag penalties. Obviously, continued evolutionary advances in methods and processes are still needed in order to provide continued improvement of the aerodynamic design technologies” (18:305). In spite of all the disadvantages, many aviation manufacturers have accepted winglets as a proven fuel-saving aerodynamic device (4).

A study conducted by Smith and Campbell in 1996 showed the effect of winglets on aerodynamic efficiency of a low-aspect-ratio model with respect to lift-to-drag. The experiment has shown an approximate increase of about 6.96% for L/D at L/D_{max} as compared to no winglet case for delta wing configuration at a $Re = 1,900K$ (27:38). This value serves as a baseline for the aerodynamic efficiency of winglets for this study.

2.6 Biplanes

“Humankind’s dream of powered flight became a reality when, in 1903, the Wright brothers demonstrated that high lift and structural rigidity of the biplane was essential to lifting man and engine into the air” (1:398). Biplanes were used in the early days of aviation primarily because the structural materials could not support a monoplane design. Wing structures, as compared to modern technology, were thin and therefore; were weak and inadequate. The biplane used struts and wires to support the upper and

lower wing which gave the aircraft a box-shaped configuration. The bracing of the wings against each other strengthened the wings and allowed for shorter wingspans. This compact layout allows for greater maneuverability as compared to monoplanes. The dual wing configuration does produce more lift than a monoplane with similar wingspan. However, there is additional drag associated with the struts, wires, extra wing surface area, and the aerodynamic interference between the wings. “It is known that in a biplane the load is not distributed equally between the wings. The presence of one wing will affect the lift characteristics of the other wing” (23:1). “For a constrained wing span, however, biplanes do possess aerodynamic efficiency advantages as compared to monoplanes...the vortex drag of a biplane tends to half that of a monoplane” (29:536). However, for a constrained wing area, the monoplane holds the aerodynamic advantage (31:12). “A biplane has many advantages, such as...good load carry capability, good lift-to-drag ratio combined with a low wing loading...high lift at low speeds...(and) excellent low-speed maneuverability” (1:399).

A biplane is uniquely defined by the following important parameters: angle of decalage, gap, and stagger. “The angle of decalage is the acute angle between the chords of the wings of a biplane. The decalage shall be called positive when the lower wing has a smaller angle of attack than the upper wing” (23:2). Gap is the distance between the planes of the chords of the upper and lower wings. It is measured along a line perpendicular to the chord of the upper wing at its leading edge. Stagger is “the amount of advance of the leading edge of the upper wing...over that of a lower wing” (23:2). Stagger is measured parallel to the chord of the upper wing. Stagger is considered

positive when the upper wing is fore of the lower wing (23:3). Figure 15 shows a biplane with a few of the listed parameters.

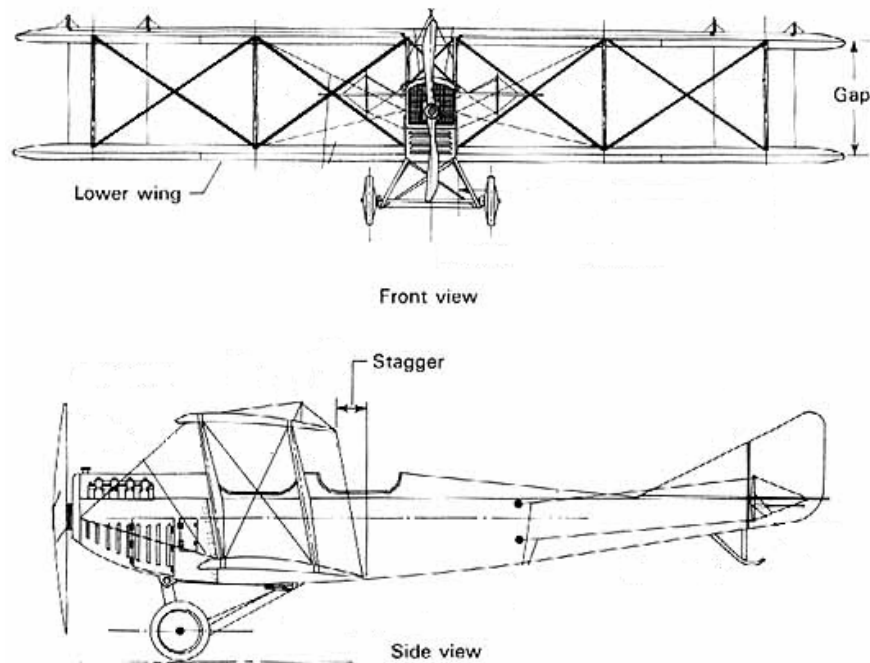


Figure 15: Biplane Parameters: Stagger and Gap (reproduced from Reference 19)

An investigation into the optimum configuration for these parameters has been conducted by two aerodynamicists, Nenadovitch and Olson (24: 6; 31:13). They concluded that a certain combination of gap, stagger, and the angle of decalage for an untwisted biplane wing design may produce lower C_D , increased C_L/C_D , and increased $C_L^{3/2}/C_D$. The optimum values are a gap of 1 chord, a stagger of 0.875 chord, and a decalage angle of -5° (24:6). “Numerical two-dimensional analysis by Rokhsaz confirmed that the combinations of gap, stagger, and decalage determined by Nenadovitch do approach optimum arrangements” (13:2).

Multiple studies have investigated the optimization of the biplane wing configuration with the use of winglets. One joint study, which consisted of efforts by Pennsylvania State University and NASA Langley Research Center, investigated the use of winglets on a box-like biplane semi-span (see Figure 16).

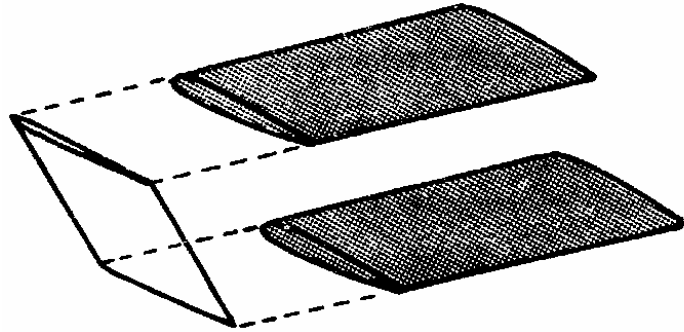


Figure 16: Isometric View of Gall's Semi-span Model (reproduced from Reference 13)

The model's wings consisted of NACA 0012 sections with constant chords of 8 inches and semi-spans of 20 inches. The airfoil that connected the two wings consisted of a constant chord, NACA 0003 section. The model was constructed to have a fixed gap and stagger that were both equal to one chord in length. The decalage angle could be varied between 0 and -5° . The results of the test revealed that there was a 5% increase in $C_{L\alpha}$ and a 4% increase in C_{Lmax} with the addition of winglets. The advantages of the winglet cannot be realized at zero lift. This is due to the induced drag being unable to overcome the increase in profile drag. It is only at lift coefficients (C_L) greater than 0.4 that winglets produce less total drag (13:3).

2.7 Joined Wings

The joined wing concept was first introduced as Patent 4,365,773 by Julian Wolkovitch in 1980. He states in his AIAA article, “The joined-wing airplane may be defined as an airplane that incorporates tandem wings arranged to form diamond shapes in both plan and front views” (33:161). Often joined wing airplanes have the rear wing attached at its root to the top of the vertical tail or the rear of the aircraft. The rear wing then sweeps forward to join the trailing edge of the swept back main forward wing (32). The rear wing acts as a unique tail and is used for pitch control, longitudinal stability, and as a structural support for the forward wing (15:215). An example of a joined-wing aircraft can be seen in Figure 17.

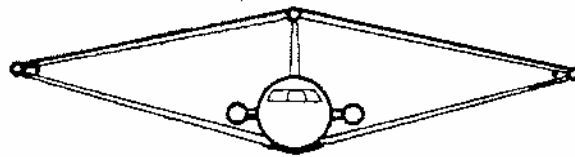


Figure 17: Front View of a Joined-Wing Aircraft (reproduced from Reference 33)

“The main concern of the early biplanes was the large profile drag due to the structural wires that connected the wings. Today, the joined-wing configurations have eliminated the connecting wires” (8:2; 31:15). Initially the use of biplanes was necessary due to the inferior strength of the structural materials in airframes. However, as material strength increased over time, the monoplane became a more efficient design as compared to a biplane. A monoplane can be designed with high aspect ratios, AR , which allows for more efficient flight (31:15). But there are limits to how high the aspect ratio can go.

Performance wise, the aircraft loses maneuverability. Structurally, the material is unable to support airframe (i.e. wingspan). The joined-wing aircraft allows for more of an increase in aspect ratio as compared to a monoplane.

As compared to an aircraft with the same wing-span, an optimally configured joined-wing aircraft has many advantages. These advantages include: lighter weight, higher stiffness, good stability and control for normal flight and stall, higher possible aspect ratios, lower induced drag, reduced wetted areas, lower total drag, suitability for thin airfoils, and higher efficiency factors (8:2; 15:215; 31:15; 33:161).

The benefits that the joined-wing can provide depend on its design goals and application. Some applications may require light weight; others may require reducing induced and parasite drag; furthermore some applications require thinner airfoils for reducing wave drag during supersonic flight (31:15; 33:175). “Joined wings are not always lighter than single wings. Weight will be saved only if the geometric parameters of the joined wing are properly chosen and if the internal wing structure is optimized” (8:2; 31:16). Although certain configurations of joined-winged aircraft will reduce drag, thus increasing aerodynamic efficiency, all flight conditions of a mission must be considered. “Performance constraints such as takeoff field length, landing field length, and climb gradient could increase the wing area required for a joined-wing configuration, thereby eliminating potential drag reduction” (14:898).

2.8 Lift-to-Drag Ratio

The lift-to-drag ratio, L/D , is a measure of aerodynamic cruise efficiency of an aircraft. As discussed in section 2.3, a propeller-driven aircraft can optimize its range by

flying at the velocity of maximum lift-to-drag, L/D_{\max} . “ L/D is usually optimized for given flight conditions (altitude) and desired lift (or aircraft weight for straight and level flight)” (31:16). At each flight condition there is a specific combination of velocity and angle of attack that maximizes the ratio of lift-to-drag. For maximum aerodynamic cruise efficiency, these values for velocity and angle of attack should be flown for the given flight condition. Table 1 lists historic values of lift-to-drag for common aircraft. Notice that L/D_{\max} is generally bounded from 8 to 20.

Table 1: Lift-to-Drag Ratios of Historical Aircraft (reproduced from Reference 12)

| Type of Aircraft | L/D Ratio | Subsonic Aircraft | L/D_{\max} |
|-------------------------------------|-----------|-----------------------|--------------|
| Supersonic Jet Transport (Concorde) | 8 | Boeing B707-320 | 19.4 |
| Tilt-rotor aircraft | 9 to 10 | Douglas DC-8 | 17.9 |
| New Supersonic Transport* | 15 | Airbus A320 | 17 |
| Oblique Flying Wing* | 16 to 17 | Boeing 767-200 | 19 |
| Subsonic Jet Transport | 16 to 18 | Boeing 747-100 | 17.7 |
| Bomber B-52 | 20 | Douglas DC-10 | 17.7 |
| * Estimated data | | Lockeed Tristar L1011 | 17 |
| | | Douglas DC-9 (1966) | 16.5 |
| | | Boeing B727-200 | 16.4 |
| | | Fokker 50 (1966) | 16 |
| | | Douglas DC-3 (1935) | 14.7 |
| | | Ford Trimotor (1927) | 12 |
| | | Wright Flyer I (1903) | 8.3 |

Figure 18 shows the historical trend of maximum lift-to-drag ratio for propeller-driven aircraft. During the years from 1920 to the early 1930’s there is a sharp increase in the L/D_{\max} upper bound curve. This increase in L/D_{\max} is a result of the reduction in parasitic drag, the advancement of structural materials, and the switch from the biplane to the monoplane (with its higher aspect ratio). The reduction in parasite drag is due to the advancement in aerodynamic design (i.e. a strut-and-wire-braced biplane to the streamlined, internally braced monoplane) (19; 31:17).

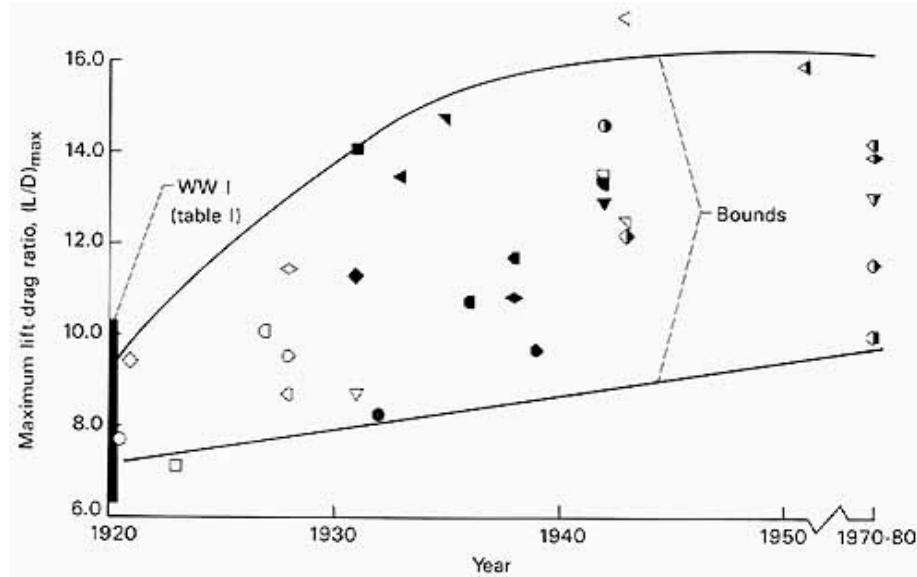


Figure 18: Historic Maximum Lift-to-Drag Ratios of Propeller-Driven Aircraft (reproduced from Reference 19)

Another measure of aerodynamic efficiency is the effective aspect ratio, eAR . The effective aspect ratio of an aircraft can be solved with Equation (8) and with additional information concerning lift and induced drag.

$$C_{D_i} = \frac{C_L^2}{\pi \cdot e \cdot AR} \quad (8)$$

where C_{D_i} is the induced drag coefficient, C_L is the lift coefficient, e is the span efficiency factor, AR is the aspect ratio, and the combination of $e AR$ is the effective aspect ratio (17:186; 31:18).

2.9 Hot-Wire Anemometry

A constant temperature anemometer (CTA) is used as one method for fluid flow data acquisition. A CTA maintains a constant wire temperature through the use of a control algorithm. A CTA also has constant resistance. As electric current is supplied to

the wire to maintain the temperature, the rate of current is measured. The air velocity is directly related to the amount of current needed to maintain the temperature in the wire. Therefore, as the velocity of the fluid changes, the controller must increase or decrease the supplied current to the constant wire resistance (thereby keeping temperature constant). The change in current is measured and calibrated, and further processing of the data converts it into a fluid velocity. “Two advantageous reasons for using a CTA are accuracy and high time-dependent resolution. The latter reason lends itself to use in collecting and analyzing turbulent flow data” (31:18).

2.10 SolidWorks®

SolidWorks is a three-dimensional computer-aided-design program, CAD. The program currently only runs on Windows-based personal computer (PC) systems. *SolidWorks* was developed in 1993 and is produced by Solid Works Corporation located in Concord, Massachusetts. *SolidWorks* utilizes a parametric, feature-based approach to the construction of models. Parameters refer to the constraints that determine size, shape, behavior, and characteristics that make up a model. Parameters can be numerical (length, width, etc) or geometric (tangent, concentric, parallel, etc). Features are the building blocks of the part. They are the shapes and operations of the part. Shapes are the functions that either add or subtract material from the part (holes, bosses, etc). Shapes usually require the use of sketches before the operation is carried out. Operations are the functions that do not require sketches but still affect the part (fillets, shelling, etc) (26).

To construct a part in *SolidWorks*, the first step usually is creating a two or three-dimensional sketch. The sketch consists of geometry (lines, arcs, etc) and then

dimensions are assigned to define the location and size of the geometry. The geometry can also have relational constraints (parallel, concentric, etc) that further define the part. A complicated design involves the use of multiple parts and is constructed in the assembly. The assembly works in the same manner as the part construction by assigning numerical and geometric parameters between parts. Finally, the model can be drafted using the drawing module of *SolidWorks*. See Figure 19 for an empty *SolidWorks* part workspace.

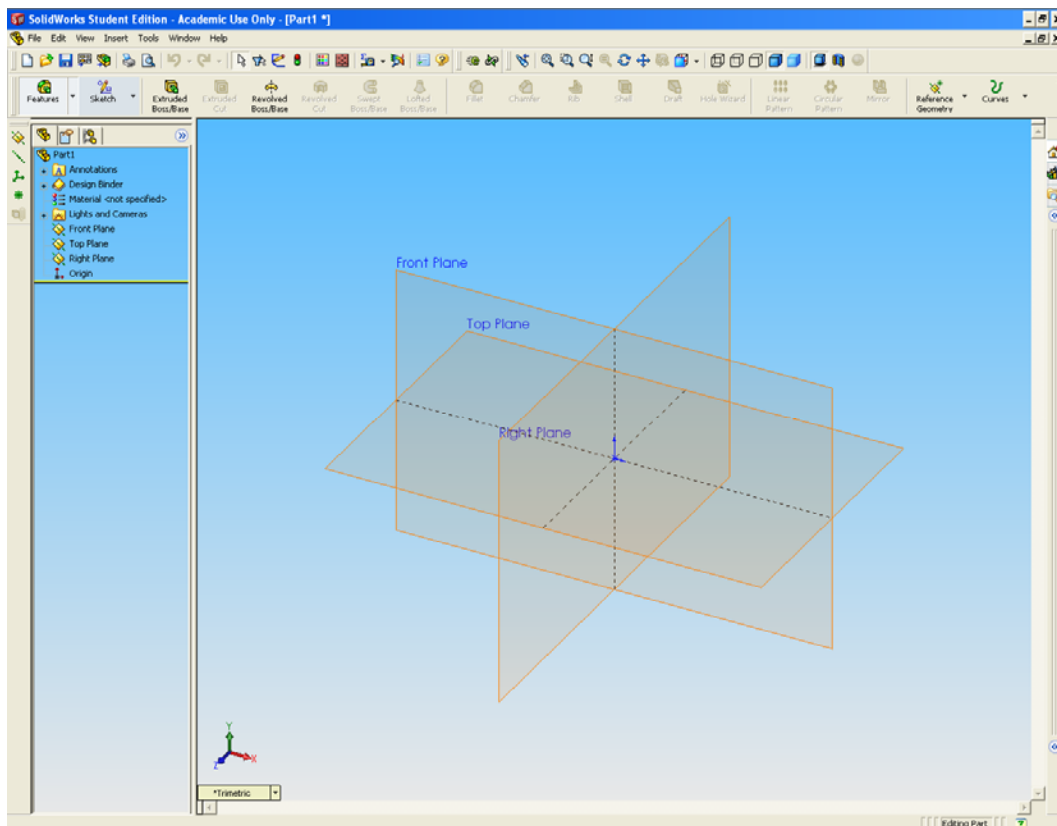


Figure 19: Planes and Axes of an Empty *SolidWorks* Part Workspace

SolidWorks in tandem with a rapid prototype machine, such as an Objet Eden series printer described in Section 3.2.11, allows for a relatively quick design to build process for any type of model.

III. Methodology

3.1 Chapter Overview

The beginning of this chapter outlines the instructions for the construction of the Original Configuration Model in SolidWorks. After that, all the model configurations that were constructed using the previously outlined method are presented in detail. Next, the chapter covers the AFIT low-speed wind tunnel and the subsequent test data that was retrieved from the tunnel α sweeps. The methods for reducing the data from these tests are also covered in this chapter. Furthermore, this chapter covers the 24" Houck Configuration data that will be used for comparison to this study. Finally, the test plan that was used to collect data is outlined.

3.2 *SolidWorks* Construction

3.2.1 Patent Specification

The models used for this study were designed using the CAD program *SolidWorks*. The model construction followed the claims specified in Ronald G. Houck II's Lifting Foil patent. More specifically, the flow guide in the model followed Claim 14 and 17, whereby the camber of the flow guide has maximum camber at the upper and lower wing-tips and has minimum camber at the mid-point of the flow guide (Figure 20) (16).

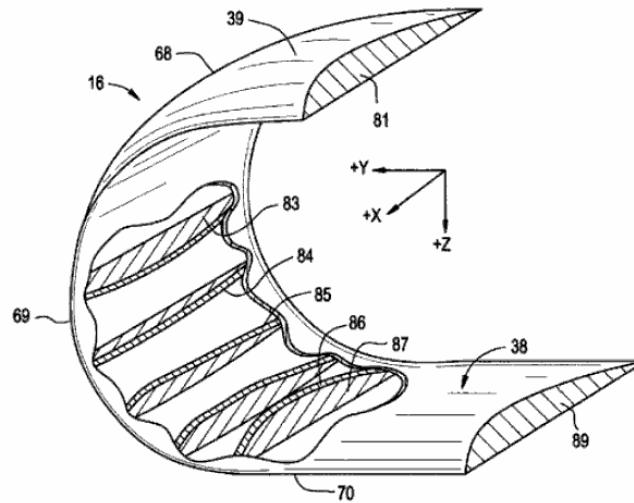


Figure 20: Progressive Camber of the Flow Guide (reproduced from Reference 16)

3.2.2 Step 1: Airfoil

The initial construction of the base model, or original configuration, began with the selection of a NACA 2412 airfoil for the biplane wings from the UIUC Airfoil Coordinate Database (30). The airfoil coordinates provided were of unit length but were resized to be three times larger (chord length of 3"). The airfoil coordinates were entered on the Y-Z sketch plane and then were splined together (Figure 21).

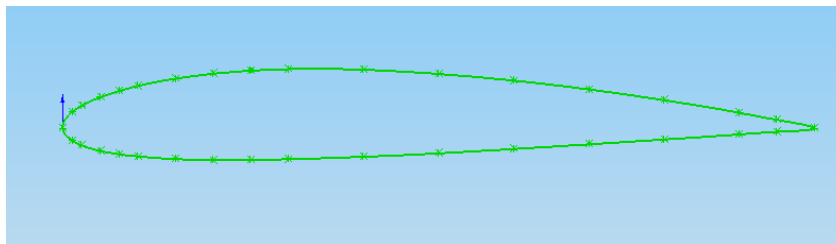


Figure 21: NACA 2412 Coordinates Splined Together in *SolidWorks*

3.2.3 Step 2: Airfoil Section Extrusion

The next step in the construction was to extrude the airfoil section with a 15° sweep and a 6.69" half-span. For this to be done, another sketch was added to guide the airfoil section extrusion (Figure 22 and Figure 23).

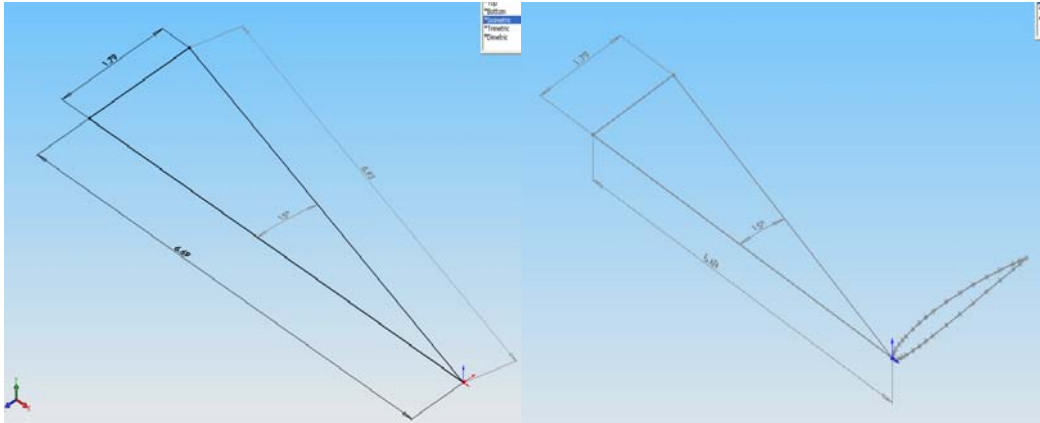


Figure 22: Sketch to Guide Airfoil Section in *SolidWorks*

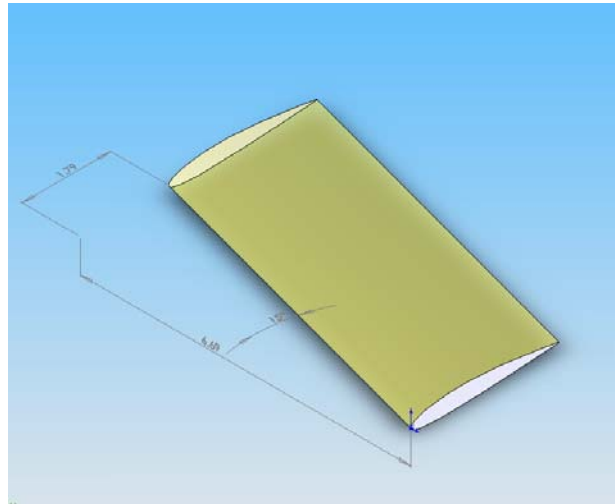


Figure 23: Sketch to Guide Airfoil Section in *SolidWorks*

3.2.4 Step 3: Upper Wing Construction

To add the upper wing, a gap of 2.5" ($0.84 \bar{c}$) was measured from the leading edge of the wing-tip. The airfoil coordinates for the upper wing were entered using a

similar method outlined in Step 1 (Figure 24). The sketch plane was the wing-tip surface plane.

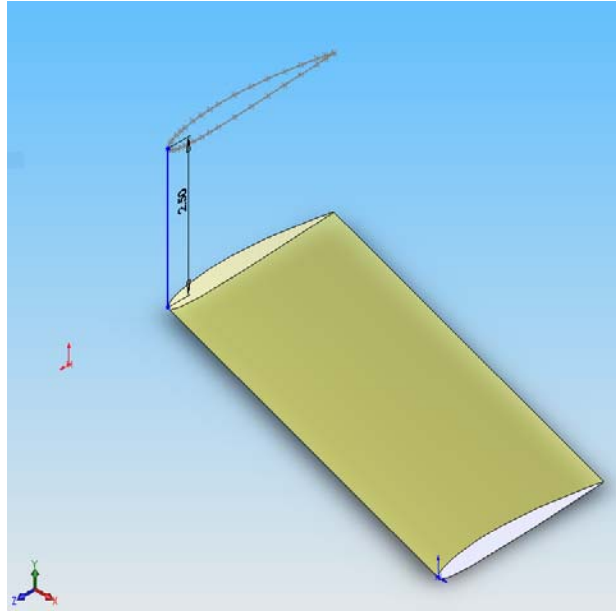


Figure 24: Gap Measurement for Upper Wing

To extrude the airfoil section with a 15° sweep and a 6.69" half-span, in the opposite direction to the lower wing, another guide sketch was added (Figure 25).

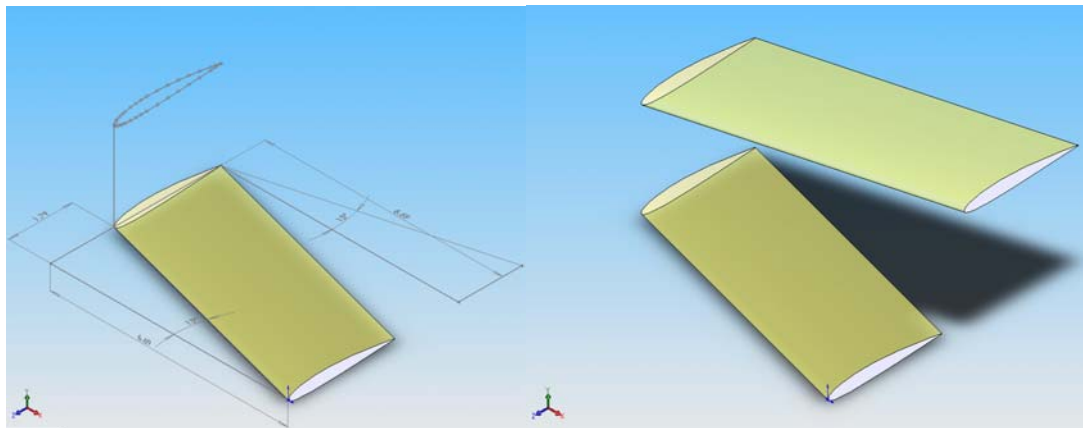


Figure 25: Upper Wing Guide Sketch and Subsequent Extrusion

3.2.5 Step 4: Mirroring the Extrusions

In order to make the model symmetric, the upper and lower wings were mirrored in the Y-Z plane (see Figure 26).

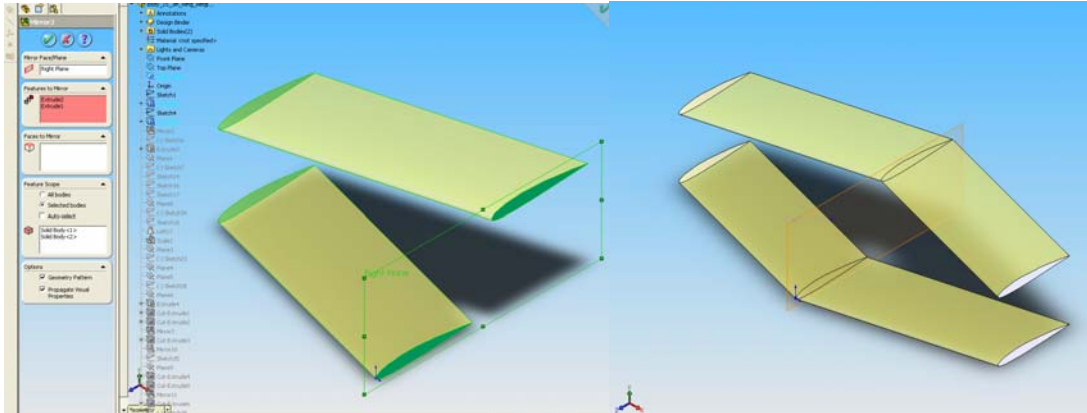


Figure 26: Mirroring over the Y-Z Plane

3.2.6 Step 5: Creating the Body that Joins the Wings

The center body that joins the wings is a NACA 0010 airfoil section that was extruded from the lower wing to the upper wing along the mid-span. The initial step was to enter the airfoil coordinates (from UIUC Airfoil Coordinate Database) in the X-Z sketch plane on the lower wing (3" chord length). Another sketch was added to guide the extrusion from lower wing leading edge to the upper wing leading edge (Figure 27).

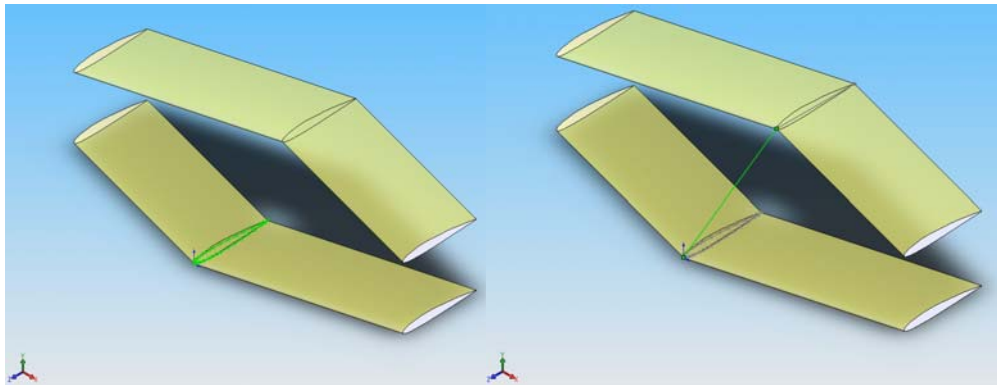


Figure 27: Body Airfoil and Guide Sketch

The extrusion of the NACA 0010 airfoil section is shown in Figure 28.

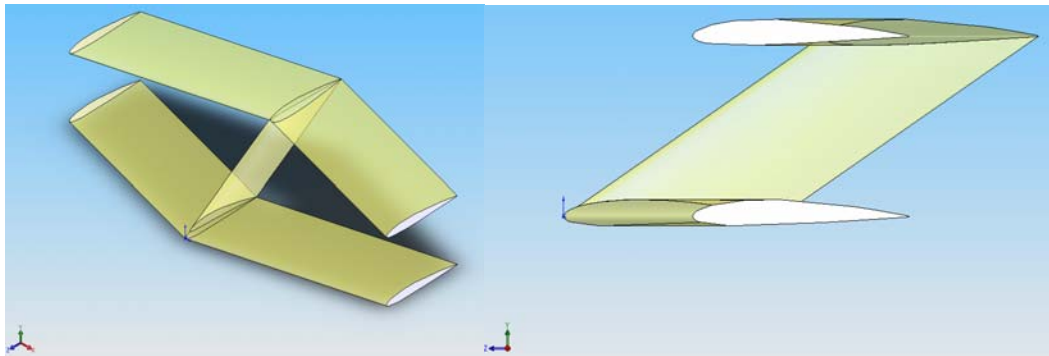


Figure 28: Extrusion of NACA 0010 Airfoil Body Section, Isometric and Side View

3.2.7 Step 6: Creating the Flow Guides that Join the Wings

The initial step for the construction of the Flow Guides was to create the sketch that would guide the lofting between the wings. The guide begins by sketching on the wing-tips of the upper and lower wings (parallel to the Y-Z plane). The points mid-chord on both wing-tips are joined by a guide line (Figure 29).

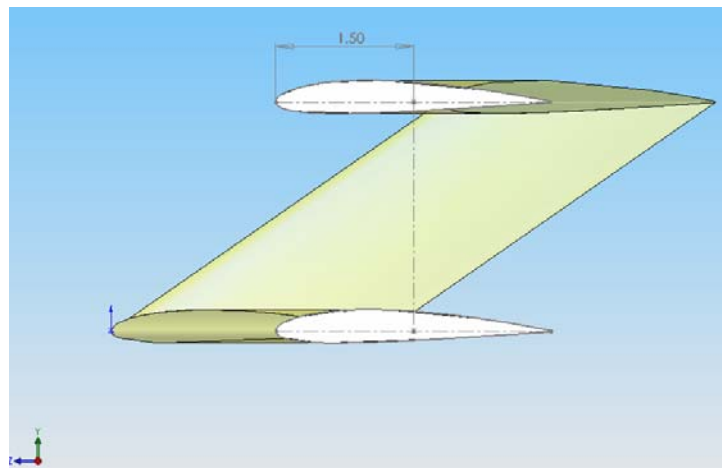


Figure 29: Connecting Mid-Chord Points on Upper and Lower Wing-Tips

Once the guide line has been drawn, the next step is to create a plane on the line that is parallel to the X-Y axis. After the plane is created, the guide sketch for loft is drawn. It is

a semi-circle with a radius of 1.25" and has guide lines drawn from 0° to 180° every 45° that originate from the center (Figure 30).

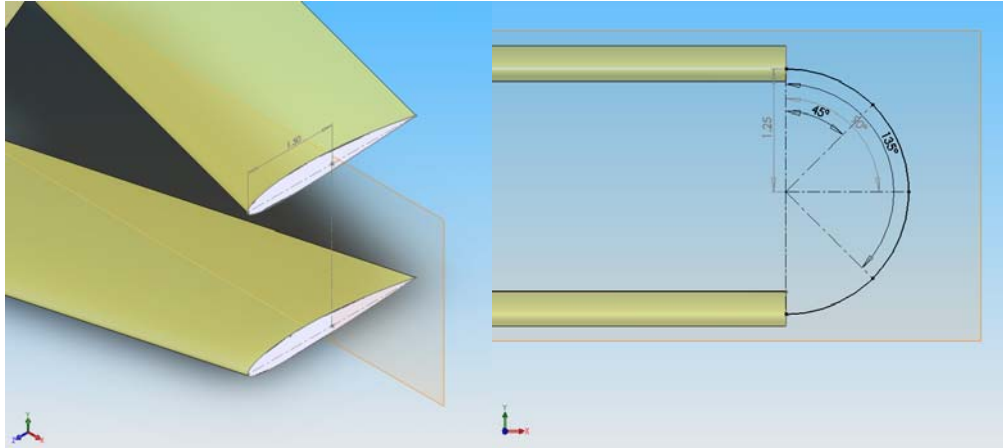


Figure 30: Guide Plane and Sketch for Flow Guide Loft

The next step is to loft the Flow Guide. Using the Loft command, select the upper and lower wing-tips' faces. Set the tangent length to 2 and complete the lofting (Figure 31).

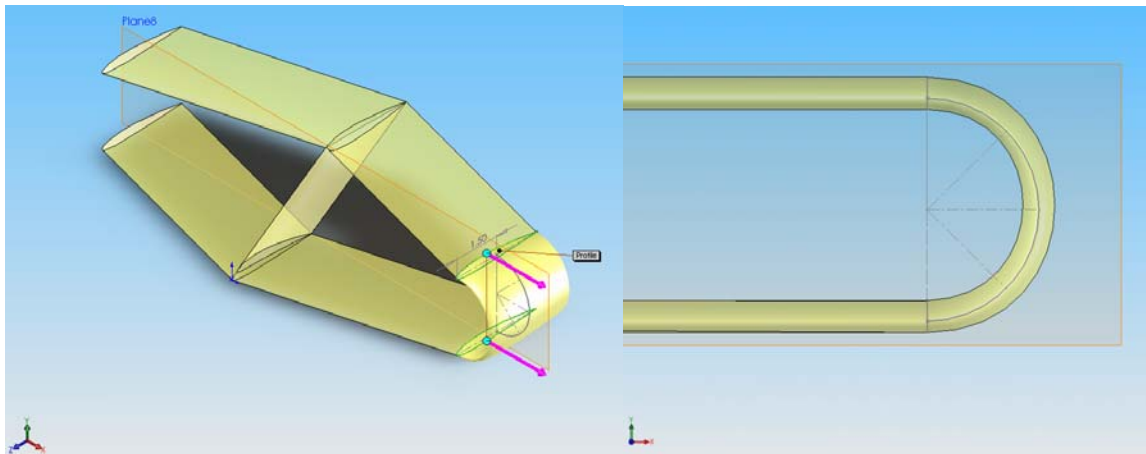


Figure 31: Lofting of the Flow Guide and the Comparison to the Guide Sketch

To finalize the lofting, the Flow Guide was mirrored in the Y-Z plane so the opposite wing would have symmetry (Figure 32).

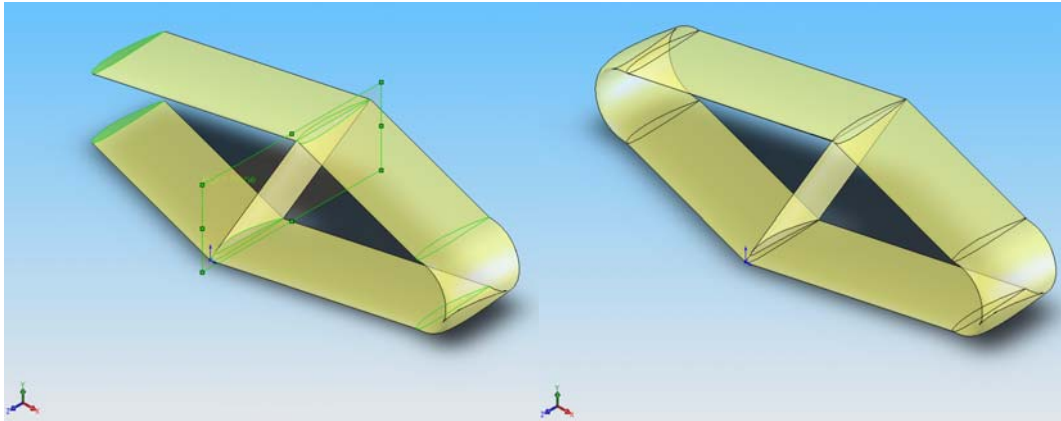


Figure 32: Mirroring the Flow Guide in the Y-Z Plane

3.2.8 Step 7: Scaling the Model

The model was resized so that the scale would be compatible with the wind tunnel. The scale of the model was set to 0.85 and it was uniformly scaled (Figure 33).

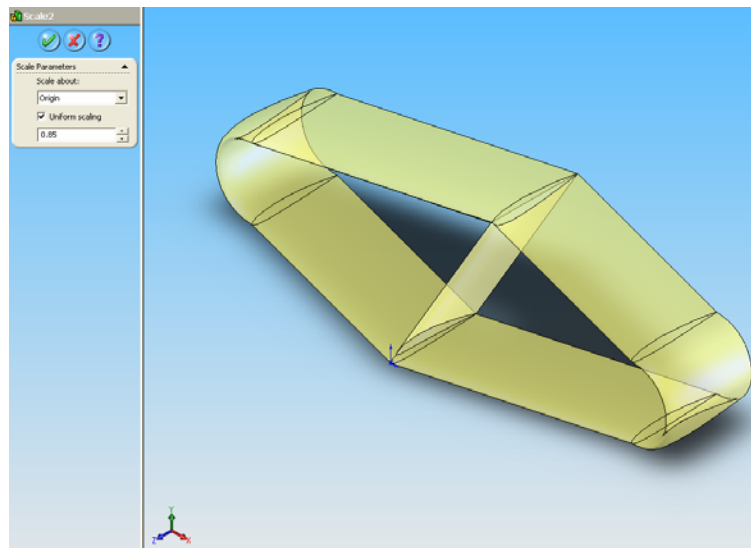


Figure 33: Uniform Scaling of the Model

3.2.9 Step 8: Adding the Balance Attachment

The initial step for the balance attachment is to sketch the mid-point for the sting in the model. It is located +0.53" in the Y-axis from the lower wing leading edge (Figure 34).

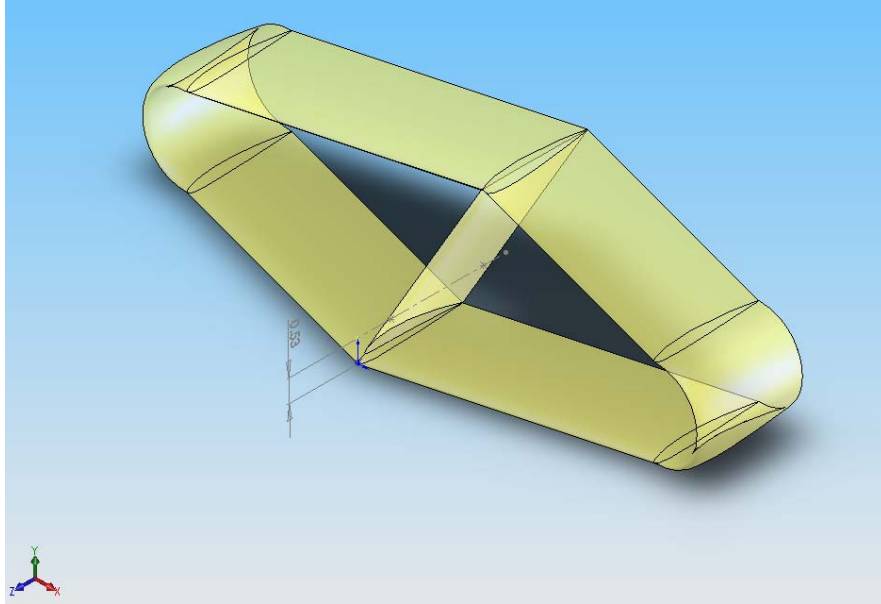


Figure 34: Sketch of the Mid-Point for the Balance

Once the mid-point is located, the guide-line for the center of the balance cylinder is drawn along the body parallel to the Z-axis. The following dimensions are needed to construct the balance attachment on the model. The plane for sketching the balance attachment's geometry is located 1.05" from the leading edge of the body that intersects the guide-line and is parallel to the X-Y plane. On this sketch plane, the diameter of the circle for the balance attachment is 1" and the center is located on the guide-line (Figure 35).

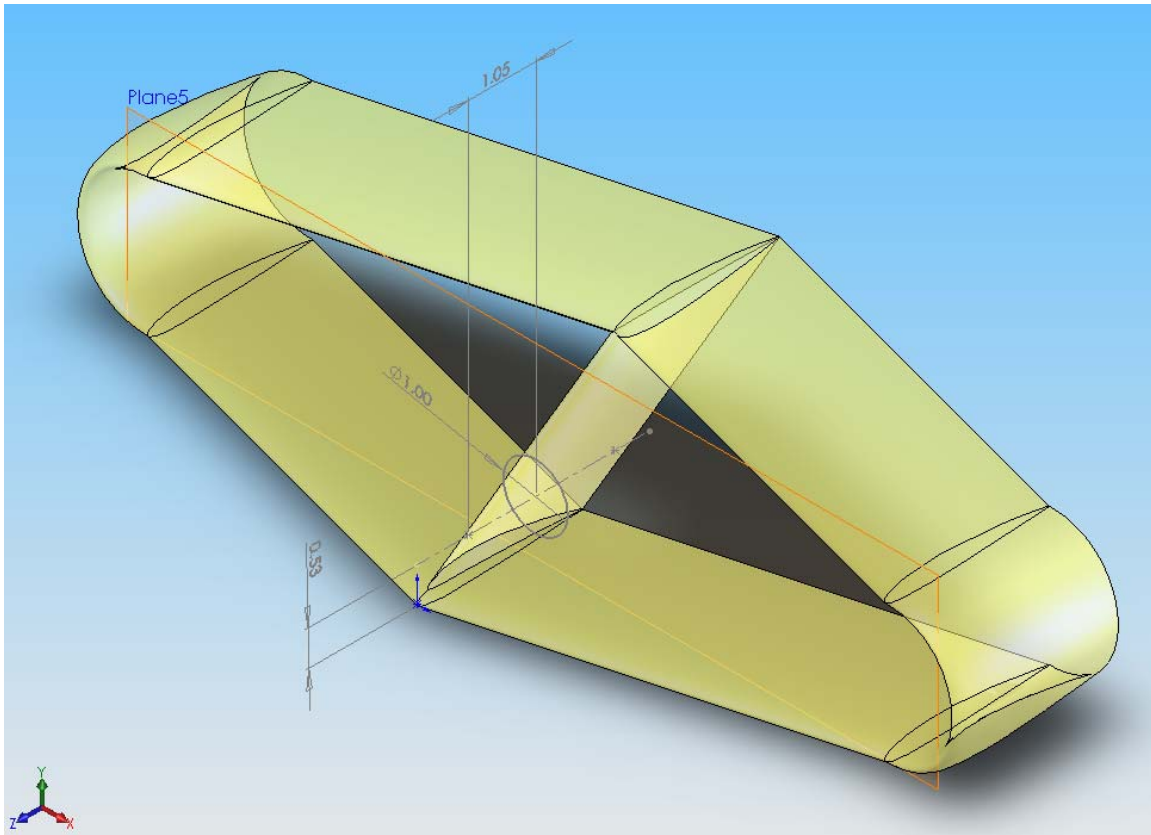


Figure 35: Sketch Plane and Geometry for the Sting Attachment Cylinder

The circle for the balance attachment is extruded out to 2.2" to the trailing edge of the body and tapered to a point 1" towards the leading edge of the body (Figure 36).

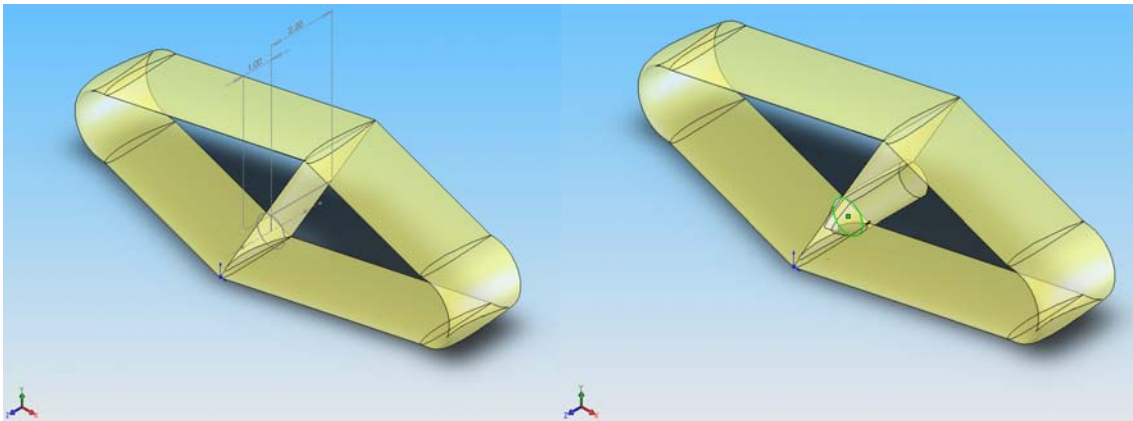


Figure 36: Extrusion of the Balance Attachment

The next step for the balance attachment is to cut out a cylinder so the balance can slide into the balance attachment. The sketch for the balance cutout is at the back of the model where the balance attachment juts out. The center of the circle is on the guide-line and the diameter is 0.5". The depth of the cutout is 2.2" (Figure 37).

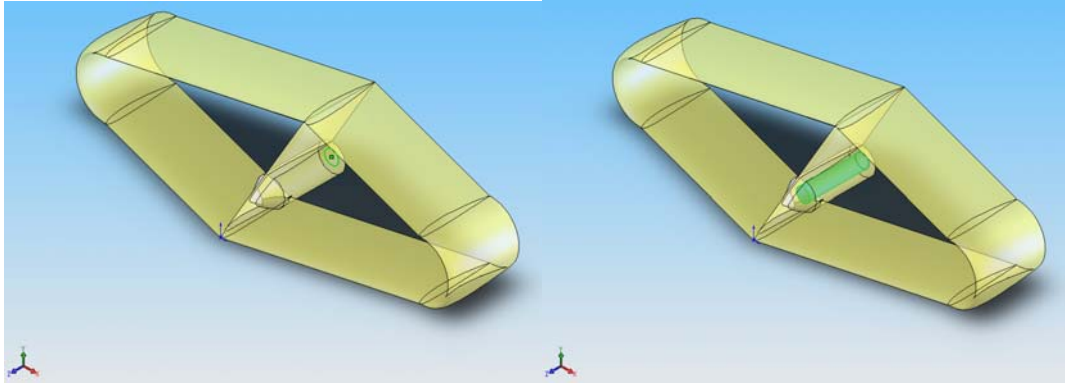


Figure 37: Cutout for the Balance

The final step for the balance attachment is to create the screw holes in the model so it can be affixed to the balance. The sides of the balance are cut, with a square drawing offset 0.46", so that they can be flat and then it is mirrored about the Y-Z plane for symmetry (Figure 38).

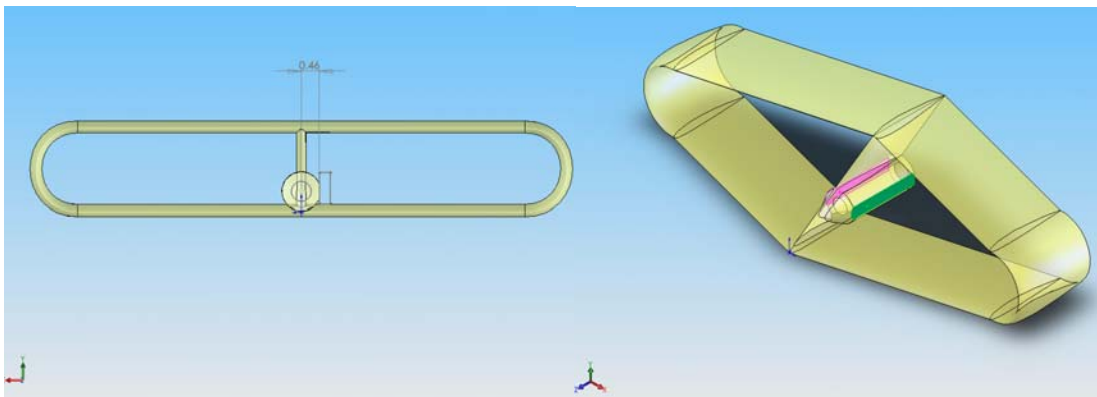


Figure 38: Flat Sides of the Balance Attachment

The screw hole is sketched on the origin's Y-Z plane. The center of the circle is located on the guide-line used for the balance attachment and is 1.25" from the leading edge of the body. The diameter of the circle is 0.09" (Figure 39).

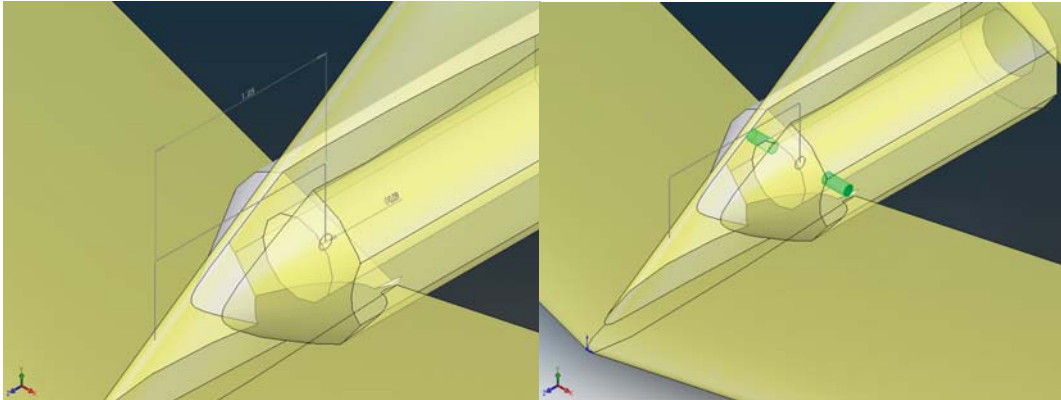


Figure 39: Hole Cutouts for the Balance Screws

The final screw hole for attachment is located on the underside of the model. It is cut in a similar method through the bottom of the model (Figure 40).

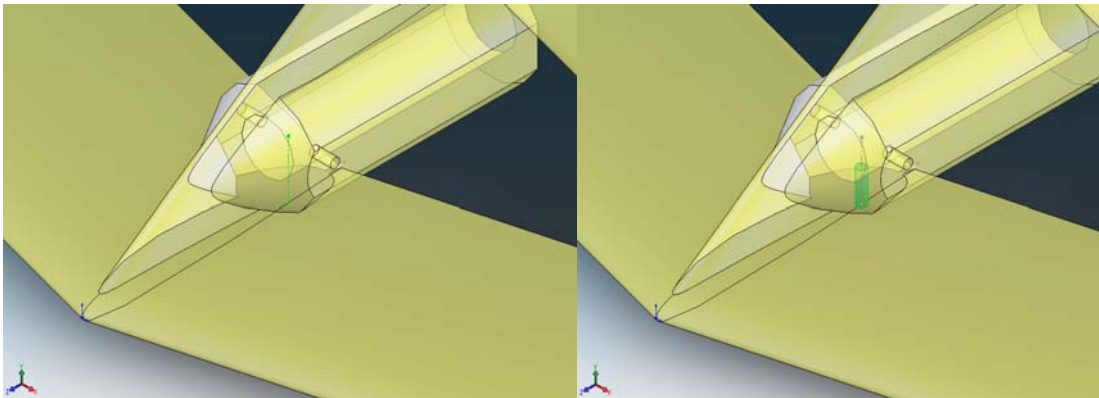


Figure 40: Bottom Hole Cutouts for the Balance Screws

Each of the holes has a counter-bore diameter of 0.14" and a depth of 0.095" (Figure 41).

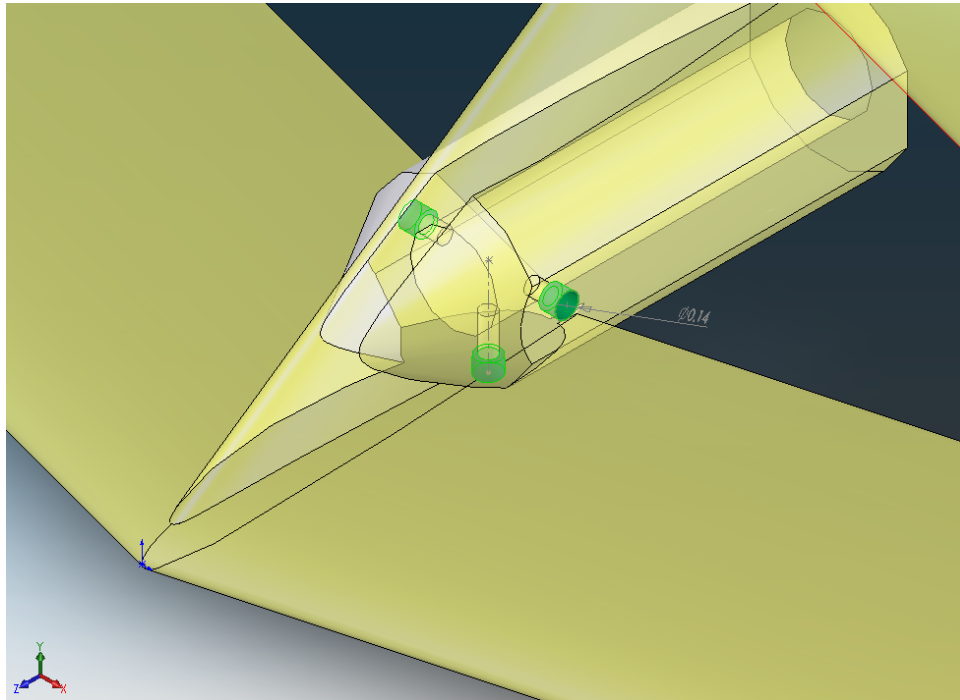


Figure 41: Counter-Bores for the Sting Attachment Holes

3.2.10 Step 9: Final Review before 3-D Printing

The final step before the build is to review the Original Configuration Model (Figure 42).

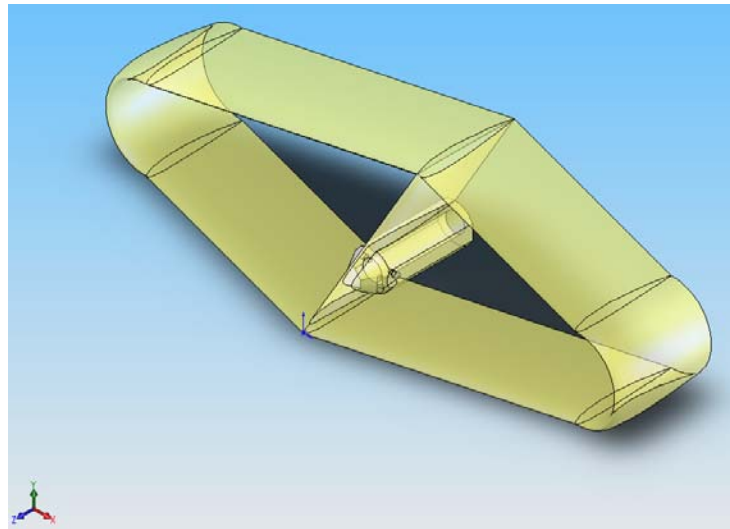


Figure 42: Final Review of the Original Configuration Model

3.2.11 Step 10: 3-D Printing

The initial step of the building process is to save the *SolidWorks* part file as a STL file. The file export options should be set as follows: output as ASCII and resolution as fine (Figure 43).

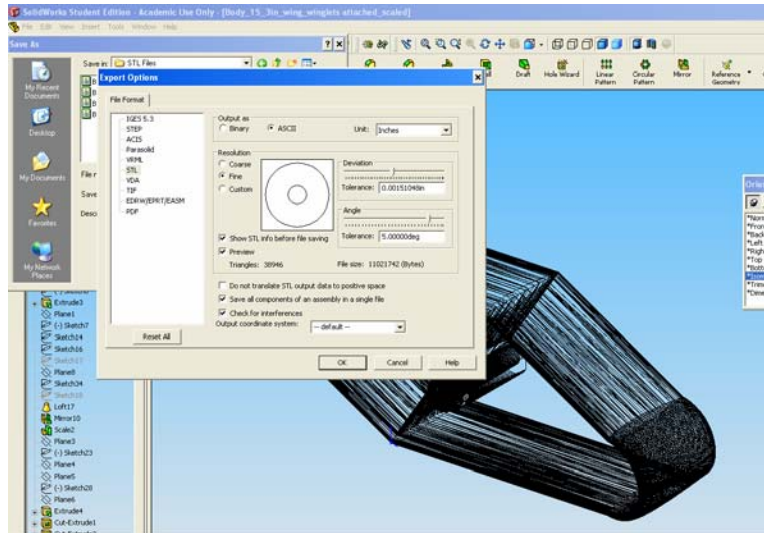


Figure 43: Export Options of the Part to STL File Save

Once the file has been converted to an STL file, it now can be built by the Objet Eden 333 series printer. The printer builds the model by layering acrylic with a print-head on a tray that drops along the z-axis. The acrylic is cured by the UV lamps that are built into the printer head (Figure 46).



Figure 44: The Objet Eden 333 Printer and the Printer Head during the Build Process

The build process for one model is approximately 26 hours. Each model requires approximately 1300 grams of support material and 500 grams of build material. Once the model is built, the support material is pressure washed away and the Original Configuration Model is complete (Figure 45).



Figure 45: The Completed Original Configuration Model

3.3 Models

3.3.1 Original Configuration Model

The Original Configuration Model was constructed according to the construction method outlined in Chapter 3.2. The aircraft parameters can be seen in Figure 46. The length of the Original Configuration Model is 5.59". The wingspan (b) is 13.808". The chord of the upper and lower wing is 2.55" and is uniform throughout each wing ($\bar{c} = 2.55$ "). The planform area (S) is 72.58 in² which included the planform areas of the upper and lower wing, and the areas of the Flow Guides. The aspect ratio, AR , was calculated for a monoplane and biplane and is as follows: $AR_{\text{mono}} = 2.63$ and $AR_{\text{bi}} = 5.26$. The aspect ratios for the rest of the models are calculated in Section 4.3.5. The volume of the aircraft is 17.78 in³. The lower wing has a leading edge sweep angle of 15°. The upper wing has a leading edge sweep angle of -15°. The distance between the leading edge of the upper and lower wing is 2.13". If biplane parameters were applied to the Original Configuration Model, it would have a gap of $0.84\bar{c}$, a stagger of $-1.2\bar{c}$, and a decalage angle of 0°. The aspect ratio of this model and each subsequent model was not calculated due to the numerous definitions available for different wing configurations (e.g., monoplane, biplane, and joined-wing). However in Section 4.3 the effective aspect ratio for each model is calculated.

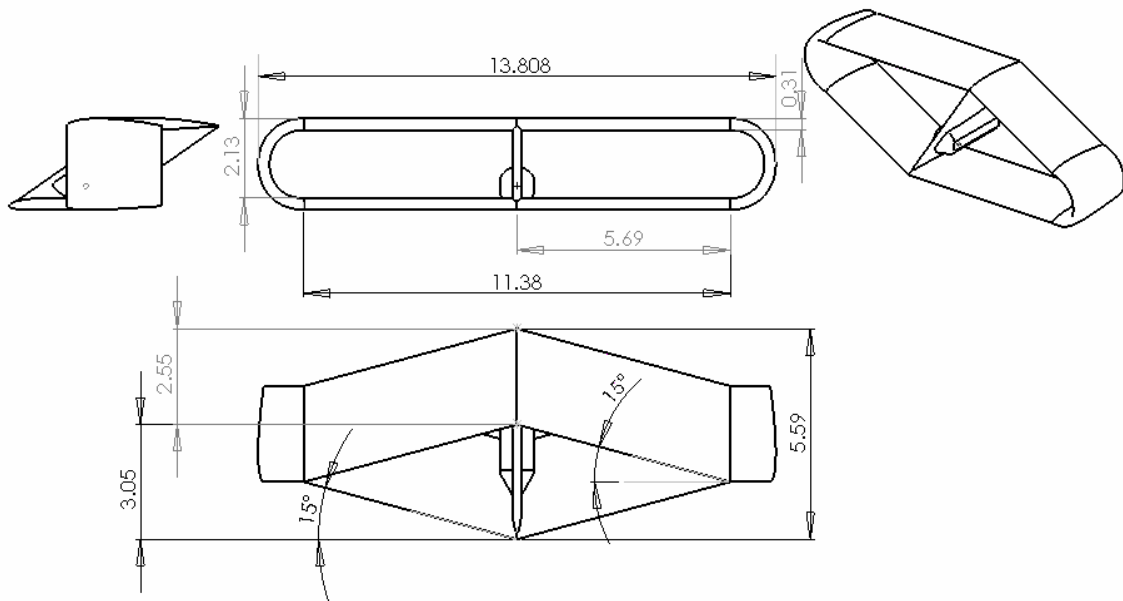


Figure 46: Left, Front, Top, and Isometric Views of the Original Configuration Model with Dimensions (in)

3.3.2 Original Configuration Model Flow Guides

The Flow Guides of the Original Configuration Model have been built to the description in Claim 17 of the Lifting Foil patent. The camber of the flow guide has maximum camber at the upper and lower wing-tips and has minimum camber at the mid-point of the flow guide. The Original Configuration Flow Guide has maximum camber at the upper and lower wing-tips (Figure 47).

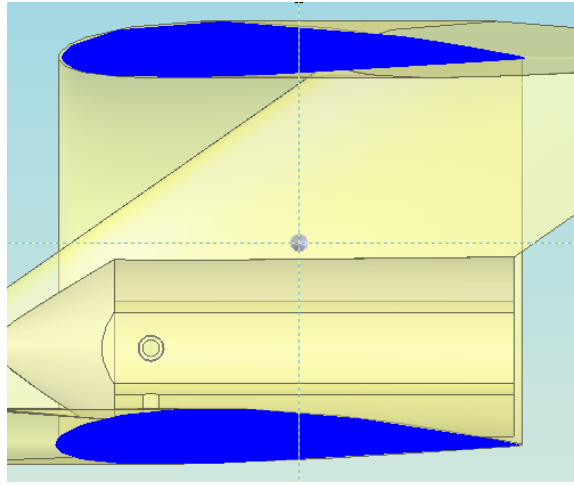


Figure 47: Maximum Camber of Flow Guide at Upper and Lower Wings

From the upper wing, the camber gradually (linearly with arc length) diminishes until it reaches the mid-point of the flow guide (Figure 48).

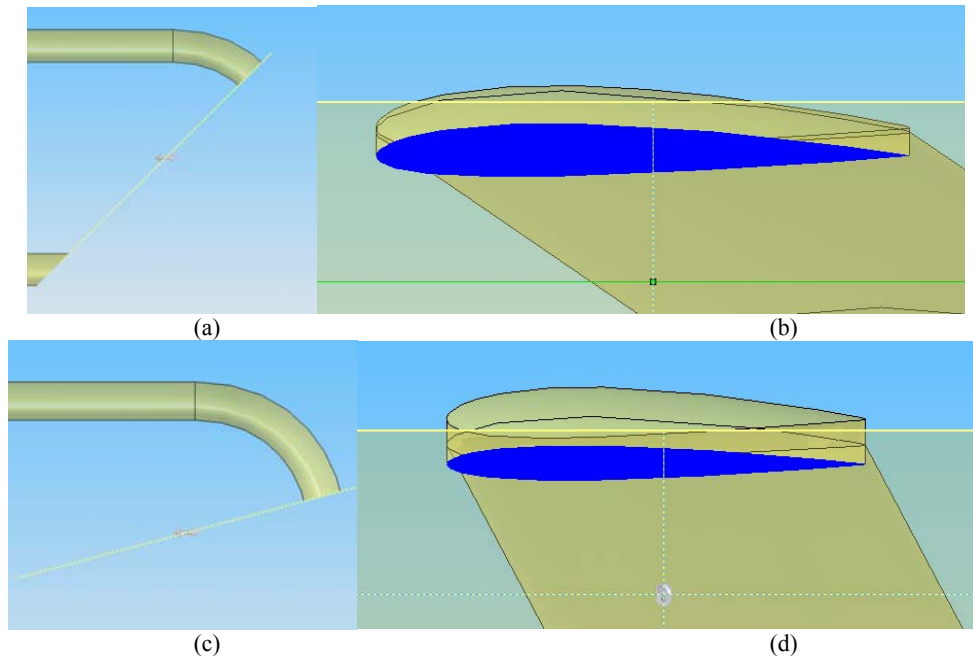


Figure 48: Gradually Diminishing Camber of the Airfoil on the Flow Guide

(a) Front view of 45° Cut of Flow Guide, (b) Airfoil of 45° Cut,
(c) Front view of 75° Cut of Flow Guide, (d) Airfoil of 75° Cut

Once at the midpoint of the flow guide, the flow guide has zero camber (symmetrical airfoil) (Figure 49).

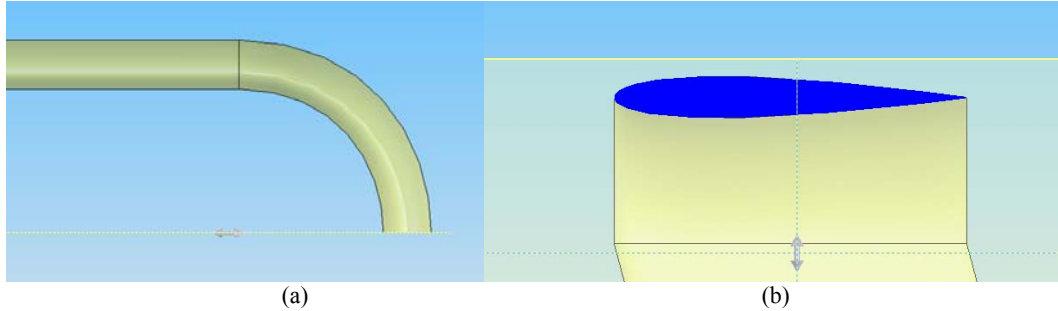


Figure 49: Symmetrical Airfoil at the Midpoint of the Flow Guide
(a) Front view of 90° Cut of Flow Guide, (b) Airfoil of 90° Cut

Past the midpoint of the flow guide, the camber continues to diminish negatively; however, from the lower wing perspective the camber is increasing (Figure 50).

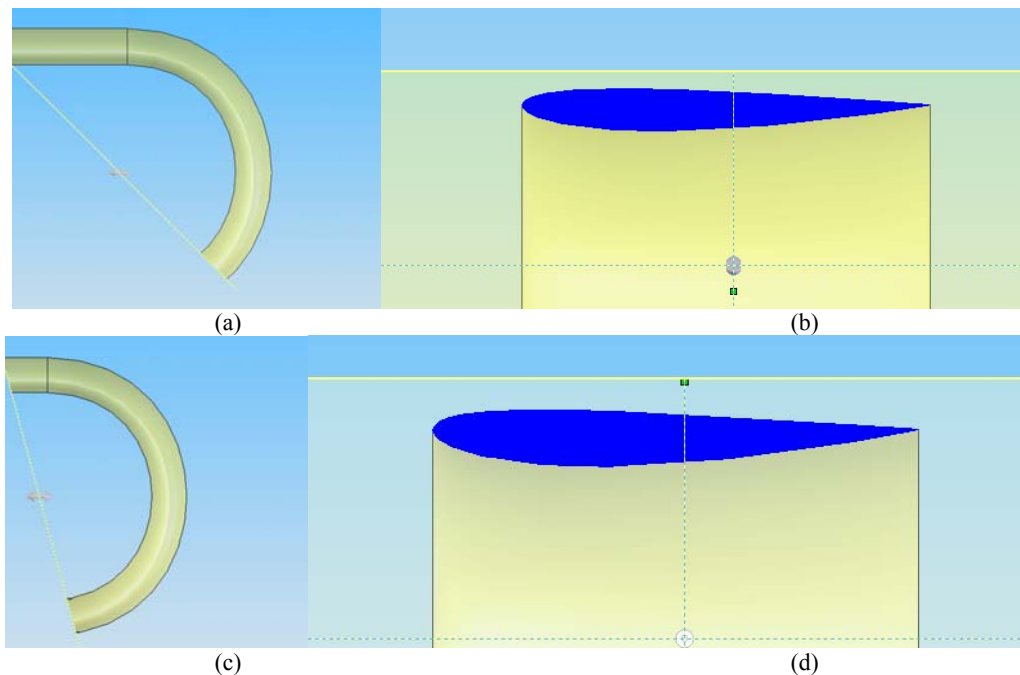


Figure 50: Past Midpoint: Gradually Diminishing Camber of the Airfoil on the Flow Guide
(a) Front view of 135° Cut of Flow Guide, (b) Airfoil of 135° Cut,
(c) Front view of 165° Cut of Flow Guide, (d) Airfoil of 165° Cut

Once the flow guide attaches to the lower wing, it is at maximum camber and is identical to the lower wing airfoil (Figure 47: Lower Wing). The comparison of the patent claim and the constructed flow guide is shown in Figure 51 (16)

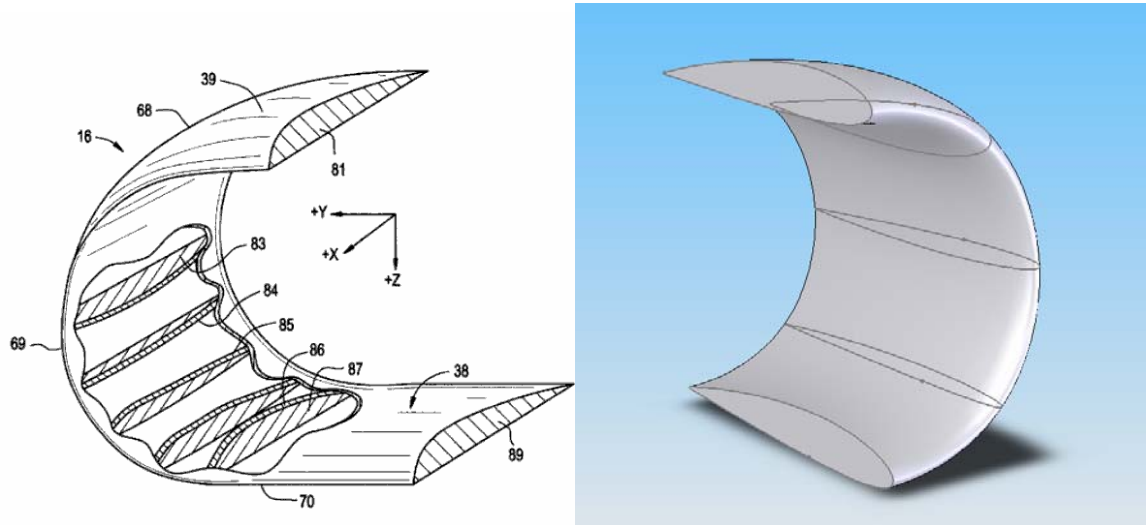


Figure 51: Comparison of the Houck Patent Claim 17 and the Original Configuration Flow Guide (reproduced from Reference 16)

3.3.3 Positive 5° Canted Flow Guide Model

The Positive 5° Canted Flow Guide Model (+ 5° Model) was built according to the same method for the Original Model except that the Flow Guides were altered with a + 5° cant in the airfoils located at the 45° and 135° planes (Figure 52).

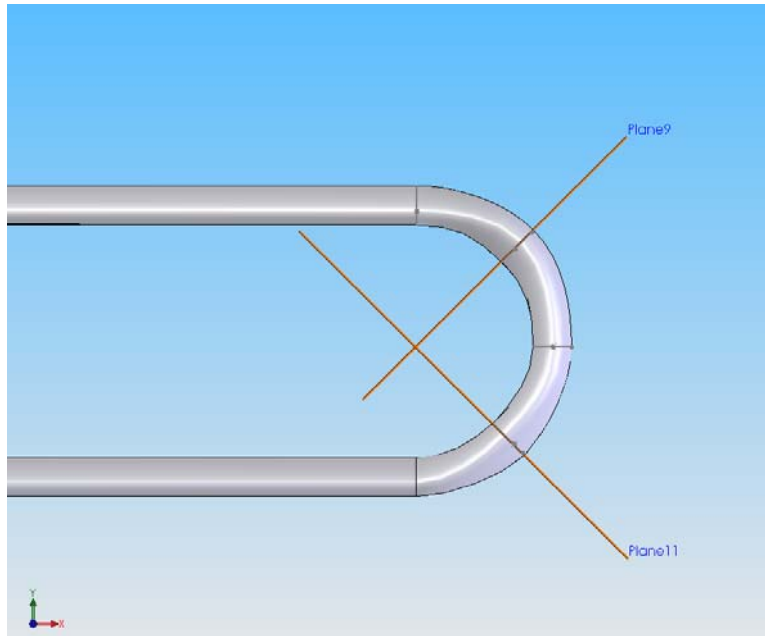


Figure 52: The 45° and 135° planes where the Canted Airfoils are Located

The + 5° cant was accomplished in *SolidWorks* by rotating the airfoils 5° in the clockwise direction about the mid-chord (Figure 53).

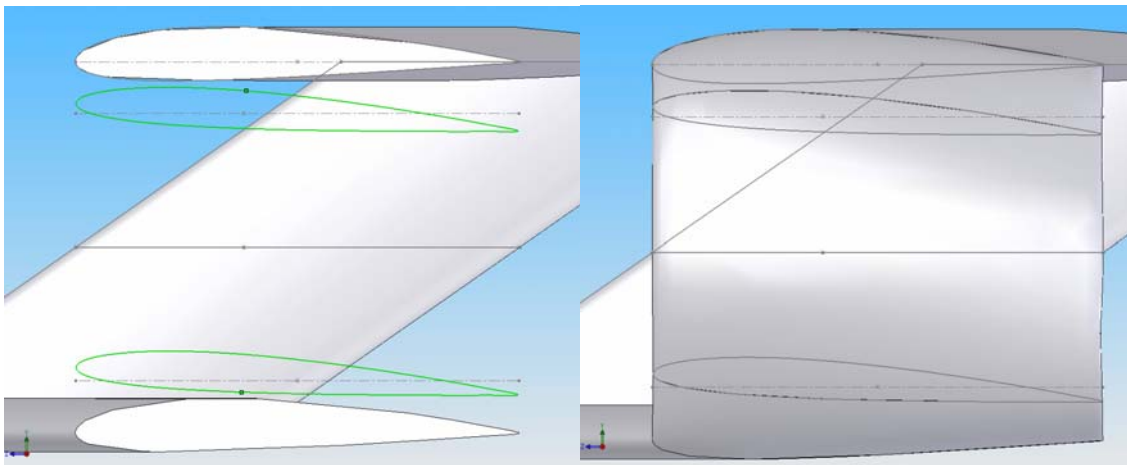


Figure 53: The Rotated Airfoils and Subsequent +5° Canted Airfoil

The aircraft views for the + 5° Model can be seen in Figure 54 and Figure 55. The + 5° Model differs from the Original Configuration Model with the following parameters. The

wingspan (b) is 13.806". The planform area (S) is 72.56in² and is calculated the same way as the Original Configuration Model. The volume of the model is 17.74 in³.

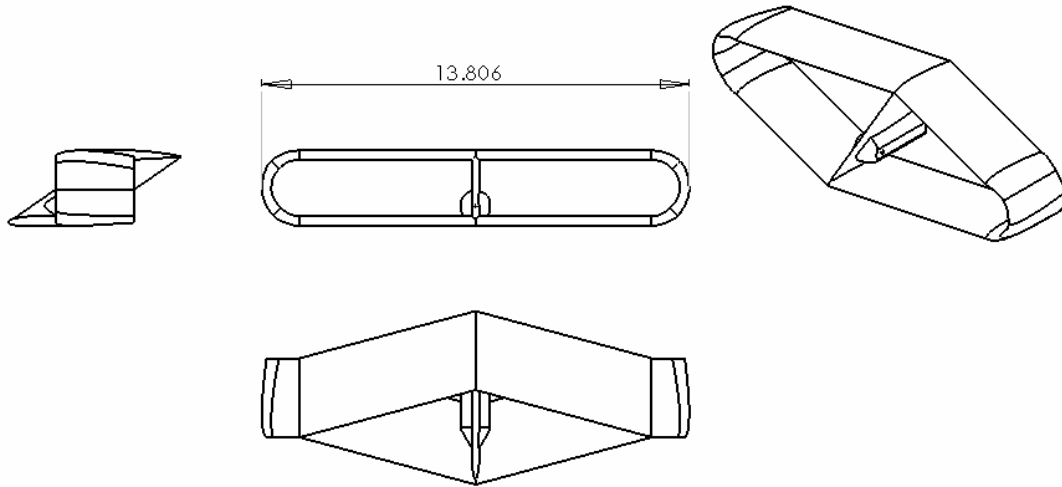


Figure 54: Left, Front, Top, and Isometric Views of the + 5° Canted Flow Guide Model

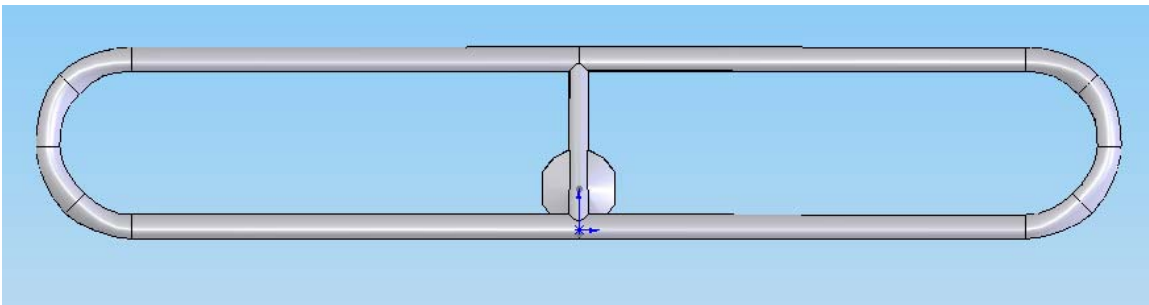


Figure 55: Front View of the + 5° Canted Flow Guide Model

3.3.4 Negative 5° Canted Flow Guide Model

The Negative 5° Canted Flow Guide Model (-5° Model) was built according to the same method for the Original Model except that the Flow Guides were altered with a -5° cant in the airfoils located at the 45° and 135° planes (Figure 52). The -5° cant was accomplished in *SolidWorks* by rotating the airfoils 5° in the counter-clockwise direction

about the mid-chord (Figure 56). The aircraft views for the -5° Model can be seen in Figure 57 and Figure 58. The parameters for the -5° model are identical to the $+5^\circ$ Model parameters.

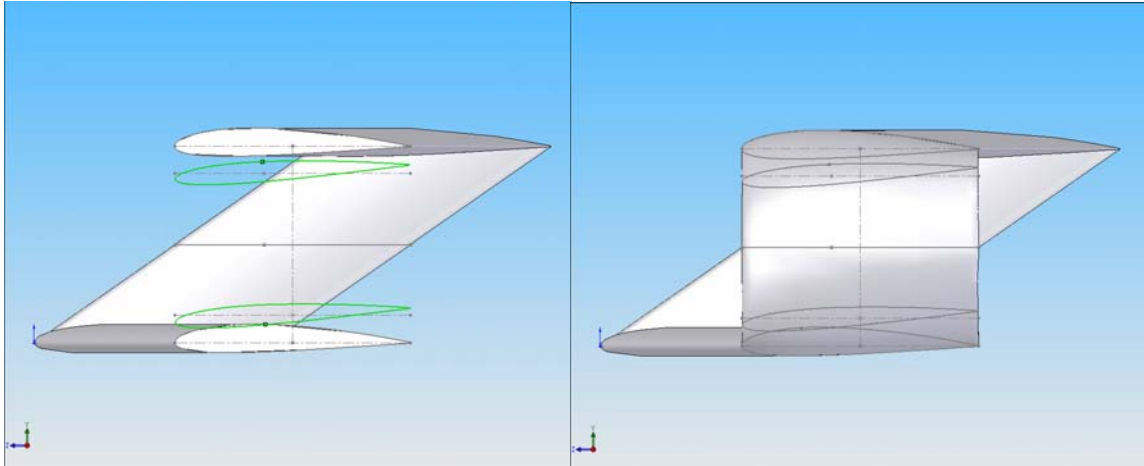


Figure 56: The Rotated Airfoils and Subsequent -5° Canted Airfoil

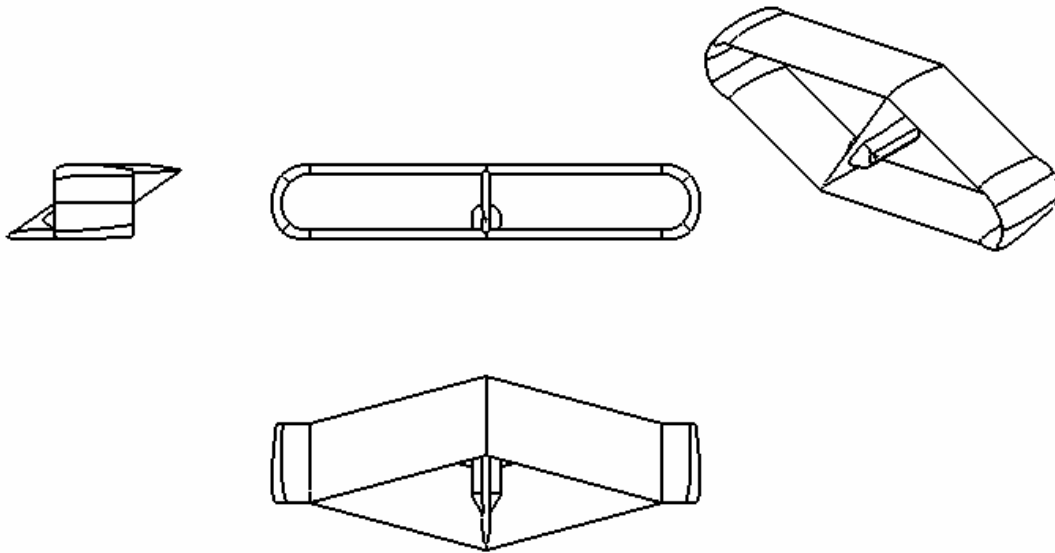


Figure 57: Left, Front, Top, and Isometric Views of the -5° Canted Flow Guide Model

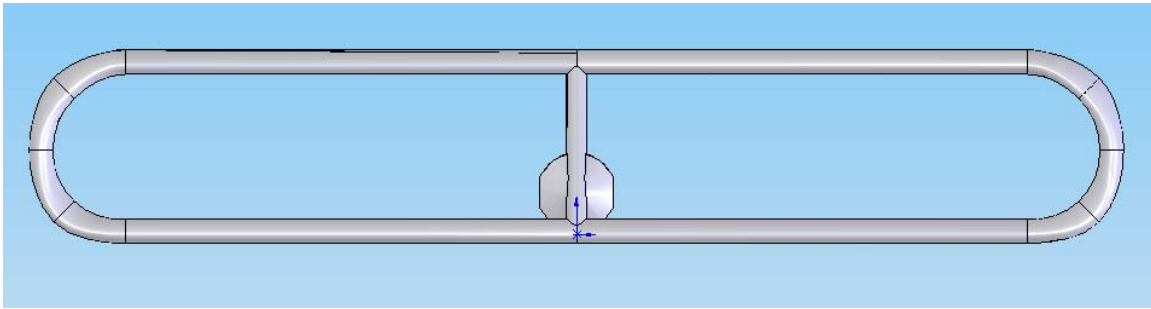


Figure 58: Front View of the - 5° Canted Flow Guide Model

3.3.5 Endplate Configuration

The Endplate Configuration Model was built according to the same method for the Original Configuration Model except that aluminum flat plates were substituted for the Flow Guides. The aluminum plates were cut to cover the upper and lower wingtips and to cover the gap. The plates are 0.0625" in depth. The aircraft views for the Endplate Configuration Model can be seen in Figure 59 and Figure 60. The Endplate Model differs from the Original Configuration Model with the following parameters. The wingspan (b) is 11.439". The planform area (S) is 58.326 in² and is calculated the same way as the Original Configuration Model minus the Flow Guides' area but including the End Plates' area. The volume of the model is 14.85 in³.

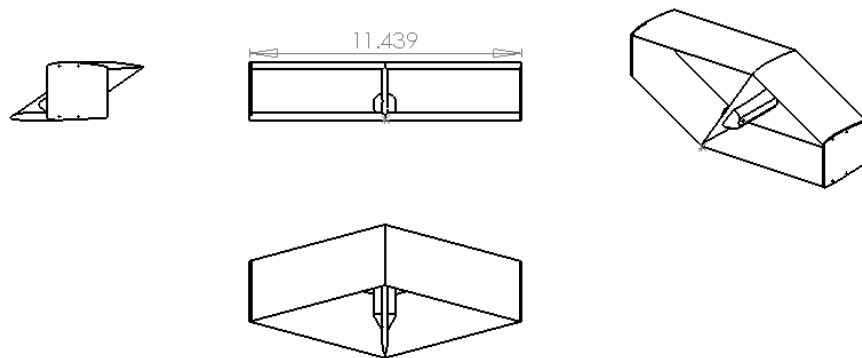


Figure 59: Left, Front, Top, and Isometric Views of the End Plate Configuration Model

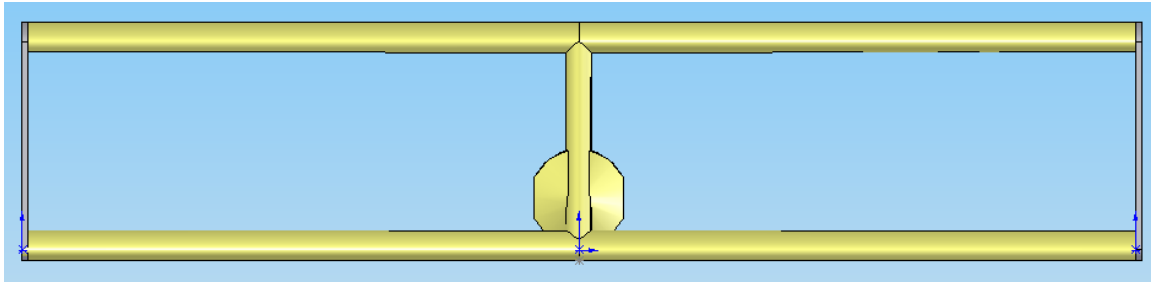


Figure 60: Front View of the End Plate Configuration Model

3.3.6 No Flow Guide Configuration

The No Flow Guide Configuration Model was built according to the same method for the Original Configuration Model except that the Flow Guides were not added. The aircraft views for the No Flow Guide Configuration Model can be seen in Figure 61 and Figure 62. The No Flow Guide Model differs from the Original Configuration Model with the following parameters. The wingspan (b) is 11.377". The planform area (S) is 58.02 in² and is calculated the same way as the Original Configuration Model minus the Flow Guides' area. The volume of the model is 14.10 in³.

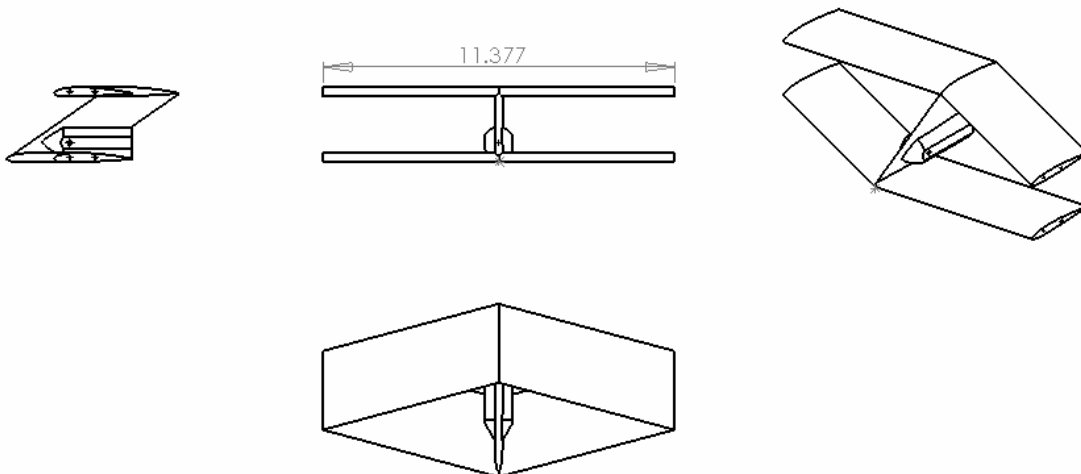


Figure 61: Left, Front, Top, and Isometric Views of the No Flow Guide Configuration Model

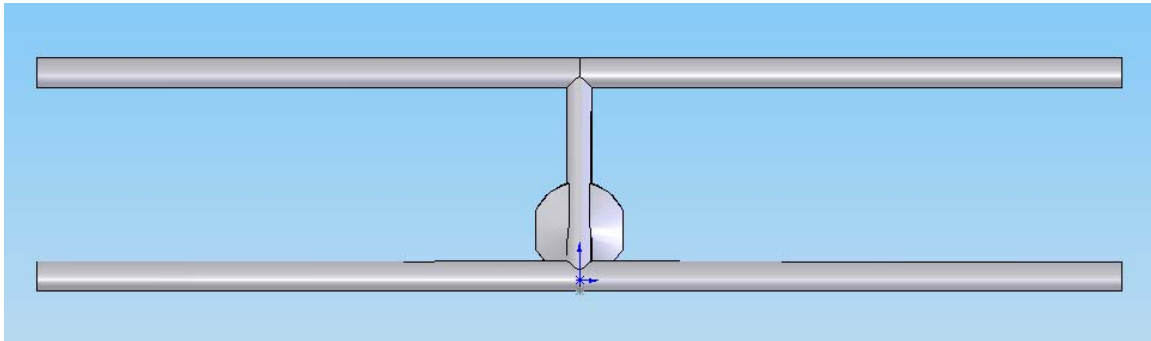


Figure 62: Front View of the No Flow Guide Configuration Model

3.4 Experimental Equipment

3.4.1 AFIT Low-Speed Wind Tunnel

The tests completed in this study utilized the Air Force Institute of Technology's low-speed, open-circuit wind tunnel. The schematic for the low-speed wind tunnel can be seen in Figure 63.

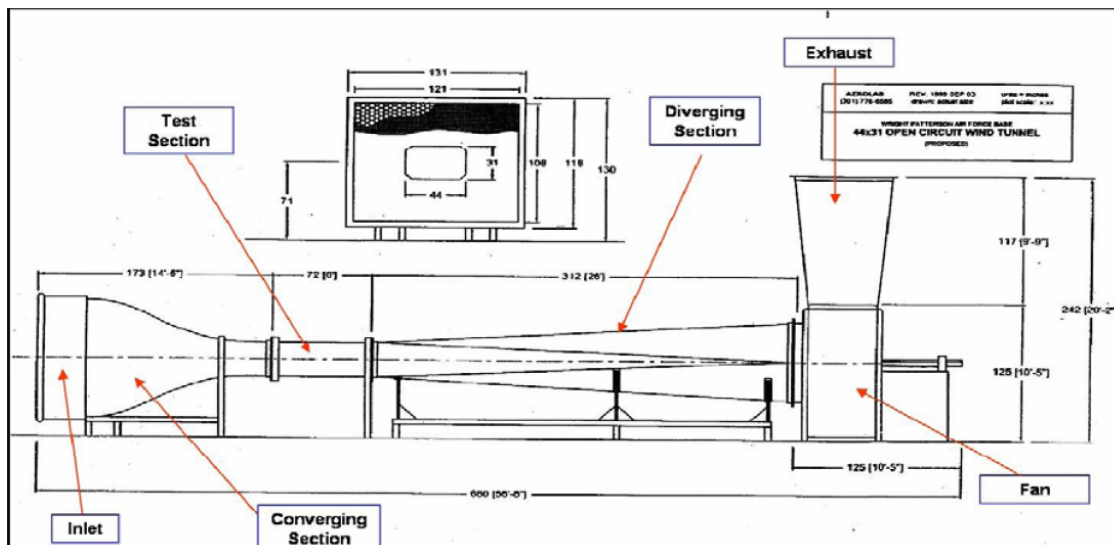


Figure 63: Schematic of the Low-Speed Wind Tunnel (reproduced from Reference 31:24)

Initially, ambient air is drawn through the intake plenum of the wind tunnel by the fan. Next, the air passes through an aluminum honeycomb flow-straightener and then through

steel mesh anti-turbulence screens. Once the flow passes through the last anti-turbulence screen it enters the convergent section of the tunnel. The intake and convergent section of the tunnel are shown in Figure 64.



Figure 64: Intake and Convergent Section of the Wind Tunnel (reproduced from Reference 31:25)

The convergent section of the wind tunnel accelerates the airflow into the octagon-shaped test section. The test section has a width of 44" and height of 31". Upon exiting the test section, the airflow enters the diffuser section of the wind tunnel. The diffuser decelerates the airflow and it is then exhausted vertically back into the room. The test models are mounted to an internal balance that is attached to a movable sting in the test section of the tunnel. The sting is manipulated by a movable control table and a pitch control device. The wind tunnel test section, balance, sting mechanism, and moveable table for β measurements are shown in Figure 65.



Figure 65: Test Section, Balance, Sting, and Moveable Table (reproduced from Reference 31:25)

Measurements can be taken by the balance once the wind tunnel reaches a desired velocity. Angle of attack sweeps (α sweeps) can be accomplished by pitching the balance and subsequent model using the angle control device. This device is a system of bars and cables that is controlled by motors underneath the tunnel (Figure 66).



Figure 66: Angle Control Device (reproduced from Reference 31:26)

The data acquisition was accomplished using a computerized data acquisition system (Figure 67) operated by AFIT lab technician John Hixenbaugh, who has been trained and is proficient with the system.



Figure 67: Computerized Data Acquisition System

All data files for each test run were stored on the hard drive of the acquisition system and were later retrieved for data reduction. The acquisition recorded the following values: α , β , tunnel speed, unresolved normal force, unresolved axial force, side force, pitch moment, yaw moment, and roll moment. All forces and moments were measured about the balance center. The balance records the force data by comparing voltage measurements to the calibrated voltage measurements. This comparison allows the forces that act on the balance to be determined.

Before testing each model, a tare run was completed for an identical α sweep that would be used for the actual test at speed. The tare was necessary to subtract the weight of the model from the data at all angles of attack. Between each change of airspeed during testing, the wind tunnel velocity was brought back to zero to ensure that the balance was still calibrated correctly.

3.4.2 AFIT 10 lb Strain Gage Balance

A 10 lb strain gage balance was used in the AFIT low-speed wind tunnel to record the force measurements on all the models. The balance is manufactured by Modern Machine and Tool Company. Figure shows the balance mounted in the sting of the test section of the wind tunnel.

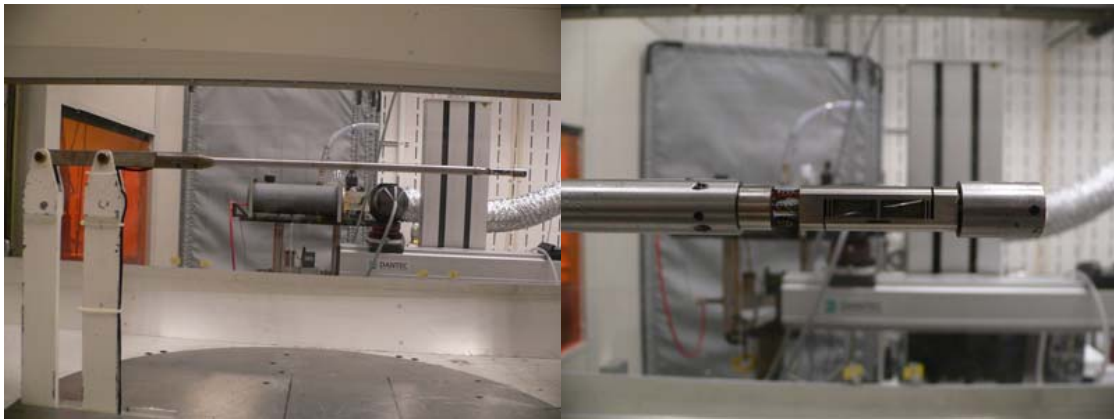


Figure 68: 10 lb Balance Mounted in Test Section of the Wind Tunnel (reproduced from Reference 31:28)

A list of the maximum allowable forces and moments is listed in Table 2. If forces or moments exceed the allowable range then the balance could be damaged and thus invalidate the calibration.

Table 2: Max Allowable Forces and Moments for the 10 lb Balance

| Component | Max Load |
|-----------|-----------|
| Normal | 10 lbs |
| Axial | 5 lbs |
| Pitch | 10 in-lbs |
| Roll | 4 in-lbs |
| Yaw | 5 in-lbs |
| Side | 5 lbs |

The balance's moment center is located 1.3350" aft of the screws. The screws are where the balance is attached to the model. The other dimensions of the balance can be seen in Appendix A.

3.5 Collecting and Processing Data

3.5.1 Correction of Balance Data using *MATLAB*® 10 lb Balance Code

Once the wind tunnel tests have been completed, the data has to be processed and reduced in order to receive useable results. This process is done using a *MATLAB* m-file to perform a series of operations and calculations on the tunnel output data. The *MATLAB* 10 lb Balance Code was adapted from previous research conducted by former AFIT students Rivera Parga, Deluca, and Walker (10; 25; 31). The modified *MATLAB* 10 lb Balance Code can be seen in Appendix B. The m-file requires multiple inputs about the model and ambient conditions at the time of testing (e.g., room temperature, barometric pressure) plus the tare and wind tunnel data for each model. The temperature and pressure in the wind tunnel room varied between each test run. These values were recorded for each test and were input into each model's corresponding code.

When the aircraft is mounted on the balance, it is at the reference zero angle of attack. When the balance is at the 0° position, the model is at 0° aircraft angle of attack, AoA.

In order to obtain the moment data from the wind tunnel results, a reference center of gravity for the aircraft must be determined. For the data reduction in this study, the center of gravity was placed at the mean of the quarter chord locations of the upper and lower wings (Equation 9).

$$c_{\frac{1}{4}} = \frac{0.25\bar{c}_{upper} + 0.25\bar{c}_{lower}}{2} \quad (9)$$

The resulting center of gravity is 2.1625" from the nose of the model in the x-direction, 0.53" above the lower wing's chord line in the z-direction, and is centered in the y - directions (aircraft body coordinate system located at nose of model) (Figure 69).

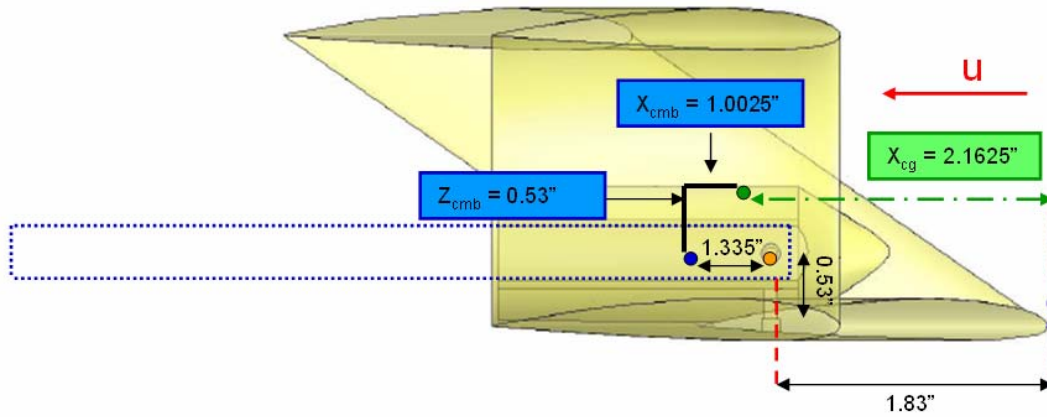


Figure 69: Location of Aircraft Center of Gravity and Balance Moment Center

The aircraft center of gravity (green dot) is located 1.0025" in front of the balance moment center (blue dot) and 0.53" above the balance moment center (in the wind axis coordinate system). These values were input into the *MATLAB* 10 lb Balance Code for data reduction.

Data reduction, using the *MATLAB* 10 lb Balance Code, begins by subtracting the tare data from the test data. Next, there are a few corrections to the data that must be added. The first correction to the data is to account for the blockage of flow in the wind tunnel by the model. This adjustment is done by determining the blockage correction factor. The blockage correction factor accounts for the change in speed of the airflow due

to the reduction in the available cross-sectional area of the tunnel near the model. The delta term (δ_b), blockage correction factor, is approximated for all the model configurations. This is due to their effective spans of 13.808" (Original Configuration), 13.806" (+ 5° and – 5° configurations), 11.5" (Endplate Configuration), and 11.38" (No Flow Guide Configuration) making little difference in the estimation of the parameter. The δ_b term was found to be 0.1177 using the chart found in Barlow, Rae, and Pope (3:387). The δ_b was found by first calculating the wind tunnel aspect ratio:

$$\lambda = \frac{height_{tunnel}}{width_{tunnel}} \quad (10)$$

where λ is the wind tunnel aspect ratio, $height_{tunnel}$ (ft) is the height of the wind tunnel cross-section, and $width_{tunnel}$ (ft) is the width of the wind tunnel cross-section. The AFIT low-speed wind tunnel has $\lambda = 0.705$. The next calculation that was needed was the ratio of the model's wingspan to the width of the wind tunnel:

$$k = \frac{b}{width_{tunnel}} \quad (11)$$

Where k (-) is the ratio of span to the wind tunnel test section width, and b (ft, m) is the wingspan of the model. For these tests, k ranged from 0.259 to 0.313 for the models tested. The values for λ and k are then used to find the blockage correction factor, δ_b .

The second correction to the data involves transferring the normal and axial balance data into the proper frame of reference with respect to the flow. This correction is necessary to translate the lift and force data so it is with respect to the free stream velocity and not the angle of attack of the balance or model. The calculations of the lift and drag coefficients from the normal and axial force acting on the balance is as follows:

$$C_L = \frac{N \cdot \cos \alpha - A \cdot \sin \alpha}{\frac{1}{2} \rho \cdot V^2 \cdot S} \quad (12)$$

$$C_D = \frac{N \cdot \sin \alpha + A \cdot \cos \alpha}{\frac{1}{2} \rho \cdot V^2 \cdot S} \quad (13)$$

Where C_L (-) is the lift coefficient, C_D (-) is the drag coefficient, N (lb) is the normal force acting on the balance, A (lb) is the axial force acting on the balance, α ($^\circ$) is the angle of attack of the balance, ρ (mmHg) is the air density, V (mph, m/s) is the tunnel wind velocity, and S (in²) is the planform area (wing area) of the aircraft model.

3.5.2 Uncertainty Analysis

The Uncertainty Analysis methodology followed Michael Walker's Thesis (31:37). Uncertainty analysis was performed on the lift-to-drag ratio for the Original Configuration Model in Section 4.2.1. The analysis was done by taking the equation for lift-to-drag and breaking it into a form consisting only of measurements from the wind tunnel results:

$$L/D = \frac{C_L}{C_D} = \frac{N \cdot \cos \alpha - A \cdot \sin \alpha}{N \cdot \sin \alpha + A \cdot \cos \alpha} \quad (14)$$

where L/D (-) is the lift-to-drag ratio, C_L (-) is the lift coefficient, C_D (-) is the drag coefficient, N (lb) is the normal force measurements on the balance, A (lb) is the axial force measurement on the balance, and α ($^\circ$) is the angle of the balance to the free stream velocity.

Then the partial of Equation (14) is taken with respect to both N and A :

$$\frac{\partial(L/D)}{\partial N} = \frac{A}{(N \cdot \sin \alpha + A \cdot \cos \alpha)^2} \quad (15)$$

$$\frac{\partial(L/D)}{\partial A} = \frac{-N}{(N \cdot \sin \alpha + A \cdot \cos \alpha)^2} \quad (16)$$

where $\frac{\partial(L/D)}{\partial N}$ is the partial of the lift-to-drag ratio with respect to the unresolved normal force, and $\frac{\partial(L/D)}{\partial A}$ is the partial of the lift-to-drag ratio with respect to the unresolved axial force.

Next, a worse case possible error and a realistic case possible error in lift-to-drag can be calculated:

$$\Delta(L/D)_{worst} = \left| \frac{\partial(L/D)}{\partial N} \cdot \Delta N \right| + \left| \frac{\partial(L/D)}{\partial A} \cdot \Delta A \right| \quad (17)$$

$$\Delta(L/D)_{realistic} = \sqrt{\left(\frac{\partial(L/D)}{\partial N} \cdot \Delta N \right)^2 + \left(\frac{\partial(L/D)}{\partial A} \cdot \Delta A \right)^2} \quad (18)$$

where $\Delta(L/D)_{worst}$ is a worst-case error value in lift-to-drag ratio, $\Delta(L/D)_{realistic}$ is a more realistic error value in lift-to-drag ratio, ΔN is the possible error in the normal force measurement, and ΔA is the possible error in the axial force measurement.

For the 10 lb balance, the uncertainty in the normal force measurement, ΔN , is specified by the manufacturer to be more than 0.025 lbs. The uncertainty in the axial force measurement, ΔA , is specified by the manufacturer to be more than 0.0125 lbs. These values are considered to be too conservative for actual data acquisition. The range for the possible lift-to-drag ratio can then be determined:

$$\frac{L}{D_{range}} = \frac{L}{D} \pm \Delta(\frac{L}{D}) \quad (19)$$

where L/D_{range} is the possible range of the lift-to-drag ratio given uncertainty in the measurements taken, L/D is the measured lift-to-drag ratio, and $\Delta(L/D)$ is the possible error in the L/D measurement (in one direction).

Another method, used to determine the uncertainty in the normal force measurement, ΔN , and in the axial force measurement, ΔA , was to determine the standard deviation of the force measurements at each given angle of attack (α) for a constant speed. Multiple data points are logged for each angle, therefore the actual sample variance and hence standard deviation can be computed. This method is explored in Section 4.2.1.6 and is labeled the tested uncertainty analysis. Uncertainty analysis by this method reflects a more realistic error value.

3.5.3 Houck 24" Hot-Wire Analysis

In the Fall of 2006 and Winter of 2007, a study on the Houck 24" Configuration was completed at the Air Force Institute of Technology by Masters thesis student 1st LT Michael Walker, USAF and his advisor Dr. Mark Reeder. The model, tested in the AFIT low-speed wind tunnel, was the 24" Houck Configuration. The 24" Houck Configuration can be seen in Figure 70. The Hot-Wire data from the study was analyzed to find the vortex moment (concentration of the vortex in the y-direction). The α sweep data of the Original 24" and No Flow Guide Houck 24" were used for comparison with the model configurations tested in this study.



Figure 70: 24" Houck Configuration Three-View Representation (reproduced from Reference 31)

3.6 Test Plan

3.6.1 Overview

A summary of tests performed on the various model configurations can be found in Table 3. Experimental information has primarily been collected through the use of balance data. The tests used for the 24" Houck comparison consisted of balance and the use of Hot-Wire data. Further detail of testing for each model configuration will be discussed in the remainder of this section.

Table 3: Summary of Tests Performed

| Model Configuration | Re (-) | V (mph) | Balance Data | Hot Wire |
|-------------------------|--------|---------|----------------|--------------------|
| | | | α sweep | $\alpha = 4^\circ$ |
| Original | 38K | 20 | ✓ | |
| Original | 57K | 30 | ✓ | |
| Original | 78K | 40 | ✓ | |
| Original | 120K | 60 | ✓ | |
| + 5° Cant | 38K | 20 | ✓ | |
| + 5° Cant | 57K | 30 | ✓ | |
| + 5° Cant | 78K | 40 | ✓ | |
| + 5° Cant | 120K | 60 | ✓ | |
| - 5° Cant | 38K | 20 | ✓ | |
| - 5° Cant | 57K | 30 | ✓ | |
| - 5° Cant | 78K | 40 | ✓ | |
| - 5° Cant | 120K | 60 | ✓ | |
| Endplate | 38K | 20 | ✓ | |
| Endplate | 57K | 30 | ✓ | |
| Endplate | 78K | 40 | ✓ | |
| Endplate | 120K | 60 | ✓ | |
| No Flow Guide | 38K | 20 | ✓ | |
| No Flow Guide | 57K | 30 | ✓ | |
| No Flow Guide | 78K | 40 | ✓ | |
| No Flow Guide | 120K | 60 | ✓ | |
| Original 24" Houck | 80K | 20 | ✓ | |
| Original 24" Houck | 125K | 30 | ✓ | ✓ |
| No Flow Guide 24" Houck | 80K | 20 | ✓ | |
| No Flow Guide 24" Houck | 125K | 30 | ✓ | ✓ |

3.6.2 Original Configuration

Testing began with the Original Configuration Model. The model was placed on the 10 lb balance in the AFIT low-speed wind tunnel. Data was taken for all configurations for four different α sweeps from -8° to 10° by 2° increments and then from 10° to 15° by 1° increments. Testing procedures were repeated for all models. The dates of the testing and the corresponding temperature and pressure can be seen in Tables 4-8.

Table 4: Original Configuration Test Dates, Temperature, and Pressure

| Model Configuration: Original | | Date | Temperature (°F) | Barometric Pressure |
|-------------------------------|---------|-----------|------------------|---------------------|
| Re (-) | V (mph) | | | |
| 38K | 20 | 17-Apr-07 | 71 | 14.15 psi |
| 57K | 30 | 17-Apr-07 | 71 | 14.15 psi |
| 78K | 40 | 17-Apr-07 | 71 | 14.15 psi |
| 120K | 60 | 23-Apr-07 | 74.2 | 14.23 psi |

3.6.3 + 5° Configuration

Table 5: + 5° Canted Flow Guide Configuration Test Dates, Temperature, and Pressure

| Model Configuration: + 5° | | Date | Temperature (°F) | Barometric Pressure |
|---------------------------|---------|-----------|------------------|---------------------|
| Re (-) | V (mph) | | | |
| 38K | 20 | 17-Apr-07 | 71 | 14.15 psi |
| 57K | 30 | 17-Apr-07 | 71 | 14.15 psi |
| 78K | 40 | 17-Apr-07 | 71 | 14.15 psi |
| 120K | 60 | 23-Apr-07 | 74.8 | 14.21 psi |

3.6.4 - 5° Configuration

Table 6: - 5° Canted Flow Guide Configuration Test Dates, Temperature, and Pressure

| Model Configuration: - 5° | | Date | Temperature (°F) | Barometric Pressure |
|---------------------------|---------|-----------|------------------|---------------------|
| Re (-) | V (mph) | | | |
| 38K | 20 | 18-Apr-07 | 69.9 | 14.1 psi |
| 57K | 30 | 18-Apr-07 | 69.9 | 14.1 psi |
| 78K | 40 | 18-Apr-07 | 69.9 | 14.1 psi |
| 120K | 60 | 23-Apr-07 | 74.8 | 14.21 psi |

3.6.5 Endplate Configuration

Table 7: Endplate Configuration Test Dates, Temperature, and Pressure

| Model Configuration: Endplates | | Date | Temperature (°F) | Barometric Pressure |
|--------------------------------|---------|-----------|------------------|---------------------|
| Re (-) | V (mph) | | | |
| 38K | 20 | 20-Apr-07 | 72.6 | 14.32 psi |
| 57K | 30 | 20-Apr-07 | 72.6 | 14.32 psi |
| 78K | 40 | 20-Apr-07 | 72.6 | 14.32 psi |
| 120K | 60 | 20-Apr-07 | 72.6 | 14.32 psi |

3.6.6 No Flow Guide Configuration

Table 8: No Flow Guide Configuration Test Dates, Temperature, and Pressure

| Model Configuration: No Flow Guides | | Date | Temperature (°F) | Barometric Pressure |
|-------------------------------------|---------|-----------|------------------|---------------------|
| Re (-) | V (mph) | | | |
| 38K | 20 | 18-Apr-07 | 71.2 | 14.09 psi |
| 57K | 30 | 18-Apr-07 | 71.2 | 14.09 psi |
| 78K | 40 | 18-Apr-07 | 71.2 | 14.09 psi |
| 120K | 60 | 20-Apr-07 | 71.9 | 14.33 psi |

IV. Results and Analysis

4.1 Chapter Overview

In this chapter, results will be shown for wind tunnel tests conducted on the Original Configuration Model, +5° Cant Configuration Model, -5° Cant Configuration Model, Endplate Configuration Model, and the No Flow Guide Configuration Model. In addition to the wind-tunnel results, there will be analysis on the 24" Houck (with and without flow guides) Configuration's Hot-Wire results (31). The aerodynamic data for all five models can be seen in Appendix C.

The results will be divided into four main sections. The first section will present each model's results. This section includes analysis on the balance data from each model's α sweeps that were performed in the AFIT low-speed wind tunnel at various speeds (20 mph, 30 mph, 40 mph, and 60 mph). The second section will compare the results of each model at each speed. Only balance data using α sweeps performed in the AFIT low-speed wind tunnel will be described in this section. The third section will discuss the process and results of the Original Configuration Model's neutral longitudinally stable $C_{m\alpha}$. The fourth and final section will discuss the process and results of the vortex centroid analysis of the 24" Houck Configuration.

4.2 Wind Tunnel Balance Data – Alpha Sweeps: Individual Models

4.2.1 Original Configuration Model

4.2.1.1 Summary

In the AFIT low-speed wind tunnel, an α sweep from -8° to 10° in steps of 2° and then from 10° to 15° in steps of 1° was performed on the Original Configuration Model at

four different speeds: 20 mph (8.94 m/s), 30 mph (13.41 m/s), 40 mph (17.88 m/s), and 60 mph (26.82 m/s). A summary of the resulting aerodynamic performance of the Original Configuration Model at $Re \approx 38,000$ (20 mph), $Re \approx 57,000$ (30 mph), $Re \approx 78,000$ (40 mph), and $Re \approx 120,000$ (60 mph) can be seen in Table 9. The Reynolds numbers are based on the average root chord of the upper and lower wings ($\bar{c} = 2.55''$).

Table 9: Aerodynamic Performance of the Original Configuration Model

| Model | Re (-) | Min Drag | | Zero Lift | Slopes | |
|------------------------|--------|--------------|--------------|-------------------------------|--------------------|--------------------|
| | | C_{D0} (-) | α (°) | $\alpha_{0 \text{ Lift}}$ (°) | $C_{L\alpha}$ (/°) | $C_{m\alpha}$ (/°) |
| Original Configuration | 38K | 0.0327 | -2.03 | -0.52 | 0.0528 | 0.0106 |
| Original Configuration | 57K | 0.0275 | -2.02 | -1.33 | 0.0555 | 0.0099 |
| Original Configuration | 78K | 0.0251 | 0.03 | -1.50 | 0.0538 | 0.0105 |
| Original Configuration | 120K | 0.0204 | 0.12 | -1.54 | 0.053 | 0.0114 |

| Model | Re (-) | Max Range | | | | Max Endurance | | | |
|------------------------|--------|-----------|--------------|-----------|-----------|-----------------------|--------------|-----------|-----------|
| | | L/D (-) | α (°) | C_L (-) | C_D (-) | $C_L^{(3/2)}/C_D$ (-) | α (°) | C_L (-) | C_D (-) |
| Original Configuration | 38K | 6.2241 | 8.43 | 0.4631 | 0.0744 | 4.2385 | 10.55 | 0.5625 | 0.0995 |
| Original Configuration | 57K | 9.4369 | 6.33 | 0.4252 | 0.0451 | 7.0672 | 10.57 | 0.6110 | 0.0676 |
| Original Configuration | 78K | 10.5512 | 6.32 | 0.4154 | 0.0394 | 7.7068 | 10.56 | 0.5969 | 0.0598 |
| Original Configuration | 120K | 11.8368 | 6.41 | 0.4240 | 0.0358 | 8.5435 | 10.56 | 0.6003 | 0.0544 |

4.2.1.2 Drag Coefficient

The drag coefficient, C_D , for the Original Configuration Model is shown in Figure 71 for four different Reynolds numbers (38K, 57K, 78K, and 120K). C_D has been plotted both versus C_L and α .

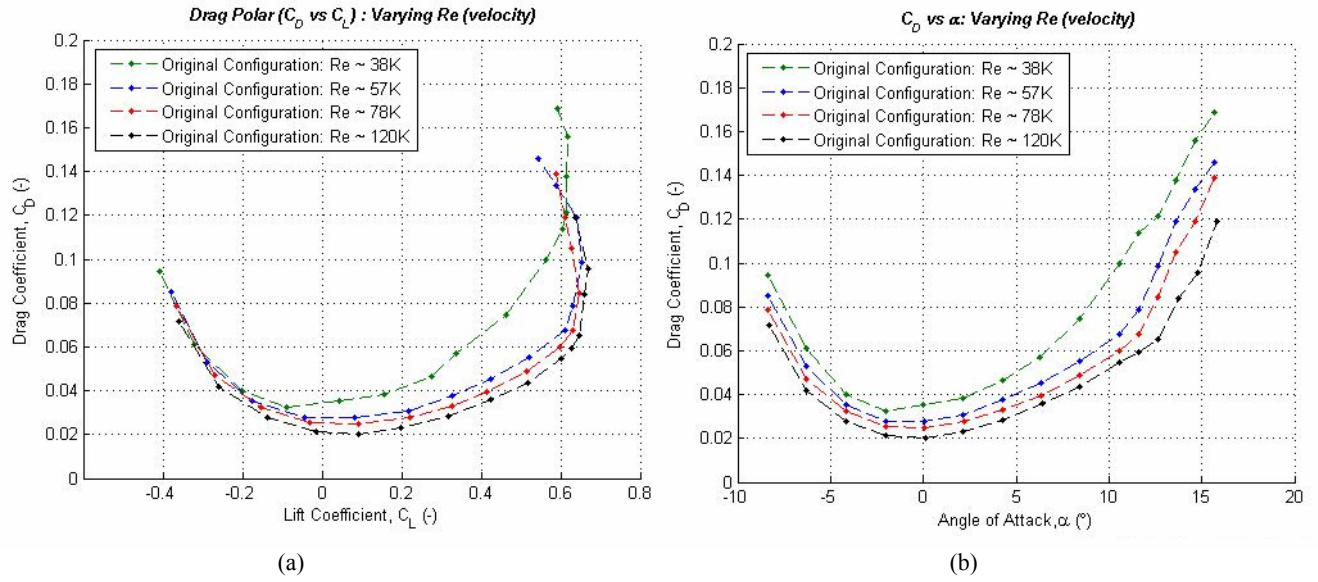


Figure 71: Drag Coefficient – Original Configuration Model
(a) Drag Coefficient vs. Lift Coefficient (Drag Polar), (b) Drag Coefficient vs. Alpha

4.2.1.3 Lift Coefficient

Figure 72 plots the lift coefficient, C_L , vs. α for the Original Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). From the lift curve, a number of important aerodynamic values can be attained. C_{Lmax} is the maximum lift coefficient of the aircraft. An aircraft flying at the α that corresponds to C_{Lmax} will produce the highest amount of lift at that speed. C_{Lmax} usually occurs right before stall. As seen in Figure 72, the Original Configuration Model exhibits the gradual stall characteristic of most aircraft past an $\alpha = 10^\circ$. $C_{L\alpha}$ is the lift curve slope, and gives a ratio of change of C_L with respect to α for the linear region (α from -8° to $+8^\circ$) of the lift curve, while $\alpha_{0\text{ Lift}}$ is the angle of attack where the aircraft produces zero lift.

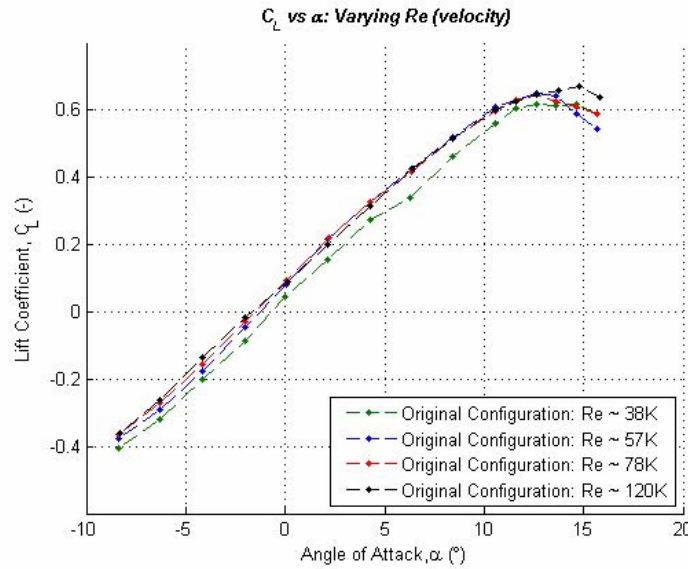


Figure 72: Lift Coefficient vs. Angle of Attack – Original Configuration Model

4.2.1.4 Pitching Moment Coefficient

Figure 73 plots the pitching moment coefficient, C_m , vs. α for the Original Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The longitudinal static stability derivative, $C_{m\alpha}$, can be attained from the linear portion of this plot (α from -8° to $+8^\circ$). It is desirable to have a negative value for $C_{m\alpha}$. A negative $C_{m\alpha}$ value will return the aircraft to trim state ($C_m = 0$) when it is perturbed. The Original Configuration Model is longitudinally unstable, due to a positive $C_{m\alpha}$ value, about the reference CG (2.1625" aft of nose), for all four Reynolds numbers tested.

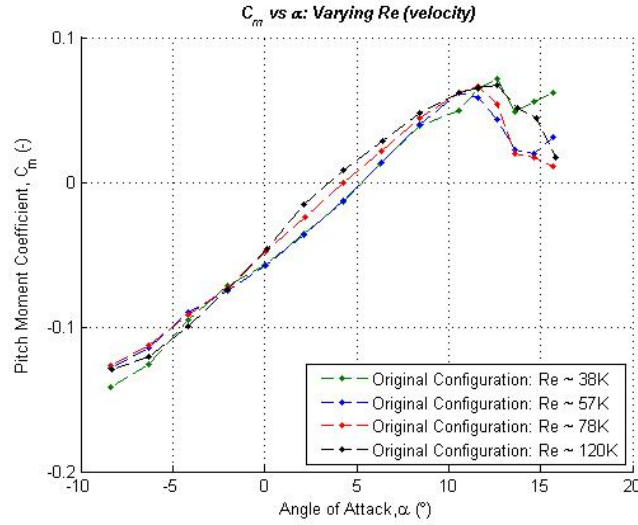


Figure 73: Pitch Moment Coefficient vs. Angle of Attack – Original Configuration Model ($X_{cmb} = 1.0025"$)

4.2.1.5 Lift-to-Drag Ratio

Figure 74 shows the lift-to-drag ratio for the Original Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). L/D has been plotted versus α and C_L . Lift-to-drag is one measure of aircraft efficiency. An aircraft that flies at the angle of attack that corresponds to the maximum L/D , is maximizing its range (34). There is a strong correlation between an increase in Reynolds number and an increase in L/D values. The efficiency of the Original Configuration Model increases as the Reynolds number increases. L/D values for each Reynolds number increase over the range $\alpha \approx -4^\circ$ to 6° . Once L/D_{max} is reached for each Reynolds number, the L/D values start to decrease. This event occurs beyond $\alpha \approx 6^\circ$ and $C_L \approx 0.41$.

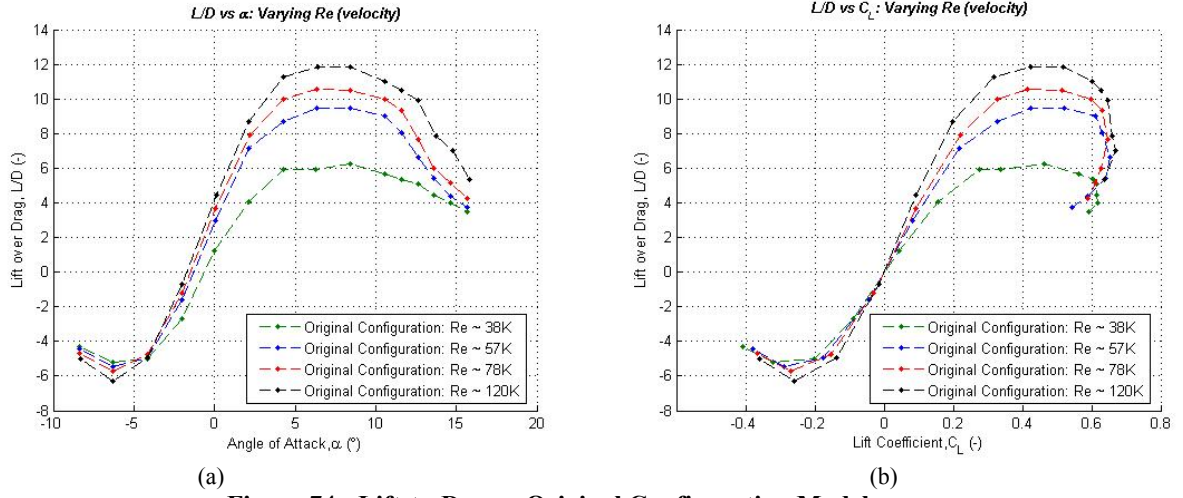


Figure 74: Lift-to-Drag – Original Configuration Model
(a) Lift-to-Drag vs. Alpha, (b) Lift-to-Drag vs. Lift Coefficient

4.2.1.6 Lift-to-Drag Error Analysis

Figure 75 shows the lift-to-drag ratio plotted for all Reynolds numbers (38K, 57K, 78K, and 120K) with error bars. The error bars were calculated using the conservative method outlined in the beginning of Section 3.5.2. The results of lift-to-drag ratio at all Reynolds numbers for the Original Configuration Model can be seen in Table 10. The worst case scenario is the case where each possible case of error occurs in the same direction. The realistic case scenario is geometric mean of the possible errors and is a more probable occurrence.

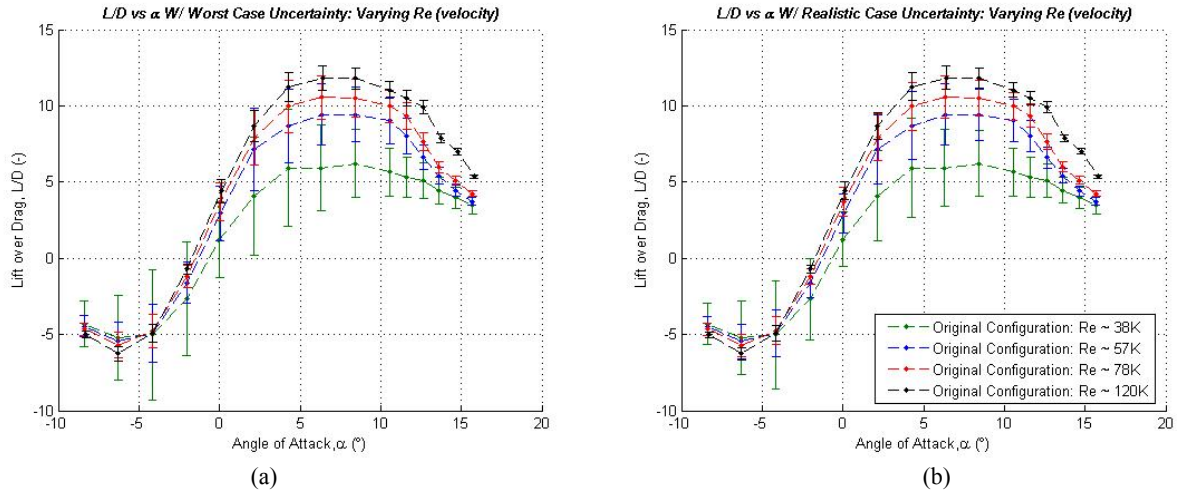


Figure 75: Lift-to-Drag – Conservative Uncertainty Analysis – Original Configuration Model
(a) Worst Case Uncertainty Analysis, (b) Realistic Uncertainty Analysis

For a Reynolds number of approximately 38K, the worst case error ranges from 8.47% to 61.49% of L/D and the realistic case ranges from 8.54% to 61.38% of L/D. The possible error at L/D_{\max} is 40.98% for the worst case scenario and 36.69% for the realistic case scenario. For a Reynolds number of approximately 57K, the worst case error ranges from 3.93% to 38.84% of L/D and the realistic case ranges from 2.96% to 24.87% of L/D. The possible error at L/D_{\max} is 29.19% for the worst case scenario and 22.23% for the realistic case scenario. For a Reynolds number of approximately 78K, the worst case error ranges from 2.71% to 26.00% of L/D and the realistic case ranges from 1.76% to 16.12% of L/D. The possible error at L/D_{\max} is 20.61% for the worst case scenario and 14.05% for the realistic case scenario. For a Reynolds number of approximately 120K, the worst case error ranges from 1.89% to 14.68% of L/D and the realistic case ranges from 0.97% to 7.82% of L/D. The possible error at L/D_{\max} is 11.55% for the worst case scenario and 6.57% for the realistic case scenario.

Table 10: Conservative Uncertainty Analysis in L/D for the Original Configuration Model

| Re = 38K (20 MPH) | | | | Re = 57K (30 MPH) | | | |
|-------------------|---------|----------------|-----------|--------------------|---------|----------------|-----------|
| α (°) | L/D (-) | Error in % L/D | | α (°) | L/D (-) | Error in % L/D | |
| | | Worst | Realistic | | | Worst | Realistic |
| -8.39 | -4.445 | 21.88% | 19.14% | -8.38 | -4.446 | 9.95% | 6.71% |
| -6.27 | -5.537 | 40.17% | 35.18% | -6.26 | -5.479 | 18.90% | 12.78% |
| -4.15 | -6.056 | 61.38% | 50.72% | -4.14 | -5.120 | 27.21% | 17.05% |
| -2.03 | -3.245 | 53.75% | 38.71% | -2.02 | -1.974 | 19.36% | 10.48% |
| 0.10 | 1.762 | 35.64% | 25.93% | 0.11 | 2.631 | 26.03% | 14.26% |
| 2.14 | 5.404 | 56.18% | 42.80% | 2.15 | 6.479 | 38.84% | 24.87% |
| 4.25 | 6.470 | 55.74% | 47.39% | 4.27 | 8.238 | 34.94% | 24.51% |
| 6.29 | 6.924 | 40.98% | 36.69% | 6.30 | 9.077 | 29.19% | 22.23% |
| 8.41 | 6.251 | 31.81% | 30.76% | 8.41 | 8.859 | 26.13% | 18.62% |
| 10.52 | 5.860 | 22.56% | 22.39% | 10.52 | 8.238 | 22.25% | 15.04% |
| 11.58 | 5.555 | 19.25% | 18.80% | 11.57 | 7.179 | 17.10% | 11.48% |
| 12.63 | 5.125 | 16.79% | 16.10% | 12.63 | 6.497 | 11.24% | 7.64% |
| 13.67 | 4.557 | 12.65% | 12.35% | 13.67 | 5.367 | 7.70% | 5.38% |
| 14.73 | 4.186 | 10.30% | 10.22% | 14.71 | 4.673 | 5.28% | 3.82% |
| 15.76 | 3.734 | 8.54% | 8.39% | 15.74 | 3.939 | 3.93% | 2.96% |
| Re = 78K (40 MPH) | | | | Re = 120K (60 MPH) | | | |
| α (°) | L/D (-) | Error in % L/D | | α (°) | L/D (-) | Error in % L/D | |
| | | Worst | Realistic | | | Worst | Realistic |
| -8.37 | -4.606 | 5.96% | 3.71% | -8.36 | -5.042 | 2.99% | 1.62% |
| -6.25 | -5.596 | 11.76% | 7.32% | -6.24 | -6.322 | 6.49% | 3.53% |
| -4.13 | -4.790 | 15.99% | 9.05% | -4.12 | -5.031 | 8.51% | 4.13% |
| -2.01 | -1.602 | 10.17% | 5.14% | -2.01 | -0.928 | 4.50% | 2.09% |
| 0.11 | 3.614 | 18.26% | 9.33% | 0.11 | 4.241 | 10.93% | 4.88% |
| 2.15 | 7.769 | 26.00% | 15.46% | 2.14 | 8.770 | 14.68% | 7.56% |
| 4.27 | 9.475 | 24.59% | 16.12% | 4.27 | 11.204 | 13.70% | 7.82% |
| 6.29 | 9.956 | 20.61% | 14.05% | 6.29 | 11.676 | 11.55% | 6.57% |
| 8.40 | 9.718 | 18.11% | 11.56% | 8.41 | 11.308 | 10.05% | 5.38% |
| 10.52 | 9.201 | 15.08% | 9.16% | 10.52 | 10.403 | 8.06% | 4.12% |
| 11.58 | 8.782 | 12.82% | 7.66% | 11.58 | 9.889 | 7.10% | 3.57% |
| 12.63 | 7.249 | 8.40% | 5.05% | 12.63 | 9.358 | 6.21% | 3.07% |
| 13.67 | 5.844 | 5.16% | 3.20% | 13.68 | 8.682 | 3.87% | 1.93% |
| 14.72 | 5.179 | 3.91% | 2.45% | 14.73 | 6.640 | 3.11% | 1.55% |
| 15.75 | 4.615 | 2.71% | 1.76% | 15.77 | 5.206 | 1.89% | 0.97% |

The error values are decreasing as the Reynolds number is increased. This is due to higher velocities producing greater balance loading and therefore, increased sensitivity.

The lower loadings are closer to the balance's minimum resolution which causes the error to increase. These uncertainty values are conservative, as the actual uncertainty values for the balance measurements are smaller than published.

The next method, the tested uncertainty analysis, produced results that had significantly less error percentages than the previous conservative error analysis. The average standard deviation of the normal force and axial force at each wind tunnel run speed for a given α were used as the ΔN and ΔA . The calculated average standard deviation values were $\Delta N = 0.0056$ and $\Delta A = 0.0011$. These standard deviation values provided a confidence interval of approximately 99.9% (3:453). Figure 76 shows the lift-to-drag ratio plotted for all Reynolds numbers (38K, 57K, 78K, and 120K) with error bars. The error bars were calculated using the tested method outlined at the end of Section 3.5.2. The tested error value results of lift-to-drag ratio at all Reynolds numbers for the Original Configuration Model can be seen in Table 11. The worst case scenario is the case where each possible case of error occurs in the same direction. The realistic case scenario is geometric mean of the possible errors and is a more probable occurrence.

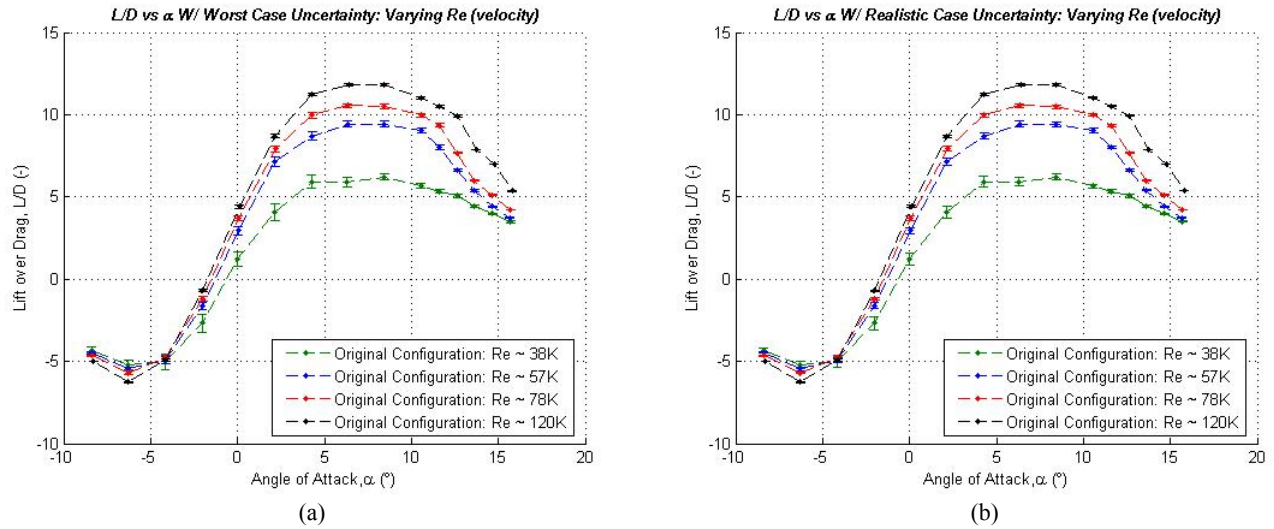


Figure 76: Lift-to-Drag – Tested Uncertainty Analysis – Original Configuration Model
(a) Worst Case Uncertainty Analysis, (b) Realistic Uncertainty Analysis

Table 11: Tested Uncertainty Analysis in L/D for the Original Configuration Model

| Re = 38K (20 MPH) | | | | Re = 57K (30 MPH) | | | |
|-------------------|---------|----------------|-----------|-------------------|---------|----------------|-----------|
| | | Error in % L/D | | | | Error in % L/D | |
| α (°) | L/D (-) | Worst | Realistic | α (°) | L/D (-) | Worst | Realistic |
| -8.39 | -4.445 | 2.33% | 1.79% | -8.38 | -4.446 | 0.80% | 0.62% |
| -6.27 | -5.537 | 4.27% | 3.29% | -6.26 | -5.479 | 1.51% | 1.18% |
| -4.15 | -6.056 | 7.05% | 5.12% | -4.14 | -5.120 | 2.40% | 1.74% |
| -2.03 | -3.245 | 7.68% | 5.62% | -2.02 | -1.974 | 2.39% | 1.89% |
| 0.10 | 1.762 | 6.15% | 5.10% | 0.11 | 2.631 | 2.86% | 2.10% |
| 2.14 | 5.404 | 7.23% | 5.12% | 2.15 | 6.479 | 3.33% | 2.45% |
| 4.25 | 6.470 | 6.16% | 4.59% | 4.27 | 8.238 | 2.65% | 2.21% |
| 6.29 | 6.924 | 4.23% | 3.36% | 6.30 | 9.077 | 1.96% | 1.96% |
| 8.41 | 6.251 | 2.95% | 2.72% | 8.41 | 8.859 | 1.94% | 1.66% |
| 10.52 | 5.860 | 2.01% | 1.97% | 10.52 | 8.238 | 1.78% | 1.39% |
| 11.58 | 5.555 | 1.76% | 1.66% | 11.57 | 7.179 | 1.38% | 1.07% |
| 12.63 | 5.125 | 1.57% | 1.42% | 12.63 | 6.497 | 0.89% | 0.70% |
| 13.67 | 4.557 | 1.15% | 1.09% | 13.67 | 5.367 | 0.59% | 0.49% |
| 14.73 | 4.186 | 0.92% | 0.90% | 14.71 | 4.673 | 0.38% | 0.34% |
| 15.76 | 3.734 | 0.77% | 0.74% | 15.74 | 3.939 | 0.27% | 0.26% |

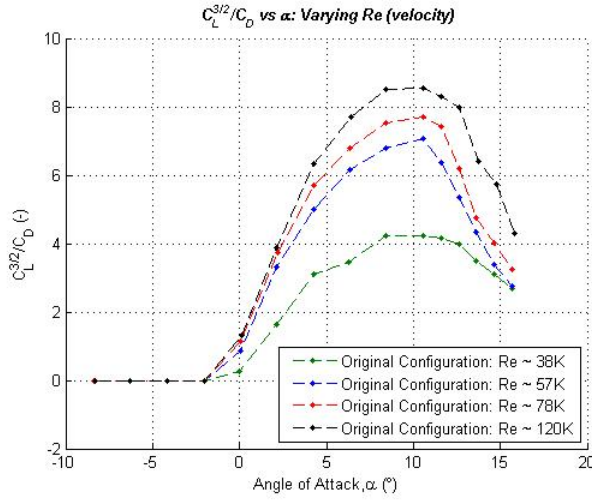
| Re = 78K (40 MPH) | | | | Re = 120K (60 MPH) | | | |
|-------------------|---------|----------------|-----------|--------------------|---------|----------------|-----------|
| | | Error in % L/D | | | | Error in % L/D | |
| α (°) | L/D (-) | Worst | Realistic | α (°) | L/D (-) | Worst | Realistic |
| -8.37 | -4.606 | 0.43% | 0.34% | -8.36 | -5.042 | 0.18% | 0.15% |
| -6.25 | -5.596 | 0.84% | 0.67% | -6.24 | -6.322 | 0.38% | 0.32% |
| -4.13 | -4.790 | 1.30% | 0.94% | -4.12 | -5.031 | 0.59% | 0.42% |
| -2.01 | -1.602 | 1.22% | 1.01% | -2.01 | -0.928 | 0.50% | 0.45% |
| 0.11 | 3.614 | 1.74% | 1.25% | 0.11 | 4.241 | 0.85% | 0.60% |
| 2.15 | 7.769 | 1.98% | 1.49% | 2.14 | 8.770 | 0.94% | 0.71% |
| 4.27 | 9.475 | 1.64% | 1.43% | 4.27 | 11.204 | 0.76% | 0.69% |
| 6.29 | 9.956 | 1.30% | 1.24% | 6.29 | 11.676 | 0.64% | 0.58% |
| 8.40 | 9.718 | 1.26% | 1.04% | 8.41 | 11.308 | 0.61% | 0.49% |
| 10.52 | 9.201 | 1.12% | 0.86% | 10.52 | 10.403 | 0.52% | 0.39% |
| 11.58 | 8.782 | 0.97% | 0.73% | 11.58 | 9.889 | 0.47% | 0.35% |
| 12.63 | 7.249 | 0.63% | 0.48% | 12.63 | 9.358 | 0.42% | 0.31% |
| 13.67 | 5.844 | 0.37% | 0.29% | 13.68 | 8.682 | 0.26% | 0.19% |
| 14.72 | 5.179 | 0.28% | 0.22% | 14.73 | 6.640 | 0.21% | 0.15% |
| 15.75 | 4.615 | 0.18% | 0.16% | 15.77 | 5.206 | 0.12% | 0.09% |

For a Reynolds number of approximately 38K, the worst case error ranges from 0.77% to 7.68% of L/D and the realistic case ranges from 0.74% to 5.62% of L/D. The possible error at L/D_{\max} is 4.23% for the worst case scenario and 3.36% for the realistic

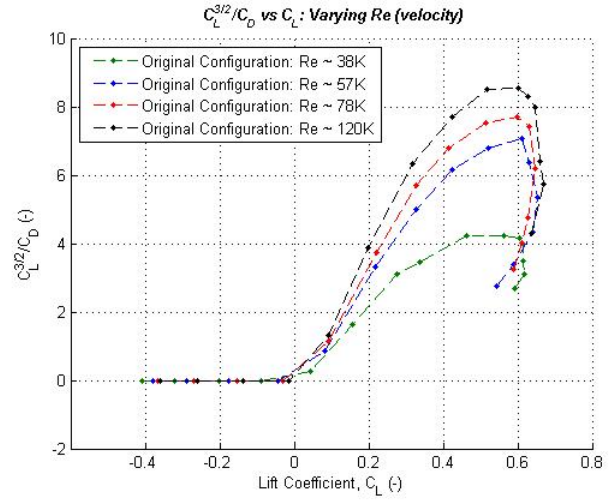
case scenario. For a Reynolds number of approximately 57K, the worst case error ranges from 0.27% to 3.33% of L/D and the realistic case ranges from 0.26% to 2.45% of L/D. The possible error at L/D_{\max} is 1.96% for the worst case scenario and 1.96% for the realistic case scenario. For a Reynolds number of approximately 78K, the worst case error ranges from 0.18% to 1.98% of L/D and the realistic case ranges from 0.16% to 1.49% of L/D. The possible error at L/D_{\max} is 1.30% for the worst case scenario and 1.24% for the realistic case scenario. For a Reynolds number of approximately 120K, the worst case error ranges from 0.12% to 0.94% of L/D and the realistic case ranges from 0.09% to 0.71% of L/D. The possible error at L/D_{\max} is 0.64% for the worst case scenario and 0.58% for the realistic case scenario. As compared to the conservative error percentages, the tested error percentages are much smaller and thus reflect the actual precision of the 10lb balance for measurement.

4.2.1.7 Max Endurance

Figure 77 shows the ratio of $C_L^{3/2}/C_D$ plotted for the Original Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The $C_L^{3/2}/C_D$ has been plotted against α and C_L . $C_L^{3/2}/C_D$ is another measure of aircraft efficiency, more specifically the aircraft's maximum endurance. If an aircraft is flying at an α that corresponds to the maximum $C_L^{3/2}/C_D$, then it is maximizing its time in flight with a set amount of fuel (endurance).



(a)



(b)

Figure 77: $C_L^{3/2}/C_D$ – Max Endurance – Original Configuration Model

(a) $C_L^{3/2}/C_D$ vs. Alpha, (b) $C_L^{3/2}/C_D$ vs. Lift Coefficient

Similar to L/D, there is a strong correlation between an increase in Reynolds number and an increase in $C_L^{3/2}/C_D$ values. $C_L^{3/2}/C_D$ values increase for each Reynolds number case during the range $\alpha \approx -2^\circ$ to 10.5° . Once $C_L^{3/2}/C_{D_{max}}$ is reached for each Reynolds number, the $C_L^{3/2}/C_D$ values start to decrease. This occurs beyond $\alpha \approx 11^\circ$ and $CL \approx 0.6$.

4.2.2 + 5° Cant Configuration Model

4.2.2.1 Summary

In the AFIT low-speed wind tunnel, an α sweep from -8° to 10° in steps of 2° and then from 10° to 15° in steps of 1° was performed on the + 5° Configuration Model at four different speeds: 20 mph (8.94 m/s), 30 mph (13.41 m/s), 40 mph (17.88 m/s), and 60 mph (26.82 m/s). A summary of the resulting aerodynamic performance of the + 5° Configuration Model at $Re \approx 38,000$ (20 mph), $Re \approx 57,000$ (30 mph), $Re \approx 78,000$ (40 mph), and $Re \approx 120,000$ (60 mph) can be seen in Table 12. The Reynolds numbers are based on the average root chord of the upper and lower wings ($\bar{c} = 2.55''$).

Table 12: Aerodynamic Performance of the + 5° Cant Configuration Model

| Model | Re (-) | Min Drag | | Zero Lift | Slopes | |
|--------------------|--------|--------------|-----------------------|--|-----------------------------|-----------------------------|
| | | C_{D0} (-) | α ($^\circ$) | $\alpha_{0 \text{ Lift}}$ ($^\circ$) | $C_{L\alpha}$ (l°) | $C_{m\alpha}$ (l°) |
| + 5° Configuration | 38K | 0.0278 | -2.02 | -0.99 | 0.0539 | 0.0107 |
| + 5° Configuration | 57K | 0.0277 | -2.01 | -1.60 | 0.0562 | 0.0098 |
| + 5° Configuration | 78K | 0.0250 | -2.00 | -1.78 | 0.0536 | 0.0103 |
| + 5° Configuration | 120K | 0.0218 | 0.13 | -1.92 | 0.053 | 0.0113 |

| Model | Re (-) | Max Range | | | | Max Endurance | | | |
|--------------------|--------|-----------|-----------------------|-----------|-----------|-----------------------|-----------------------|-----------|-----------|
| | | L/D (-) | α ($^\circ$) | C_L (-) | C_D (-) | $C_L^{(3/2)}/C_D$ (-) | α ($^\circ$) | C_L (-) | C_D (-) |
| + 5° Configuration | 38K | 6.3652 | 8.44 | 0.5007 | 0.0787 | 4.5040 | 8.44 | 0.5007 | 0.0787 |
| + 5° Configuration | 57K | 9.3534 | 6.34 | 0.4503 | 0.0481 | 6.9491 | 10.58 | 0.6395 | 0.0736 |
| + 5° Configuration | 78K | 10.3334 | 6.33 | 0.4284 | 0.0415 | 7.3994 | 10.56 | 0.5971 | 0.0624 |
| + 5° Configuration | 120K | 11.7204 | 6.33 | 0.4387 | 0.0374 | 8.3031 | 8.45 | 0.5277 | 0.0462 |

4.2.2.2 Drag Coefficient

The drag coefficient, C_D , for the + 5° Cant Configuration Model is shown in Figure 78 for four different Reynolds numbers (38K, 57K, 78K, and 120K). C_D has been plotted both versus C_L and α .

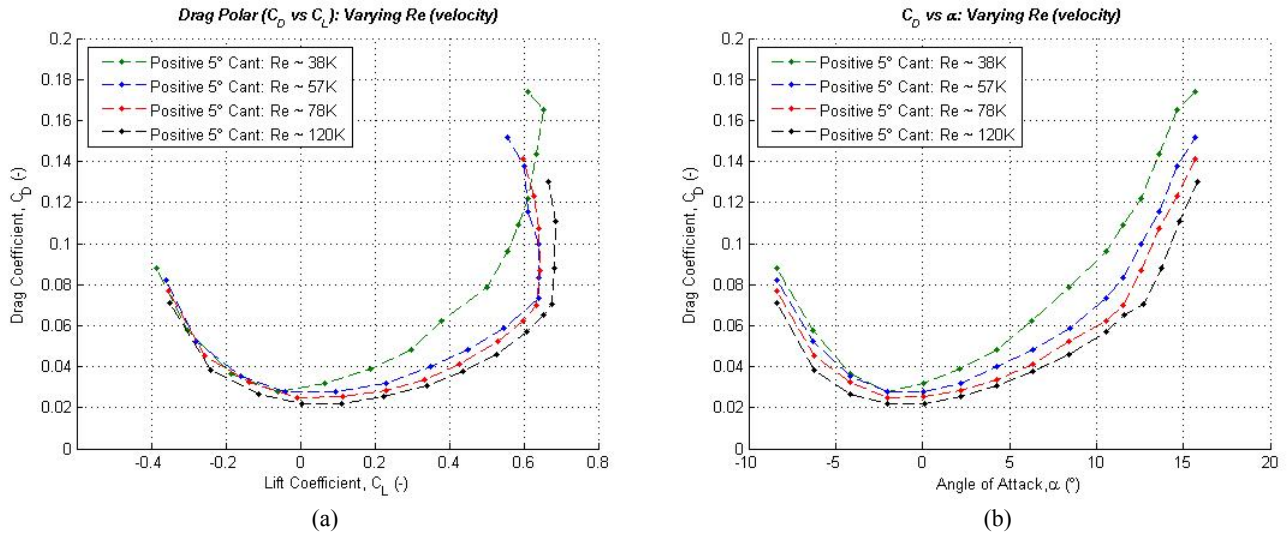


Figure 78: Drag Coefficient – + 5° Cant Configuration Model
(a) Drag Coefficient vs. Lift Coefficient (Drag Polar), (b) Drag Coefficient vs. Alpha

4.2.2.3 Lift Coefficient

Figure 79 plots the lift coefficient, C_L , vs. α for the + 5° Cant Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). As seen in Figure 79, the - 5° Cant Configuration Model exhibits the gradual stall characteristic of most aircraft past an $\alpha = 11^\circ$. $C_{L\alpha}$ is the lift curve slope, and gives a ratio of change of C_L with respect to α for the linear region (α from - 8° to + 8°) of the lift curve, while $\alpha_{0 \text{ Lift}}$ is the angle of attack where the aircraft produces zero lift.

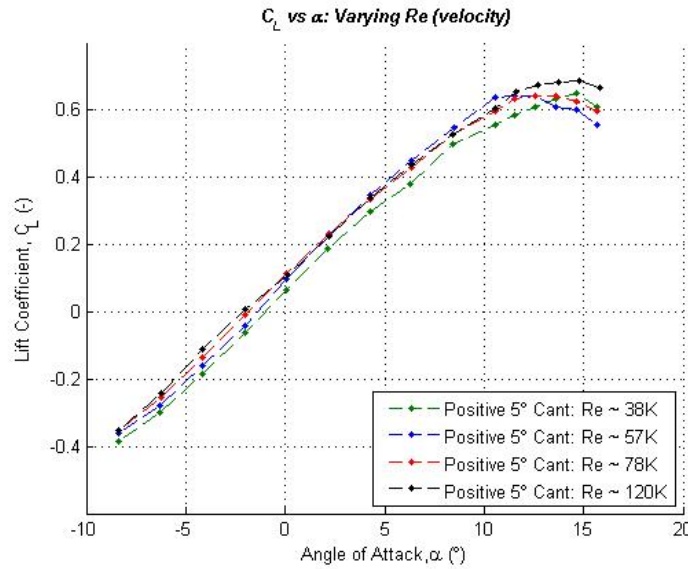


Figure 79: Lift Coefficient vs. Angle of Attack – + 5° Cant Configuration Model

4.2.2.4 Pitching Moment Coefficient

Figure 80 plots the pitching moment coefficient, C_m , vs. α for the + 5° Cant Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The longitudinal static stability derivative, $C_{m\alpha}$, can be attained from the linear portion of this plot (α from - 8° to + 8°). The + 5° Cant Configuration Model is longitudinally unstable, due to a positive $C_{m\alpha}$ value, about the reference CG (2.1625" aft of nose), for all four Reynolds numbers tested.

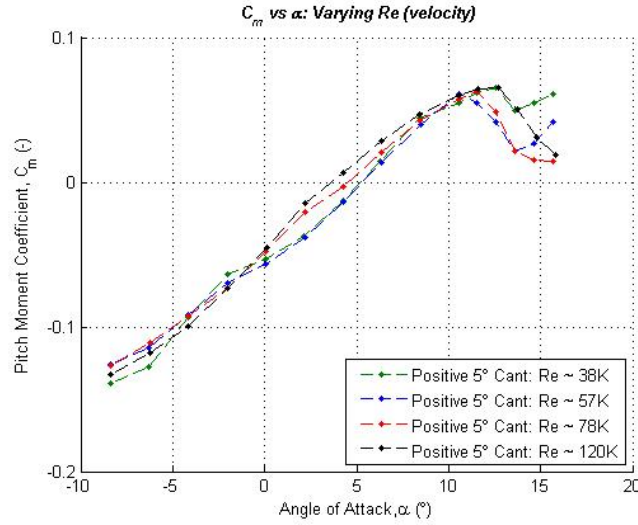
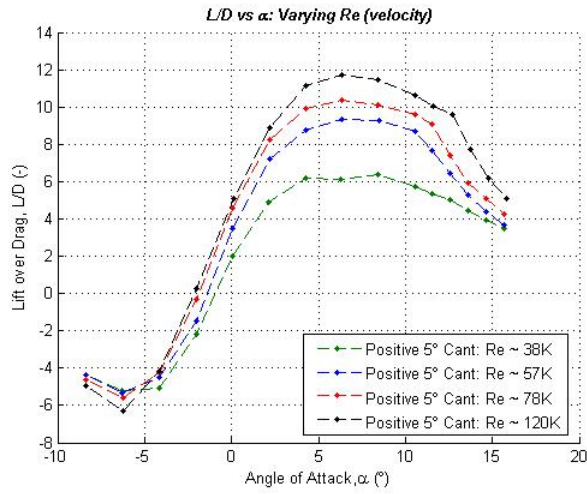


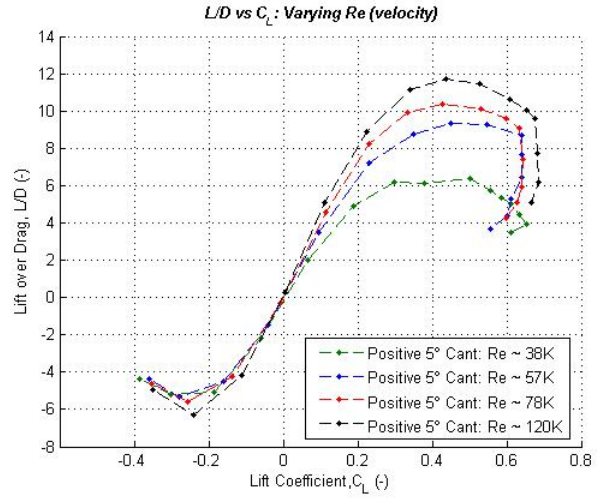
Figure 80: Pitch Moment Coefficient vs. Angle of Attack – + 5° Cant Configuration Model ($X_{cmb} = 1.0025''$)

4.2.2.5 Lift-to-Drag Ratio

Figure 81 shows the lift-to-drag ratio for the + 5° Cant Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). L/D has been plotted versus α and C_L . Lift-to-drag is one measure of aircraft efficiency. The efficiency of the + 5° Cant Configuration Model increases as the Reynolds number increases. L/D values for each Reynolds number increase over the range $\alpha \approx -4^\circ$ to 6° . Once L/D_{max} is reached for each Reynolds number, the L/D values start to decrease. This event occurs beyond $\alpha \approx 6^\circ$ and $C_L \approx 0.41$.



(a)



(b)

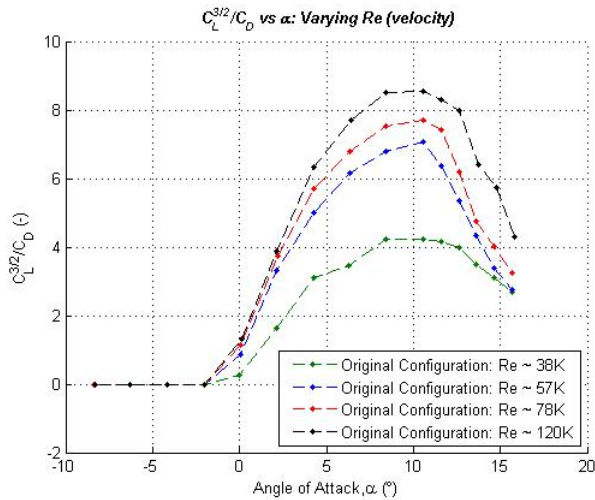
Figure 81: Lift-to-Drag – + 5° Cant Configuration Model

(a) Lift-to-Drag vs. Alpha, (b) Lift-to-Drag vs. Lift Coefficient

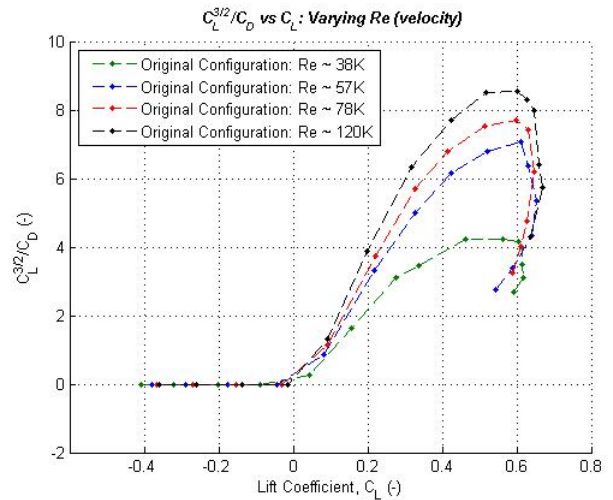
4.2.2.6 Max Endurance

Figure 82 shows the ratio of $C_L^{3/2}/C_D$ plotted for the + 5° Cant Configuration

Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The $C_L^{3/2}/C_D$ has been plotted against α and C_L .



(a)



(b)

Figure 82: $C_L^{3/2}/C_D$ – Max Endurance – + 5° Cant Configuration Model

(a) $C_L^{3/2}/C_D$ vs. Alpha, (b) $C_L^{3/2}/C_D$ vs. Lift Coefficient

4.2.3 - 5° Cant Configuration Model

4.2.3.1 Summary

In the AFIT low-speed wind tunnel, an α sweep from -8° to 10° in steps of 2° and then from 10° to 15° in steps of 1° was performed on the - 5° Configuration Model at four different speeds: 20 mph (8.94 m/s), 30 mph (13.41 m/s), 40 mph (17.88 m/s), and 60 mph (26.82 m/s). A summary of the resulting aerodynamic performance of the - 5° Configuration Model at $Re \approx 38,000$ (20 mph), $Re \approx 57,000$ (30 mph), $Re \approx 78,000$ (40 mph), and $Re \approx 120,000$ (60 mph) can be seen in Table 13. The Reynolds numbers are based on the average root chord of the upper and lower wings ($\bar{c} = 2.55''$).

Table 13: Aerodynamic Performance of the – 5° Cant Configuration Model

| Model | Re (-) | Min Drag | | Zero Lift | Slopes | |
|--------------------|--------|--------------|--------------|-------------------------------|--------------------|--------------------|
| | | C_{Do} (-) | α (°) | $\alpha_{0 \text{ Lift}}$ (°) | $C_{L\alpha}$ (/°) | $C_{m\alpha}$ (/°) |
| - 5° Configuration | 38K | 0.0324 | 0.00 | -0.07 | 0.0529 | 0.0102 |
| - 5° Configuration | 57K | 0.0273 | 0.01 | -0.57 | 0.0569 | 0.0101 |
| - 5° Configuration | 78K | 0.0241 | 0.10 | -0.65 | 0.0541 | 0.0105 |
| - 5° Configuration | 120K | 0.0201 | 0.11 | -0.88 | 0.0536 | 0.0112 |

| Model | Re (-) | Max Range | | | | Max Endurance | | | |
|--------------------|--------|-----------|--------------|-----------|-----------|-----------------------|--------------|-----------|-----------|
| | | L/D (-) | α (°) | C_L (-) | C_D (-) | $C_L^{(3/2)}/C_D$ (-) | α (°) | C_L (-) | C_D (-) |
| - 5° Configuration | 38K | 6.7311 | 8.42 | 0.4335 | 0.0644 | 4.5486 | 10.46 | 0.5422 | 0.0878 |
| - 5° Configuration | 57K | 9.3586 | 8.44 | 0.5054 | 0.0540 | 6.6534 | 8.44 | 0.5054 | 0.0540 |
| - 5° Configuration | 78K | 10.4259 | 8.43 | 0.4643 | 0.0445 | 7.2532 | 10.55 | 0.5486 | 0.0560 |
| - 5° Configuration | 120K | 11.9833 | 6.40 | 0.3945 | 0.0329 | 8.3134 | 8.43 | 0.4842 | 0.0405 |

4.2.3.2 Drag Coefficient

The drag coefficient, C_D , for the - 5° Cant Configuration Model is shown in Figure 83 for four different Reynolds numbers (38K, 57K, 78K, and 120K). C_D has been plotted both versus C_L and α .

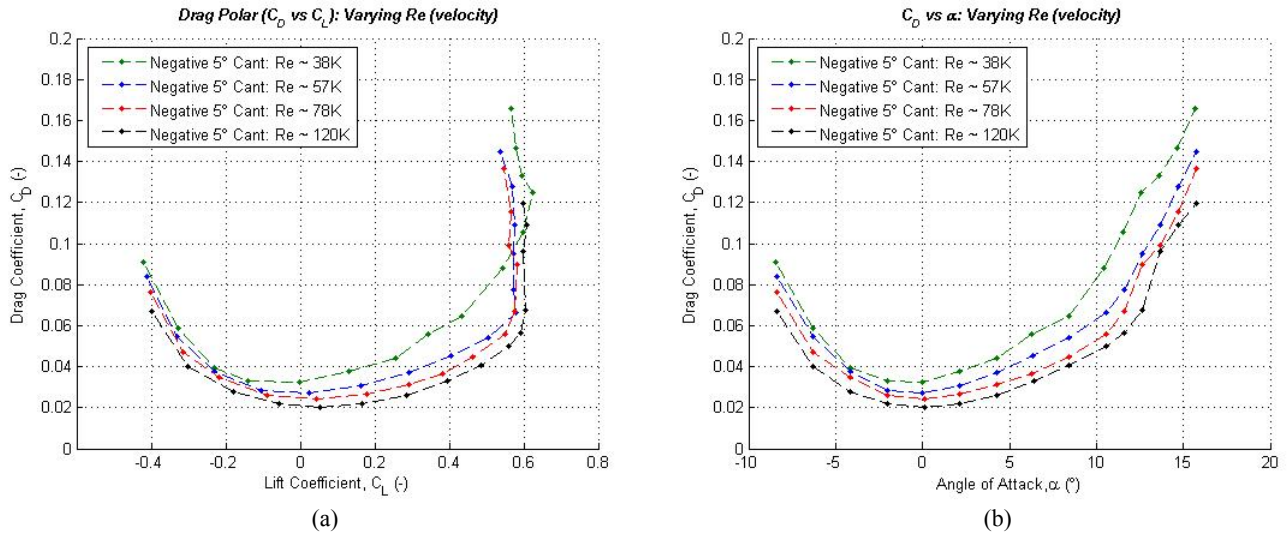


Figure 83: Drag Coefficient -- 5° Cant Configuration Model
(a) Drag Coefficient vs. Lift Coefficient (Drag Polar), (b) Drag Coefficient vs. Alpha

4.2.3.3 Lift Coefficient

Figure 84 plots the lift coefficient, C_L , vs. α for the -5° Cant Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). As seen in Figure 84, the -5° Cant Configuration Model exhibits the gradual stall characteristic of most aircraft past an $\alpha = 12^\circ$.

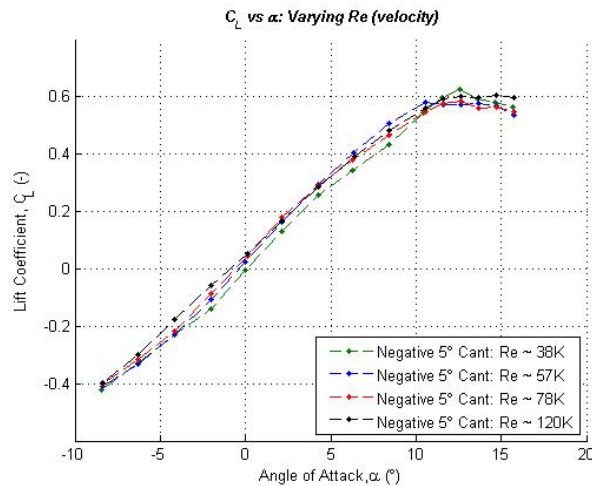


Figure 84: Lift Coefficient vs. Angle of Attack -- 5° Cant Configuration Model

4.2.3.4 Pitching Moment Coefficient

Figure 85 plots the pitching moment coefficient, C_m , vs. α for the - 5° Cant Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The - 5° Cant Configuration Model is longitudinally unstable, due to a positive $C_{m\alpha}$ value, about the reference CG (2.1625" aft of nose), for all four Reynolds numbers tested.

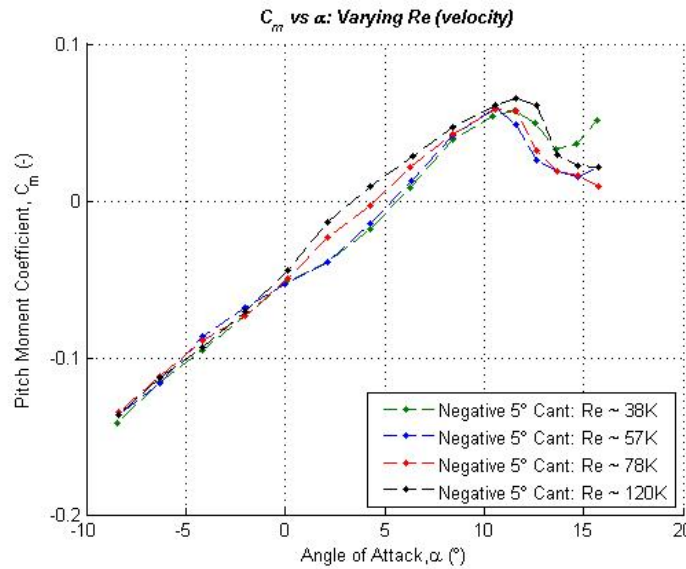
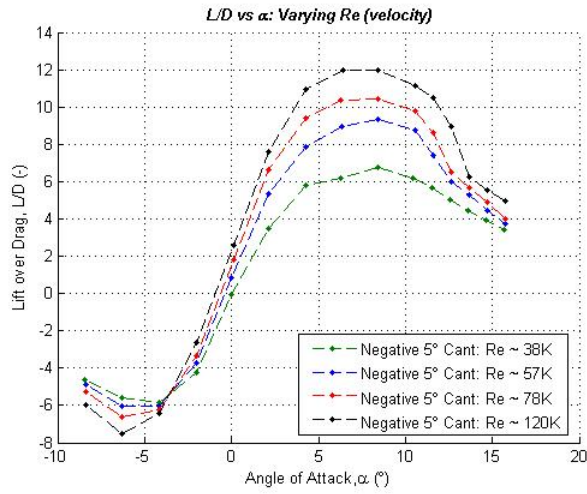


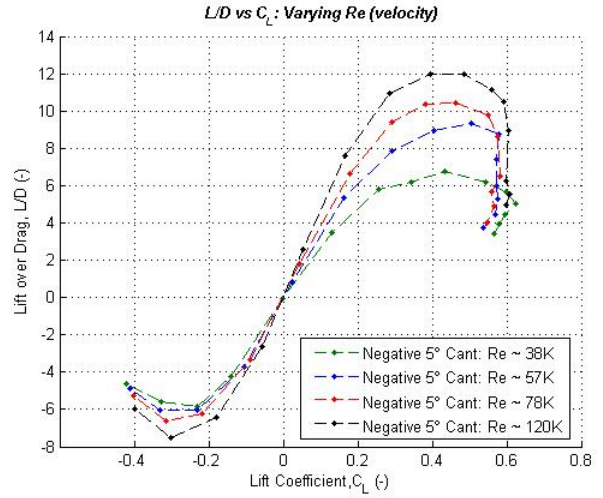
Figure 85: Pitch Moment Coefficient vs. Angle of Attack – - 5° Cant Configuration Model ($X_{cmb} = 1.0025"$)

4.2.3.5 Lift-to-Drag Ratio

Figure 86 shows the lift-to-drag ratio for the - 5° Cant Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). L/D has been plotted versus α and C_L . As the Reynolds number increases, the efficiency of the - 5° Cant Configuration Model increases as well. L/D values for each Reynolds number increase over the range $\alpha \approx -4^\circ$ to 7° . Once L/D_{max} is reached for each Reynolds number, the L/D values start to decrease. This event occurs beyond $\alpha \approx 7^\circ$ and $C_L \approx 0.43$.



(a)



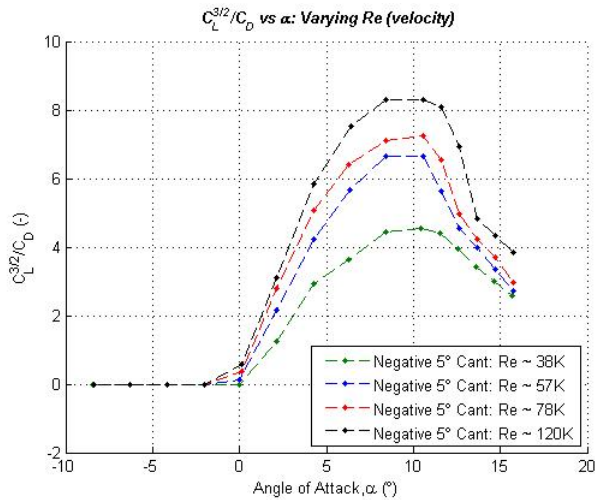
(b)

Figure 86: Lift-to-Drag – - 5° Cant Configuration Model

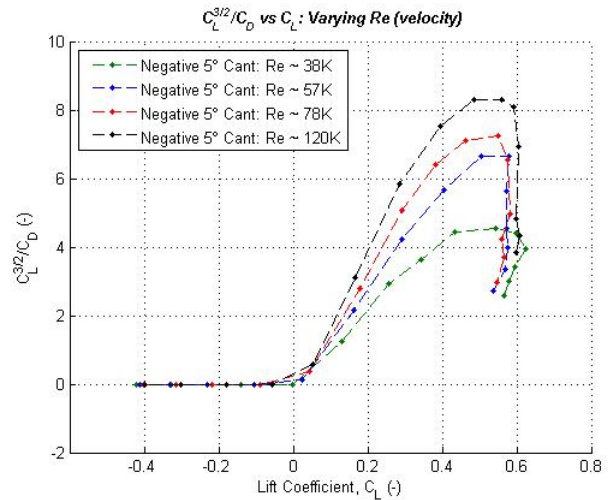
(a) Lift-to-Drag vs. Alpha, (b) Lift-to-Drag vs. Lift Coefficient

4.2.3.6 Max Endurance

Figure 87 shows the ratio of $C_L^{3/2}/C_D$ plotted for the - 5° Cant Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The $C_L^{3/2}/C_D$ has been plotted against α and C_L .



(a)



(b)

Figure 87: $C_L^{3/2}/C_D$ – Max Endurance – - 5° Cant Configuration Model

(a) $C_L^{3/2}/C_D$ vs. Alpha, (b) $C_L^{3/2}/C_D$ vs. Lift Coefficient

4.2.4 Endplate Configuration Model

4.2.4.1 Summary

In the AFIT low-speed wind tunnel, an α sweep from -8° to 10° in steps of 2° and then from 10° to 15° in steps of 1° was performed on the Endplate Configuration Model at four different speeds: 20 mph (8.94 m/s), 30 mph (13.41 m/s), 40 mph (17.88 m/s), and 60 mph (26.82 m/s). A summary of the resulting aerodynamic performance of the Endplate Configuration Model at $Re \approx 38,000$ (20 mph), $Re \approx 57,000$ (30 mph), $Re \approx 78,000$ (40 mph), and $Re \approx 120,000$ (60 mph) can be seen in Table 14. The Reynolds numbers are based on the average root chord of the upper and lower wings ($\bar{c} = 2.55''$).

Table 14: Aerodynamic Performance of the – Endplate Configuration Model

| Model | Re (-) | Min Drag | | Zero Lift | Slopes | |
|------------------------|--------|--------------|-----------------------|--|----------------------------|----------------------------|
| | | C_{Do} (-) | α ($^\circ$) | $\alpha_{0 \text{ Lift}}$ ($^\circ$) | $C_{L\alpha}$ ($^\circ$) | $C_{m\alpha}$ ($^\circ$) |
| Endplate Configuration | 38K | 0.0344 | 0.10 | -0.72 | 0.0578 | 0.0114 |
| Endplate Configuration | 57K | 0.0296 | 0.11 | -1.25 | 0.0575 | 0.0106 |
| Endplate Configuration | 78K | 0.0278 | 0.11 | -1.37 | 0.0559 | 0.0112 |
| Endplate Configuration | 120K | 0.0251 | 0.11 | -1.40 | 0.0546 | 0.0125 |

| Model | Re (-) | Max Range | | | | Max Endurance | | | |
|------------------------|--------|-----------|-----------------------|-----------|-----------|-----------------------|-----------------------|-----------|-----------|
| | | L/D (-) | α ($^\circ$) | C_L (-) | C_D (-) | $C_L^{(3/2)}/C_D$ (-) | α ($^\circ$) | C_L (-) | C_D (-) |
| Endplate Configuration | 38K | 6.3733 | 6.38 | 0.4194 | 0.0658 | 4.6633 | 10.53 | 0.6246 | 0.1059 |
| Endplate Configuration | 57K | 8.6825 | 6.39 | 0.4453 | 0.0513 | 6.4561 | 10.52 | 0.6051 | 0.0729 |
| Endplate Configuration | 78K | 9.2024 | 8.41 | 0.5198 | 0.0565 | 6.9288 | 10.52 | 0.6064 | 0.0682 |
| Endplate Configuration | 120K | 10.3918 | 8.41 | 0.5281 | 0.0508 | 7.6841 | 10.53 | 0.6157 | 0.0629 |

4.2.4.2 Drag Coefficient

The drag coefficient, C_D , for the Endplate Configuration Model is shown in Figure 88 for four different Reynolds numbers (38K, 57K, 78K, and 120K). C_D has been plotted both versus C_L and α .

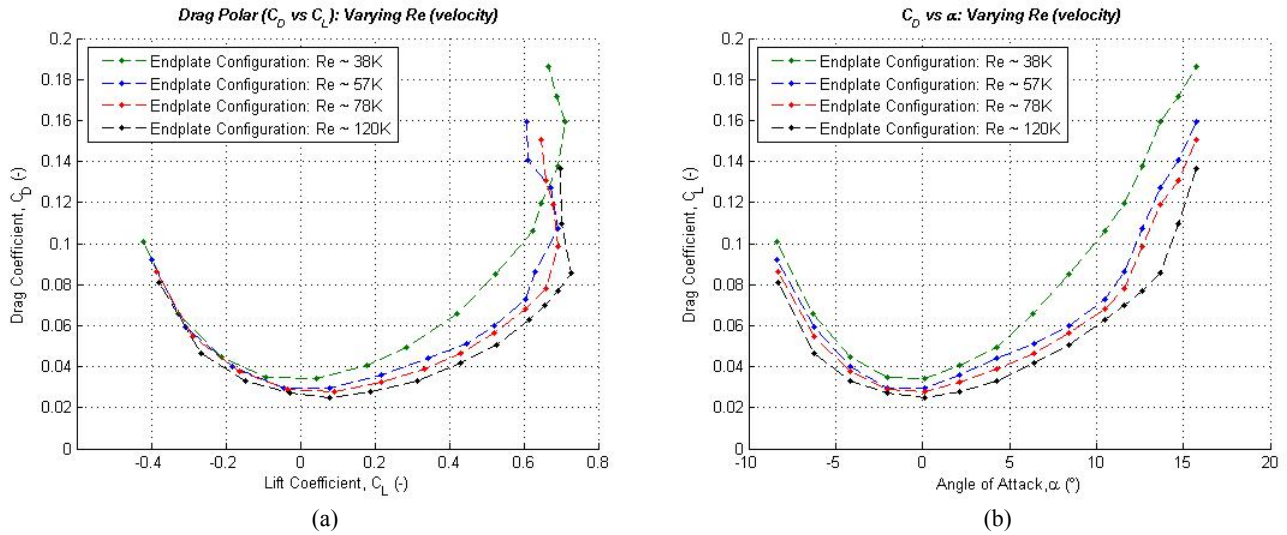


Figure 88: Drag Coefficient – Endplate Configuration Model
(a) Drag Coefficient vs. Lift Coefficient (Drag Polar), (b) Drag Coefficient vs. Alpha

4.2.4.3 Lift Coefficient

Figure 89 plots the lift coefficient, C_L , vs. α for the Endplate Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). As seen in Figure 89, the Endplate Configuration Model exhibits the gradual stall characteristic of most aircraft past an $\alpha = 13^\circ$.

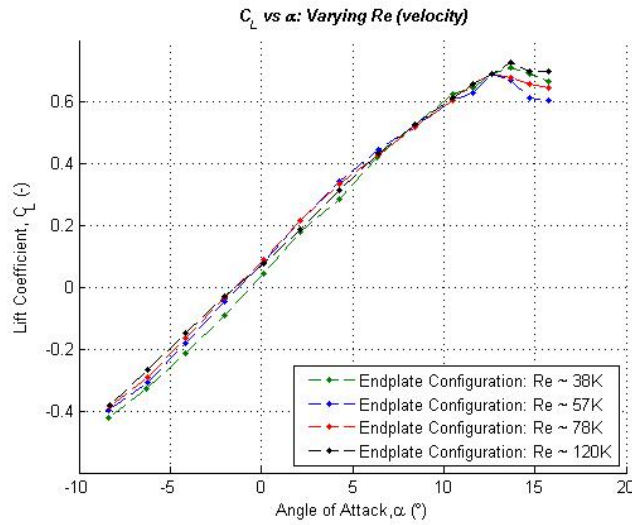


Figure 89: Lift Coefficient vs. Angle of Attack – Endplate Configuration Model

4.2.4.4 Pitching Moment Coefficient

Figure 90 plots the pitching moment coefficient, C_m , vs. α for the Endplate Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The longitudinal static stability derivative, $C_{m\alpha}$, can be attained from the linear portion of this plot (α from -8° to $+8^\circ$). The Endplate Configuration Model is longitudinally unstable for all four Reynolds numbers tested.

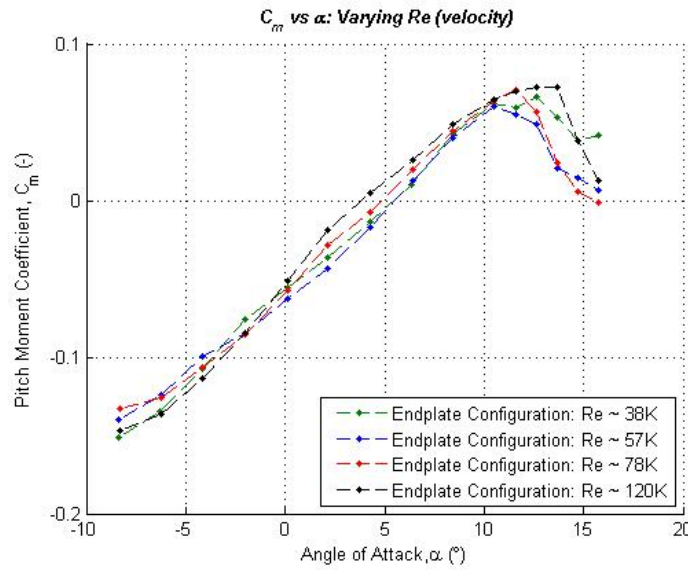
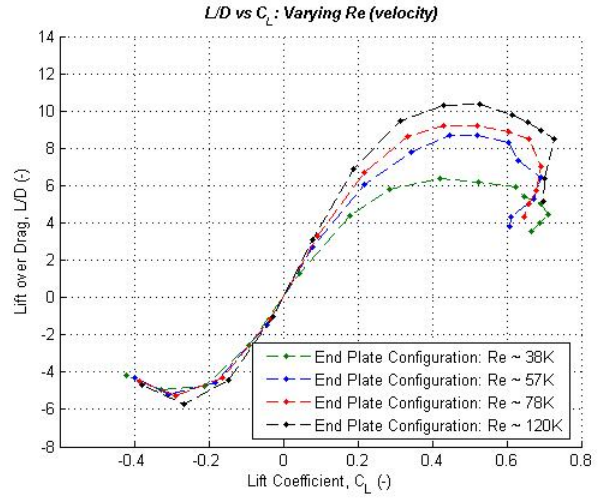
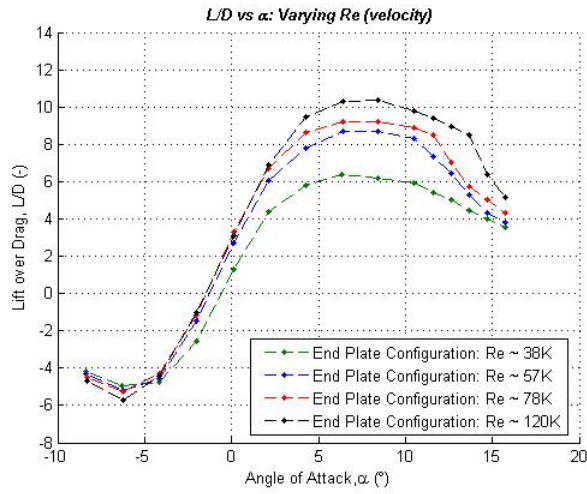


Figure 90: Pitch Moment Coefficient vs. Angle of Attack – Endplate Configuration Model ($X_{cmb} = 1.0025''$)

4.2.4.5 Lift-to-Drag Ratio

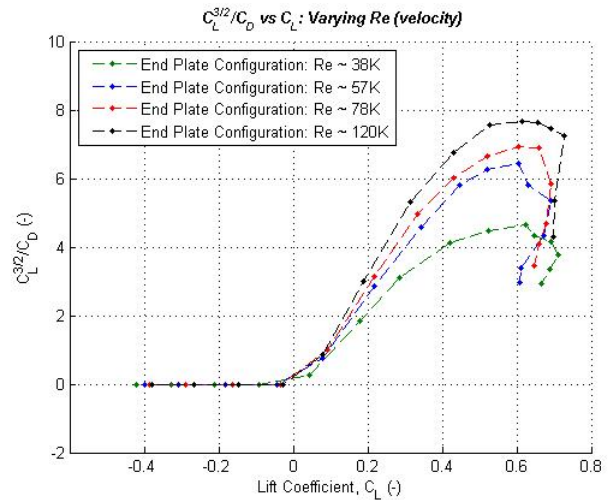
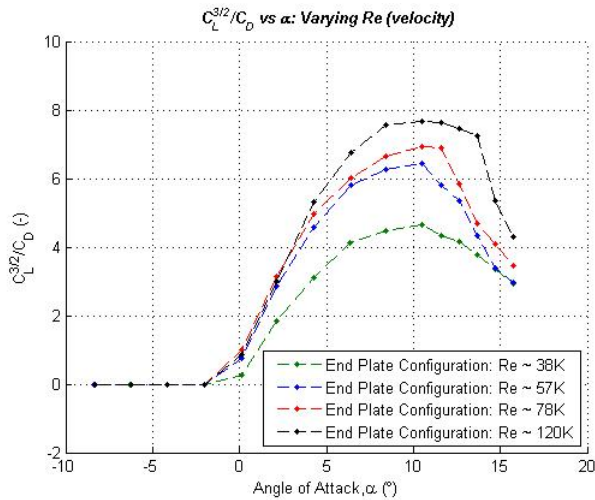
Figure 91 shows the lift-to-drag ratio for the Endplate Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). L/D has been plotted versus α and C_L .



(a) (b)
Figure 91: Lift-to-Drag – Endplate Configuration Model
 (a) Lift-to-Drag vs. Alpha, (b) Lift-to-Drag vs. Lift Coefficient

4.2.4.6 Max Endurance

Figure 92 shows the ratio of $C_L^{3/2}/C_D$ plotted for the Endplate Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The $C_L^{3/2}/C_D$ has been plotted against α and C_L .



(a) (b)
Figure 92: $C_L^{3/2}/C_D$ – Max Endurance – Endplate Configuration Model
 (a) $C_L^{3/2}/C_D$ vs. Alpha, (b) $C_L^{3/2}/C_D$ vs. Lift Coefficient

4.2.5 No Flow Guide Configuration Model

4.2.5.1 Summary

In the AFIT low-speed wind tunnel, an α sweep from -8° to 10° in steps of 2° and then from 10° to 15° in steps of 1° was performed on the No Flow Guide Configuration Model at four different speeds: 20 mph (8.94 m/s), 30 mph (13.41 m/s), 40 mph (17.88 m/s), and 60 mph (26.82 m/s). A summary of the resulting aerodynamic performance of the No Flow Guide Configuration Model at $Re \approx 38,000$ (20 mph), $Re \approx 57,000$ (30 mph), $Re \approx 78,000$ (40 mph), and $Re \approx 120,000$ (60 mph) can be seen in Table 15. The Reynolds numbers are based on the average root chord of the upper and lower wings ($\bar{c} = 2.55''$).

Table 15: Aerodynamic Performance of the – No Flow Guide Configuration Model

| Model | Re (-) | Min Drag | | Zero Lift | Slopes | |
|-----------------------------|--------|--------------|-----------------------|-------------------------------|-----------------------|-----------------------|
| | | C_{Do} (-) | α ($^\circ$) | α_{0Lift} ($^\circ$) | C_{La} ($^\circ$) | C_{ma} ($^\circ$) |
| No Flow Guide Configuration | 38K | 0.0260 | 0.10 | -0.63 | 0.0576 | 0.0111 |
| No Flow Guide Configuration | 57K | 0.0268 | 0.11 | -1.09 | 0.0565 | 0.0100 |
| No Flow Guide Configuration | 78K | 0.0233 | 0.11 | -1.31 | 0.0539 | 0.0104 |
| No Flow Guide Configuration | 120K | 0.0195 | 0.11 | -1.58 | 0.0523 | 0.0115 |

| Model | Re (-) | Max Range | | | | Max Endurance | | | |
|-----------------------------|--------|-----------|-----------------------|-----------|-----------|-----------------------|-----------------------|-----------|-----------|
| | | L/D (-) | α ($^\circ$) | C_L (-) | C_D (-) | $C_L^{(3/2)}/C_D$ (-) | α ($^\circ$) | C_L (-) | C_D (-) |
| No Flow Guide Configuration | 38K | 6.9259 | 6.29 | 0.4085 | 0.0590 | 4.5238 | 10.52 | 0.5960 | 0.1017 |
| No Flow Guide Configuration | 57K | 9.0696 | 6.30 | 0.4248 | 0.0468 | 6.3719 | 10.52 | 0.5981 | 0.0726 |
| No Flow Guide Configuration | 78K | 9.9634 | 6.29 | 0.4052 | 0.0407 | 7.1055 | 10.52 | 0.5962 | 0.0648 |
| No Flow Guide Configuration | 120K | 11.6871 | 6.29 | 0.4145 | 0.0355 | 8.1126 | 10.52 | 0.6086 | 0.0585 |

4.2.5.2 Drag Coefficient

The drag coefficient, C_D , for the No Flow Guide Configuration Model is shown in Figure 93 for four different Reynolds numbers (38K, 57K, 78K, and 120K). C_D has been plotted both versus C_L and α .

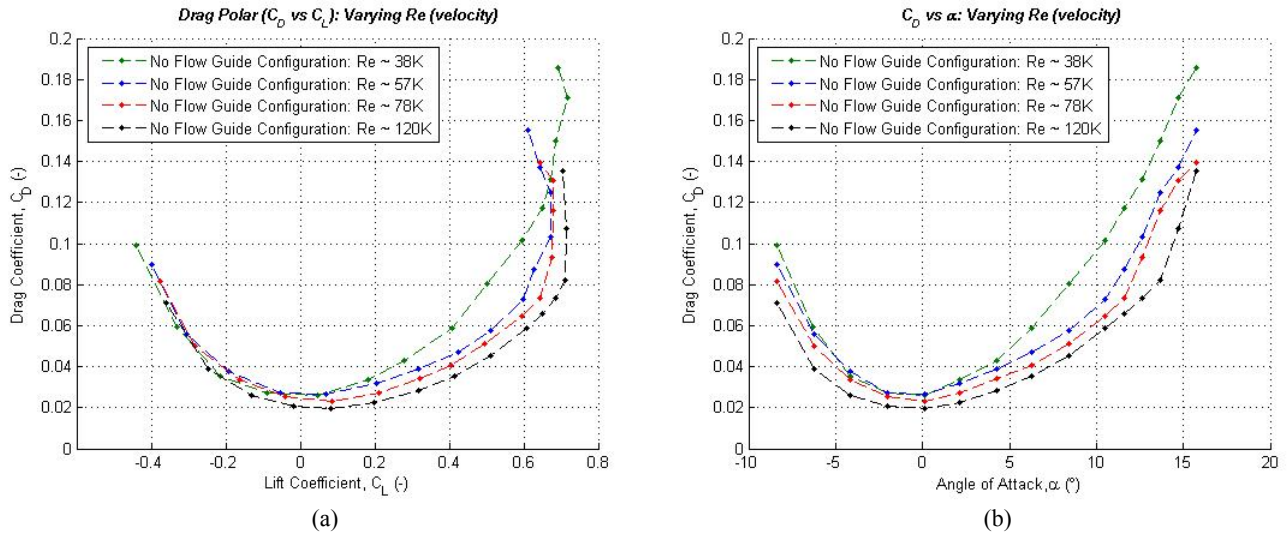


Figure 93: Drag Coefficient – No Flow Guide Configuration Model
(a) Drag Coefficient vs. Lift Coefficient (Drag Polar), (b) Drag Coefficient vs. Alpha

4.2.5.3 Lift Coefficient

Figure 94 plots the lift coefficient, C_L , vs. α for the No Flow Guide Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). As seen in Figure 94, the No Flow Guide Configuration Model exhibits the gradual stall characteristic of most aircraft past an $\alpha = 13^\circ$.

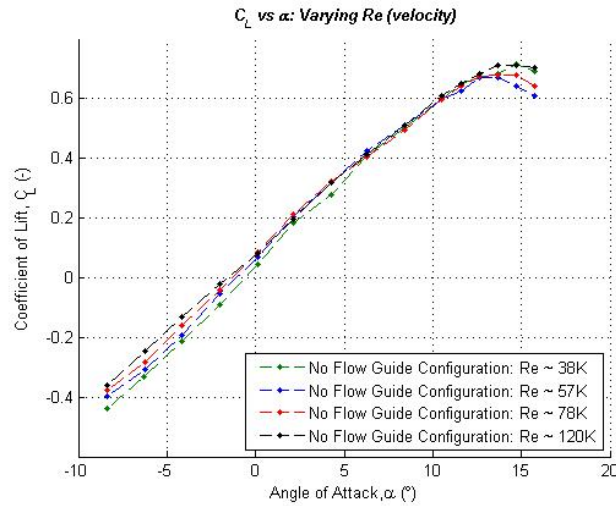


Figure 94: Lift Coefficient vs. Angle of Attack – No Flow Guide Configuration Model

4.2.5.4 Pitching Moment Coefficient

Figure 95 plots the pitching moment coefficient, C_m , vs. α for the No Flow Guide Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). The Endplate Configuration Model is longitudinally unstable, due to a positive $C_{m\alpha}$ value, about the reference CG (2.1625" aft of nose), for all four Reynolds numbers tested.

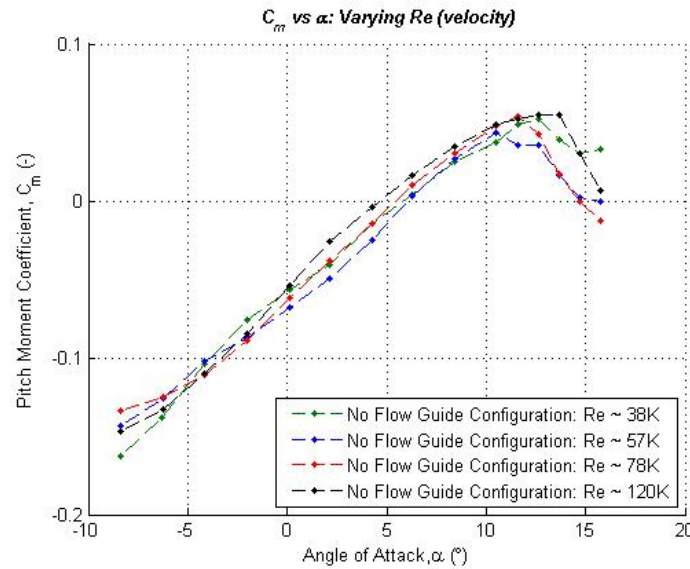
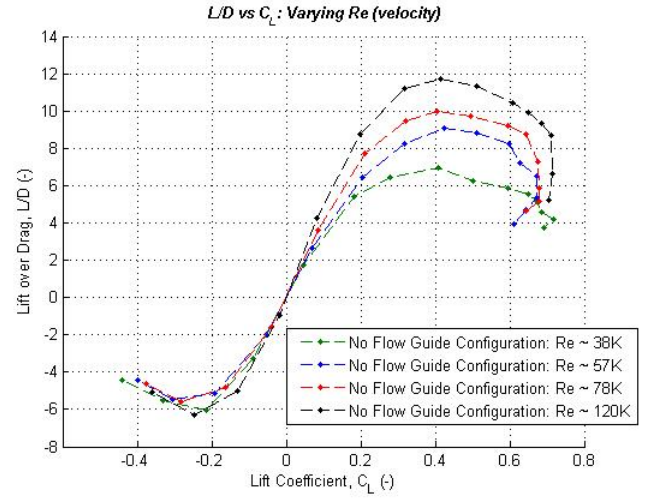
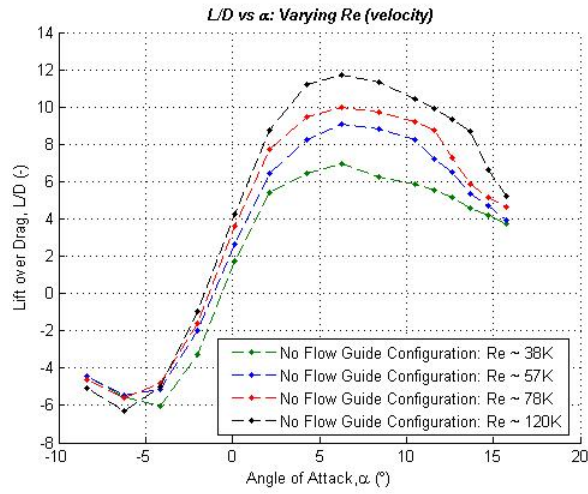


Figure 95: Pitch Moment Coefficient vs. Angle of Attack – No Flow Guide Configuration Model ($X_{cmb} = 1.0025"$)

4.2.5.5 Lift-to-Drag Ratio

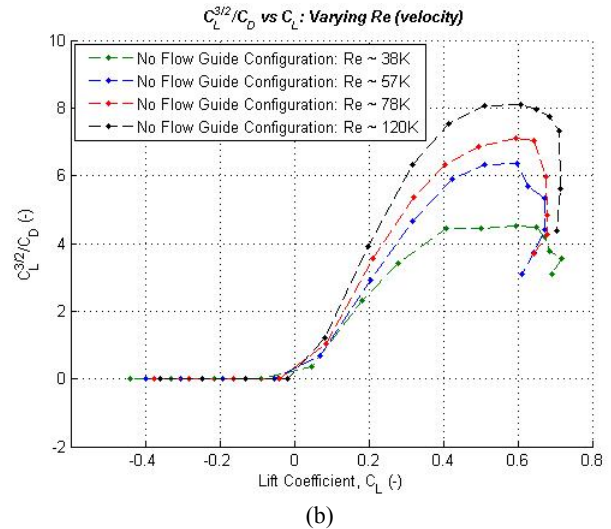
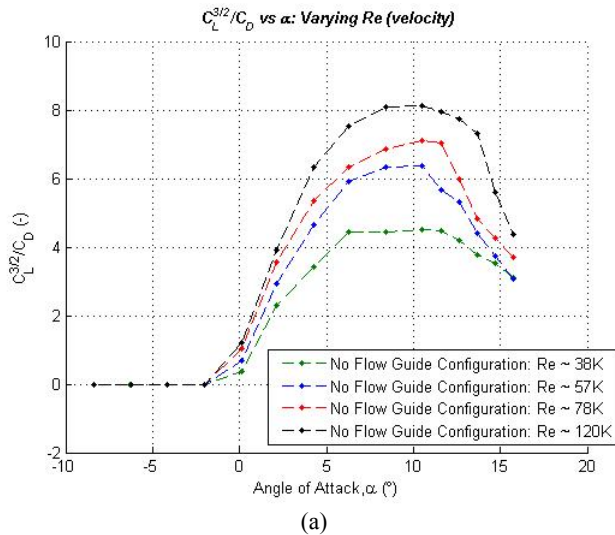
Figure 96 shows the lift-to-drag ratio for the No Flow Guide Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K). L/D has been plotted versus α and C_L .



(a) (b)
Figure 96: Lift-to-Drag – No Flow Guide Configuration Model
 (a) Lift-to-Drag vs. Alpha, (b) Lift-to-Drag vs. Lift Coefficient

4.2.5.6 Max Endurance

Figure 97 shows the ratio of $C_L^{3/2}/C_D$ plotted for the No Flow Guide Configuration Model at four different Reynolds numbers (38K, 57K, 78K, and 120K).



(a) (b)
Figure 97: $C_L^{3/2}/C_D$ – Max Endurance – No Flow Guide Configuration Model
 (a) $C_L^{3/2}/C_D$ vs. Alpha, (b) $C_L^{3/2}/C_D$ vs. Lift Coefficient

4.3 Wind Tunnel Data – Alpha Sweeps: Model Comparisons by Speed

4.3.1 $Re \approx 38K$ / 20 MPH

4.3.1.1 Summary

The data results of the five model configurations, which were presented in Section 4.2 at a Reynolds number of 38K (20 mph or 8.94 m/s), are compared to gauge the differences in aerodynamic performance of the models. The models that were included in the test were: the Original Configuration Model, the + 5° Cant Configuration Model, the – 5° Cant Configuration Model, the Endplate Configuration Model, and the No Flow Guide Configuration Model. The No Flow Guide Configuration Model served as the reference to base all the performance parameters.

A summary of aerodynamic performance comparisons between the five model configurations can be seen in Table 15. A discussion of the performance factors: drag, maximum range, maximum endurance, and effective aspect ratio will be discussed in this section with corresponding figures.

Table 16: Summary of the Aerodynamic Performance Comparison of the Five Models – $Re \sim 38K$

| Model Configuration | Re (-) | S (in ²) | b (in) | Minimum Drag | | | Zero Lift | Slopes | |
|---------------------|--------|----------------------|--------|--------------|--------------|--------|-------------------------------|--------------------|--------------------|
| | | | | C_{D0} (-) | α (°) | D (lb) | $\alpha_{0 \text{ Lift}}$ (°) | $C_{L\alpha}$ (l°) | $C_{m\alpha}$ (l°) |
| Original | 38K | 72.58 | 13.81 | 0.0327 | -2.03 | 0.015 | -0.52 | 0.053 | 0.011 |
| +5° Cant | 38K | 72.56 | 13.81 | 0.0278 | -2.02 | 0.014 | -0.99 | 0.054 | 0.011 |
| -5° Cant | 38K | 72.56 | 13.81 | 0.0324 | 0.00 | 0.016 | -0.07 | 0.053 | 0.010 |
| Endplate | 38K | 58.33 | 11.50 | 0.0344 | 0.10 | 0.012 | -0.72 | 0.058 | 0.011 |
| No Flow Guide | 38K | 58.02 | 11.38 | 0.0260 | 0.10 | 0.009 | -0.63 | 0.058 | 0.011 |

| Model Configuration | Re (-) | S (in ²) | b (in) | Maximum Range | | | | | |
|---------------------|--------|----------------------|--------|-----------------|--------------|-----------|-----------|--------|--------|
| | | | | L/D_{max} (-) | α (°) | C_L (-) | C_D (-) | L (lb) | D (lb) |
| Original | 38K | 72.58 | 13.81 | 6.2241 | 8.43 | 0.4631 | 0.0744 | 0.217 | 0.035 |
| +5° Cant | 38K | 72.56 | 13.81 | 6.3652 | 8.44 | 0.5007 | 0.0787 | 0.233 | 0.037 |
| -5° Cant | 38K | 72.56 | 13.81 | 6.7311 | 8.42 | 0.4335 | 0.0644 | 0.213 | 0.032 |
| Endplate | 38K | 58.33 | 11.50 | 6.3733 | 6.38 | 0.4194 | 0.0658 | 0.153 | 0.024 |
| No Flow Guide | 38K | 58.02 | 11.38 | 6.9259 | 6.29 | 0.4085 | 0.0590 | 0.146 | 0.021 |

| Model Configuration | Re (-) | S (in ²) | b (in) | Maximum Endurance | | | | | |
|---------------------|--------|----------------------|--------|----------------------------|--------------|-----------|-----------|--------|--------|
| | | | | $C_L^{(3/2)}/C_{Dmax}$ (-) | α (°) | C_L (-) | C_D (-) | L (lb) | D (lb) |
| Original | 38K | 72.58 | 13.81 | 4.2385 | 10.55 | 0.5625 | 0.0995 | 0.248 | 0.044 |
| +5° Cant | 38K | 72.56 | 13.81 | 4.5040 | 8.44 | 0.5007 | 0.0787 | 0.233 | 0.037 |
| -5° Cant | 38K | 72.56 | 13.81 | 4.5486 | 10.46 | 0.5422 | 0.0878 | 0.249 | 0.040 |
| Endplate | 38K | 58.33 | 11.50 | 4.6633 | 10.53 | 0.6246 | 0.1059 | 0.225 | 0.038 |
| No Flow Guide | 38K | 58.02 | 11.38 | 4.5238 | 10.52 | 0.5960 | 0.1017 | 0.213 | 0.036 |

4.3.1.2 Drag

Figure 98 plots the drag polar, C_D vs. C_L , for the five model configurations at a Reynolds number of 38K. The No Flow Guide Configuration has the lowest value of C_{D0} of all the five configurations. Table 17 compares the induced and parasite drag between all the model configurations. It is interesting to note at a Reynolds number of 38K the Endplate configuration had the least amount of induced drag percentage of the total drag. The – 5° Cant Configuration had the highest lift-to-induced drag of all the models whereas the +5° Cant Configuration had the lowest lift-to-induced drag. This phenomenon is probably due to the effective angle of attack of the flow guide which can be seen by the parameter induced drag to total drag, C_{Di}/C_D .

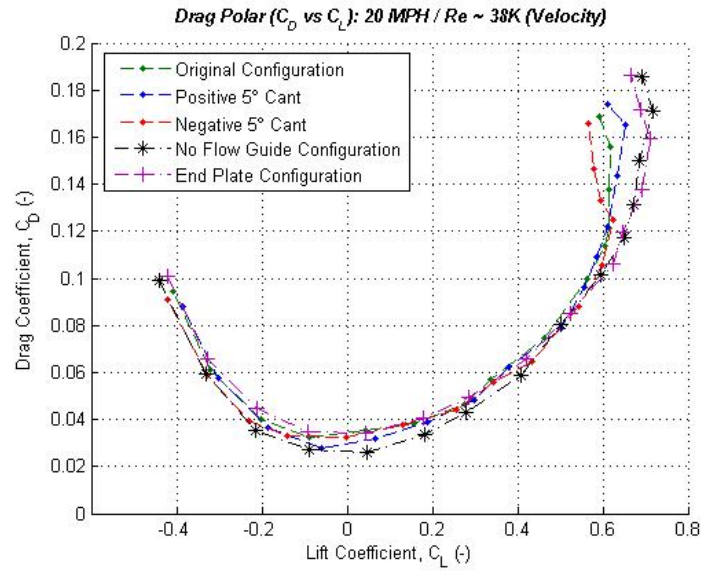


Figure 98: Drag Polar vs. Angle of Attack – Re ~ 38K / 20MPH

Table 17: Comparison of Induced and Parasite Drag of the Five Models – Re ~ 38K

| Model Configuration | Re (-) | L/D _{max} (-) | C _D (-) | C _{Do} (-) | C _{Di} (-) | C _{Di} /C _D (-) | L (lb) | D (lb) | D _{min} (lb) | D _i (lb) | L/D _i (-) |
|---------------------|--------|------------------------|--------------------|---------------------|---------------------|-------------------------------------|--------|--------|-----------------------|---------------------|----------------------|
| Original | 38K | 6.2241 | 0.0744 | 0.0327 | 0.0417 | 56.0% | 0.217 | 0.035 | 0.015 | 0.020 | 10.92 |
| +5° Cant | 38K | 6.3652 | 0.0787 | 0.0278 | 0.0508 | 64.6% | 0.233 | 0.037 | 0.014 | 0.023 | 10.31 |
| -5° Cant | 38K | 6.7311 | 0.0644 | 0.0324 | 0.0320 | 49.7% | 0.213 | 0.032 | 0.016 | 0.016 | 13.64 |
| Endplate | 38K | 6.3733 | 0.0658 | 0.0344 | 0.0314 | 47.7% | 0.153 | 0.024 | 0.012 | 0.012 | 13.26 |
| No Flow Guide | 38K | 6.9259 | 0.0590 | 0.0260 | 0.0330 | 56.0% | 0.146 | 0.021 | 0.009 | 0.012 | 12.11 |

4.3.1.3 Maximum Range and Endurance

A plot of lift-to-drag versus angle of attack for the five model configurations can be seen in Figure 98. A summary of the results is located in Table 16 and the percent change between models can be seen in Table 18. The No Flow Guide Configuration was the reference point for the other configurations. These results will help determine the best configuration for endurance. For a $Re \approx 38K$, the models with flow guides had a lower L/D_{max} than the reference No Flow Guide Configuration due to increased parasite drag.

The +5° Cant Configuration and the -5° Cant Configuration are shifted to either side of the Original Configuration due to the effective angle of attack of the canted flow guides.

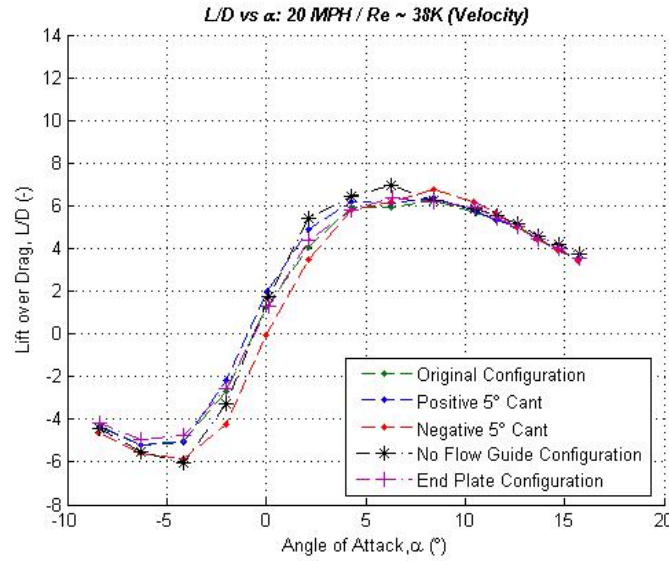


Figure 99: Lift-to-Drag vs. Angle of Attack – Re ~ 38K / 20MPH

Table 18: Comparison of L/D_{\max} and $C_L^{3/2}/C_{D\max}$ of the Five Models – Re ~ 38K

| Model Configuration | Re (-) | % Change from No Flow Guide | |
|---------------------|--------|-----------------------------|-----------------------|
| | | L/D_{\max} | $C_L^{3/2}/C_{D\max}$ |
| Original | 38K | -10.1% | -6.3% |
| +5° Cant | 38K | -8.1% | -0.4% |
| -5° Cant | 38K | -2.8% | 0.5% |
| Endplate | 38K | -8.0% | 3.1% |
| No Flow Guide | 38K | - | - |

A plot of $C_L^{3/2}/C_D$ versus angle of attack for the five model configurations can be seen in Figure 100. A summary of the results is located in Table 16 and the percent change between models can be seen in Table 18. The No Flow Guide Configuration was the reference point for the other configurations. These results will help determine the best configuration for endurance. For a $Re \approx 38K$, the model with the highest endurance

relative to the No Flow Guide Configuration was the Endplate Configuration due to its reduced induced drag.

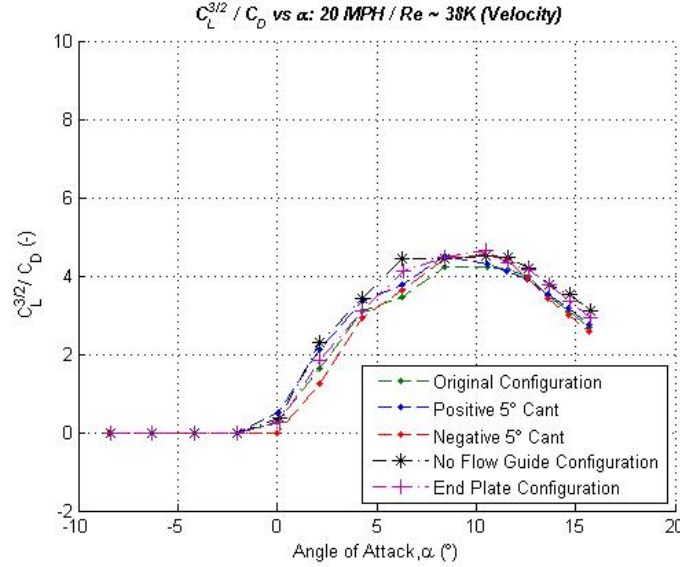


Figure 100: $C_L^{3/2}/C_D$ – Max Endurance vs. Angle of Attack – $Re \sim 38K$ / 20MPH

4.3.1.4 Effective Aspect Ratio

The effective aspect ratio, eAR , has been calculated for all five models at a $Re \approx 38K$. This data can be seen in Table 19. The induced drag coefficient and lift coefficient values were taken at L/D_{max} for all five configurations. The effective aspect ratio is highest for the -5° Cant Configuration at a $Re \approx 38K$.

Table 19: Comparison of Aspect Ratio for the Five Models – $Re \sim 38K$

| Model Configuration | Re (-) | eAR |
|---------------------|--------|------|
| Original | 38K | 1.64 |
| +5° Cant | 38K | 1.57 |
| -5° Cant | 38K | 1.87 |
| Endplate | 38K | 1.78 |
| No Flow Guide | 38K | 1.61 |

4.3.2 $Re \approx 57K$ / 30 MPH

4.3.2.1 Summary

The data results of the five model configurations, which were presented in Section 4.2 at a Reynolds number of 57K (30 mph or 13.41 m/s), are compared to gauge the differences in aerodynamic performance of the models. The models that were included in the test were: the Original Configuration Model, the + 5° Cant Configuration Model, the – 5° Cant Configuration Model, the Endplate Configuration Model, and the No Flow Guide Configuration Model. The No Flow Guide Configuration Model served as the reference to base all the performance parameters.

A summary of aerodynamic performance comparisons between the five model configurations can be seen in Table 19. A discussion of the performance factors: drag, maximum range, maximum endurance, and effective aspect ratio will be discussed in this section with corresponding figures.

Table 20: Summary of the Aerodynamic Performance Comparison of the Five Models – Re ~ 57K

| Model Configuration | Re (-) | S (in ²) | b (in) | Minimum Drag | | | Zero Lift | Slopes | |
|---------------------|--------|----------------------|--------|---------------------|--------------|--------|-------------------------------|--|--|
| | | | | C _{Do} (-) | α (°) | D (lb) | $\alpha_{0 \text{ Lift}}$ (°) | C _{Lα} (/°) | C _{mα} (/°) |
| Original | 57K | 72.58 | 13.81 | 0.0275 | -2.02 | 0.032 | -1.33 | 0.056 | 0.010 |
| +5° Cant | 57K | 72.56 | 13.81 | 0.0277 | -2.01 | 0.033 | -0.99 | 0.054 | 0.011 |
| -5° Cant | 57K | 72.56 | 13.81 | 0.0273 | 0.01 | 0.032 | -0.57 | 0.057 | 0.010 |
| Endplate | 57K | 58.33 | 11.50 | 0.0296 | 0.11 | 0.028 | -1.25 | 0.058 | 0.011 |
| No Flow Guide | 57K | 58.02 | 11.38 | 0.0268 | 0.11 | 0.024 | -1.09 | 0.057 | 0.010 |

| Model Configuration | Re (-) | S (in ²) | b (in) | Maximum Range | | | | | |
|---------------------|--------|----------------------|--------|------------------------|--------------|--------------------|--------------------|--------|--------|
| | | | | L/D _{max} (-) | α (°) | C _L (-) | C _D (-) | L (lb) | D (lb) |
| Original | 57K | 72.58 | 13.81 | 9.4369 | 6.33 | 0.4252 | 0.0451 | 0.502 | 0.053 |
| +5° Cant | 57K | 72.56 | 13.81 | 9.3534 | 6.34 | 0.4503 | 0.0481 | 0.520 | 0.056 |
| -5° Cant | 57K | 72.56 | 13.81 | 9.3586 | 8.44 | 0.5054 | 0.0540 | 0.551 | 0.059 |
| Endplate | 57K | 58.33 | 11.50 | 8.6825 | 6.39 | 0.4453 | 0.0513 | 0.419 | 0.048 |
| No Flow Guide | 57K | 58.02 | 11.38 | 9.0696 | 6.30 | 0.4248 | 0.0468 | 0.389 | 0.043 |

| Model Configuration | Re (-) | S (in ²) | b (in) | Maximum Endurance | | | | | |
|---------------------|--------|----------------------|--------|--|--------------|--------------------|--------------------|--------|--------|
| | | | | C _L ^(3/2) /C _{Dmax} (-) | α (°) | C _L (-) | C _D (-) | L (lb) | D (lb) |
| Original | 57K | 72.58 | 13.81 | 7.0672 | 10.57 | 0.6110 | 0.0676 | 0.701 | 0.078 |
| +5° Cant | 57K | 72.56 | 13.81 | 6.9491 | 10.58 | 0.6395 | 0.0736 | 0.715 | 0.082 |
| -5° Cant | 57K | 72.56 | 13.81 | 6.6534 | 8.44 | 0.5054 | 0.0540 | 0.551 | 0.059 |
| Endplate | 57K | 58.33 | 11.50 | 6.4561 | 10.52 | 0.6051 | 0.0729 | 0.587 | 0.071 |
| No Flow Guide | 57K | 58.02 | 11.38 | 6.3719 | 10.52 | 0.5981 | 0.0726 | 0.549 | 0.067 |

4.3.2.2 Drag

Figure 101 plots the drag polar, C_D vs. C_L, for the five model configurations at a Reynolds number of 57K. The No Flow Guide Configuration has the lowest value of C_{Do} of all the five configurations. Table 21 compares the induced and parasite drag between all the model configurations. It is interesting to note at a Reynolds number of 57K the Endplate configuration had the least amount of induced drag percentage of the total drag. The + 5° Cant Configuration had the highest lift-to-induced drag of all the models.

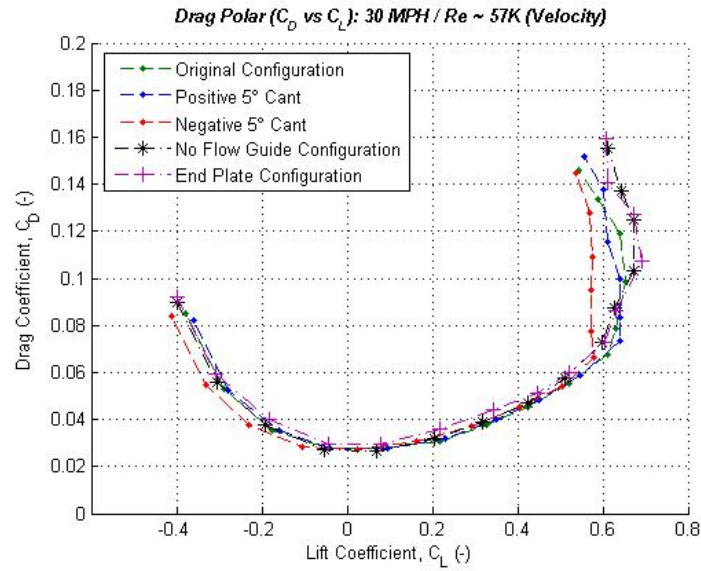


Figure 101: Drag Polar vs. Angle of Attack – Re ~ 57K / 30MPH

Table 21: Comparison of Induced and Parasite Drag of the Five Models – Re ~ 57K

| Model Configuration | Re (-) | L/D _{max} (-) | C _D (-) | C _{Do} (-) | C _{Di} (-) | C _{Di} / C _D (-) | L (lb) | D (lb) | D _{min} (lb) | D _i (lb) | L/D _i (-) |
|---------------------|--------|------------------------|--------------------|---------------------|---------------------|--------------------------------------|--------|--------|-----------------------|---------------------|----------------------|
| Original | 57K | 9.4369 | 0.0451 | 0.0275 | 0.0175 | 38.9% | 0.502 | 0.053 | 0.032 | 0.021 | 23.65 |
| +5° Cant | 57K | 9.3534 | 0.0481 | 0.0277 | 0.0205 | 42.5% | 0.520 | 0.056 | 0.033 | 0.023 | 22.85 |
| -5° Cant | 57K | 9.3586 | 0.0540 | 0.0273 | 0.0267 | 49.5% | 0.551 | 0.059 | 0.032 | 0.027 | 20.60 |
| Endplate | 57K | 8.6825 | 0.0513 | 0.0296 | 0.0217 | 42.3% | 0.419 | 0.048 | 0.028 | 0.020 | 20.85 |
| No Flow Guide | 57K | 9.0696 | 0.0468 | 0.0268 | 0.0200 | 42.7% | 0.389 | 0.043 | 0.024 | 0.019 | 20.57 |

4.3.2.3 Maximum Range and Endurance

A plot of lift-to-drag versus angle of attack for the five model configurations can be seen in Figure 102. A summary of the results is located in Table 20 and the percent change between models can be seen in Table 22. The No Flow Guide Configuration was the reference point for the other configurations. These results will help determine the best configuration for endurance. For a $Re \approx 57K$, the Original Configuration and + 5° Cant Configuration have the highest L/D_{max} values due to decreased induced drag. The +5°

Cant Configuration and the -5° Cant Configuration are shifted to either side of the Original Configuration due to the effective angle of attack of the canted flow guides.

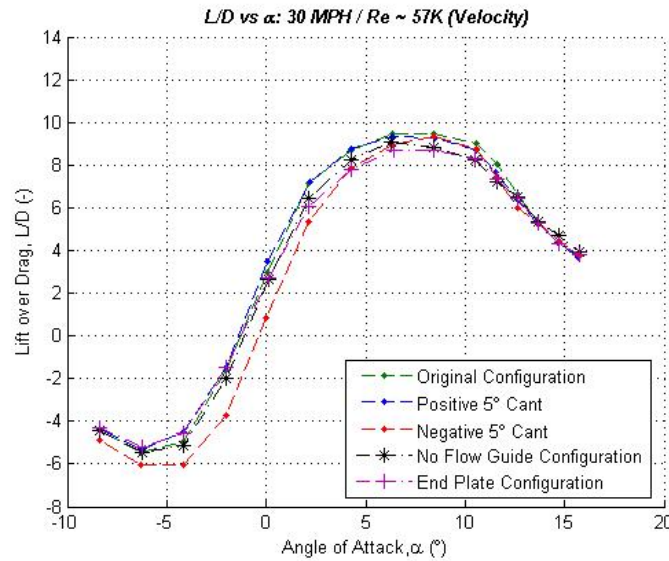


Figure 102: Lift-to-Drag vs. Angle of Attack – Re ~ 57K / 30MPH

Table 22: Comparison of L/D_{\max} and $C_L^{3/2}/C_{D\max}$ of the Five Models – Re ~ 57K

| Model Configuration | Re (-) | % Change from No Flow Guide | |
|---------------------|--------|-----------------------------|-------------------------|
| | | L/D_{\max} | $C_L^{(3/2)}/C_{D\max}$ |
| Original | 57K | 4.1% | 10.9% |
| +5° Cant | 57K | 3.1% | 9.1% |
| -5° Cant | 57K | 3.2% | 4.4% |
| Endplate | 57K | -4.3% | 1.3% |
| No Flow Guide | 57K | - | - |

A plot of $C_L^{3/2}/C_D$ versus angle of attack for the five model configurations can be seen in Figure 103. A summary of the results is located in Table 20 and the percent change between models can be seen in Table 22. The No Flow Guide Configuration was the reference point for the other configurations. These results will help determine the best configuration for endurance. For a $Re \approx 57K$, the model with the highest endurance

relative to the No Flow Guide Configuration was the Original Configuration due to its relatively low value for induced drag.

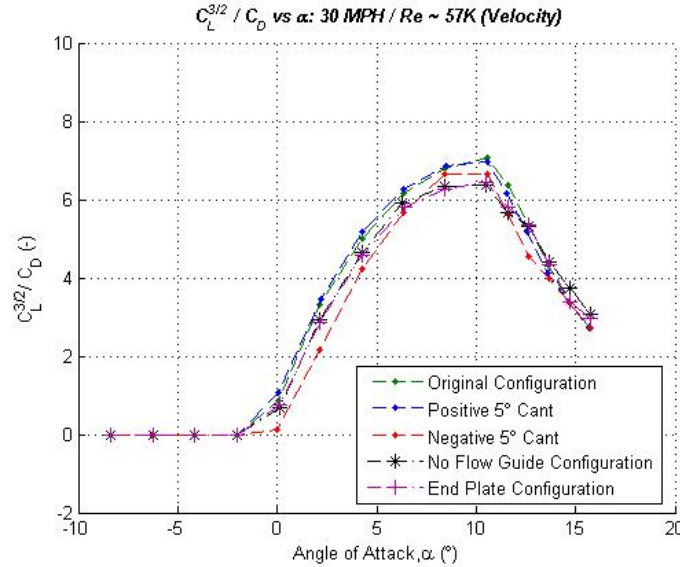


Figure 103: $C_L^{3/2}/C_D$ – Max Endurance vs. Angle of Attack – $Re \sim 57K$ / 30MPH

4.3.2.4 Effective Aspect Ratio

The effective aspect ratio, eAR , has been calculated for all five models at a $Re \approx 57K$. This data can be seen in Table 23. The induced drag coefficient and lift coefficient values were taken at L/D_{max} for all five configurations. The effective aspect ratio is highest for the Original Configuration at a $Re \approx 38K$.

Table 23: Comparison of Aspect Ratio for the Five Models – $Re \sim 57K$

| Model Configuration | Re (-) | eAR |
|---------------------|--------|------|
| Original | 57K | 3.28 |
| +5° Cant | 57K | 3.15 |
| -5° Cant | 57K | 3.04 |
| Endplate | 57K | 2.91 |
| No Flow Guide | 57K | 2.87 |

4.3.3 $Re \approx 78K$ / 40 MPH

4.3.3.1 Summary

The data results of the five model configurations, which were presented in Section 4.2 at a Reynolds number of 78K (40 mph or 17.88 m/s), are compared to gauge the differences in aerodynamic performance of the models. The models that were included in the test were: the Original Configuration Model, the + 5° Cant Configuration Model, the – 5° Cant Configuration Model, the Endplate Configuration Model, and the No Flow Guide Configuration Model. The No Flow Guide Configuration Model served as the reference to base all the performance parameters.

A summary of aerodynamic performance comparisons between the five model configurations can be seen in Table 23. A discussion of the performance factors: drag, maximum range, maximum endurance, and effective aspect ratio will be discussed in this section with corresponding figures.

Table 24: Summary of the Aerodynamic Performance Comparison of the Five Models – Re ~ 78K

| Model Configuration | Re (-) | S (in ²) | b (in) | Minimum Drag | | | Zero Lift | Slopes | |
|---------------------|--------|----------------------|--------|---------------------|--------------|--------|-------------------------------|--|--|
| | | | | C _{D0} (-) | α (°) | D (lb) | $\alpha_{0 \text{ Lift}}$ (°) | C _{Lα} (/°) | C _{mα} (/°) |
| Original | 78K | 72.58 | 13.81 | 0.0251 | 0.03 | 0.053 | -1.50 | 0.054 | 0.011 |
| +5° Cant | 78K | 72.56 | 13.81 | 0.0250 | -2.00 | 0.053 | -1.78 | 0.054 | 0.010 |
| -5° Cant | 78K | 72.56 | 13.81 | 0.0241 | 0.10 | 0.050 | -0.65 | 0.054 | 0.011 |
| Endplate | 78K | 58.33 | 11.50 | 0.0278 | 0.11 | 0.049 | -1.37 | 0.056 | 0.011 |
| No Flow Guide | 78K | 58.02 | 11.38 | 0.0233 | 0.11 | 0.039 | -1.31 | 0.054 | 0.010 |

| Model Configuration | Re (-) | S (in ²) | b (in) | Maximum Range | | | | | |
|---------------------|--------|----------------------|--------|------------------------|--------------|--------------------|--------------------|--------|--------|
| | | | | L/D _{max} (-) | α (°) | C _L (-) | C _D (-) | L (lb) | D (lb) |
| Original | 78K | 72.58 | 13.81 | 10.5512 | 6.32 | 0.4154 | 0.0394 | 0.896 | 0.085 |
| +5° Cant | 78K | 72.56 | 13.81 | 10.3334 | 6.33 | 0.4284 | 0.0415 | 0.927 | 0.090 |
| -5° Cant | 78K | 72.56 | 13.81 | 10.4259 | 8.43 | 0.4643 | 0.0445 | 1.000 | 0.096 |
| Endplate | 78K | 58.33 | 11.50 | 9.2024 | 8.41 | 0.5198 | 0.0565 | 0.901 | 0.098 |
| No Flow Guide | 78K | 58.02 | 11.38 | 9.9634 | 6.29 | 0.4052 | 0.0407 | 0.688 | 0.069 |

| Model Configuration | Re (-) | S (in ²) | b (in) | Maximum Endurance | | | | | |
|---------------------|--------|----------------------|--------|--|--------------|--------------------|--------------------|--------|--------|
| | | | | C _L ^(3/2) /C _{Dmax} (-) | α (°) | C _L (-) | C _D (-) | L (lb) | D (lb) |
| Original | 78K | 72.58 | 13.81 | 7.7068 | 10.56 | 0.5969 | 0.0598 | 1.267 | 0.127 |
| +5° Cant | 78K | 72.56 | 13.81 | 7.3994 | 10.56 | 0.5971 | 0.0624 | 1.287 | 0.134 |
| -5° Cant | 78K | 72.56 | 13.81 | 7.2532 | 10.55 | 0.5486 | 0.0560 | 1.167 | 0.119 |
| Endplate | 78K | 58.33 | 11.50 | 6.9288 | 10.52 | 0.6064 | 0.0682 | 1.062 | 0.119 |
| No Flow Guide | 78K | 58.02 | 11.38 | 7.1055 | 10.52 | 0.5962 | 0.0648 | 1.009 | 0.110 |

4.3.3.2 Drag

Figure 104 plots the drag polar, C_D vs. C_L, for the five model configurations at a Reynolds number of 78K. The No Flow Guide Configuration has the lowest value of C_{D0} of all the five configurations. Table 25 compares the induced and parasite drag between all the model configurations. It is interesting to note at a Reynolds number of 78K the Endplate configuration had the most amount of induced drag percentage of the total drag. The Original Configuration had the highest lift-to-induced drag of all the models.

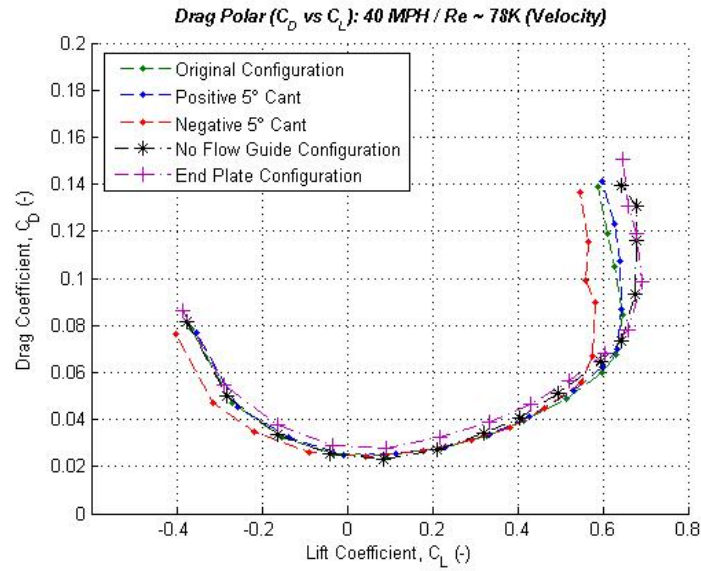


Figure 104: Drag Polar vs. Angle of Attack – Re ~ 78K / 40MPH

Table 25: Comparison of Induced and Parasite Drag of the Five Models – Re ~ 78K

| Model Configuration | Re (-) | L/D _{max} (-) | C _D (-) | C _{Do} (-) | C _{Di} (-) | C _{Di} /C _D (-) | L (lb) | D (lb) | D _{min} (lb) | D _i (lb) | L/D _i (-) |
|---------------------|--------|------------------------|--------------------|---------------------|---------------------|-------------------------------------|--------|--------|-----------------------|---------------------|----------------------|
| Original | 78K | 10.5512 | 0.0394 | 0.0251 | 0.0143 | 36.2% | 0.896 | 0.085 | 0.053 | 0.032 | 27.971 |
| +5° Cant | 78K | 10.3334 | 0.0415 | 0.0250 | 0.0164 | 39.6% | 0.927 | 0.090 | 0.053 | 0.037 | 25.351 |
| -5° Cant | 78K | 10.4259 | 0.0445 | 0.0241 | 0.0205 | 45.9% | 1.000 | 0.096 | 0.050 | 0.046 | 21.594 |
| Endplate | 78K | 9.2024 | 0.0565 | 0.0278 | 0.0286 | 50.7% | 0.901 | 0.098 | 0.049 | 0.049 | 18.306 |
| No Flow Guide | 78K | 9.9634 | 0.0407 | 0.0233 | 0.0174 | 42.8% | 0.688 | 0.069 | 0.039 | 0.030 | 23.146 |

4.3.3.3 Maximum Range and Endurance

A plot of lift-to-drag versus angle of attack for the five model configurations can be seen in Figure 105. A summary of the results is located in Table 24 and the percent change between models can be seen in Table 26. The No Flow Guide Configuration was the reference point for the other configurations. These results will help determine the best configuration for endurance. For a $Re \approx 78K$, the Original Configuration has the highest L/D_{max} value due to decreased induced drag. The +5° Cant Configuration and the -5°

Cant Configuration are shifted to either side of the Original Configuration due to the effective angle of attack of the canted flow guides.

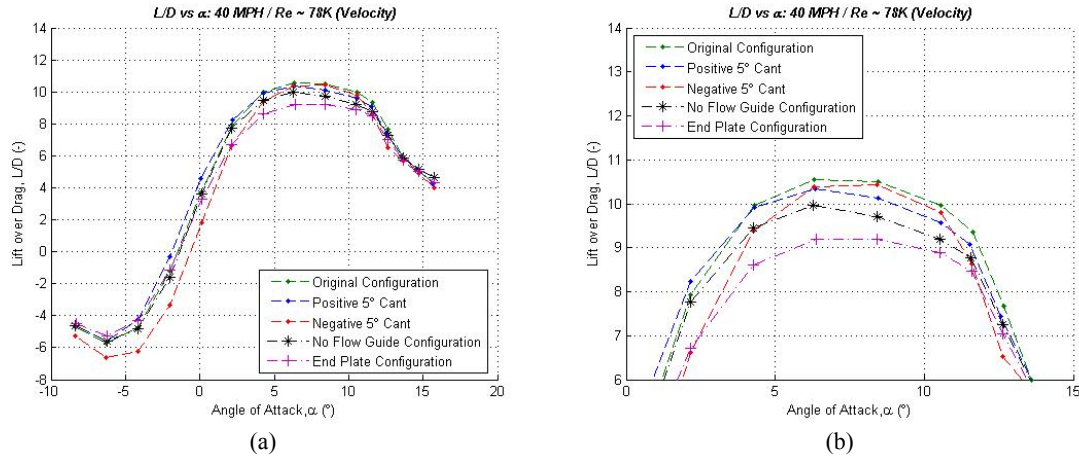


Figure 105: Lift-to-Drag vs. Angle of Attack – Re ~ 78K / 40MPH
(a) Lift-to-Drag vs. Alpha, (b) Lift-to-Drag vs. Alpha – Magnified Section

Table 26: Comparison of L/D_{\max} and $C_L^{3/2}/C_{D\max}$ of the Five Models – Re ~ 78K

| Model Configuration | Re (-) | % Change from No Flow Guide | |
|---------------------|--------|-----------------------------|-------------------------|
| | | L/D_{\max} | $C_L^{(3/2)}/C_{D\max}$ |
| Original | 78K | 5.9% | 8.5% |
| +5° Cant | 78K | 3.7% | 4.1% |
| -5° Cant | 78K | 4.6% | 2.1% |
| Endplate | 78K | -7.6% | -2.5% |
| No Flow Guide | 78K | - | - |

A plot of $C_L^{3/2}/C_D$ versus angle of attack for the five model configurations can be seen in Figure 106. A summary of the results is located in Table 24 and the percent change between models can be seen in Table 26. The No Flow Guide Configuration was the reference point for the other configurations. These results will help determine the best configuration for endurance. For a $Re \approx 78K$, the model with the highest endurance relative to the No Flow Guide Configuration was the Original Configuration due to its relatively low value for induced drag.

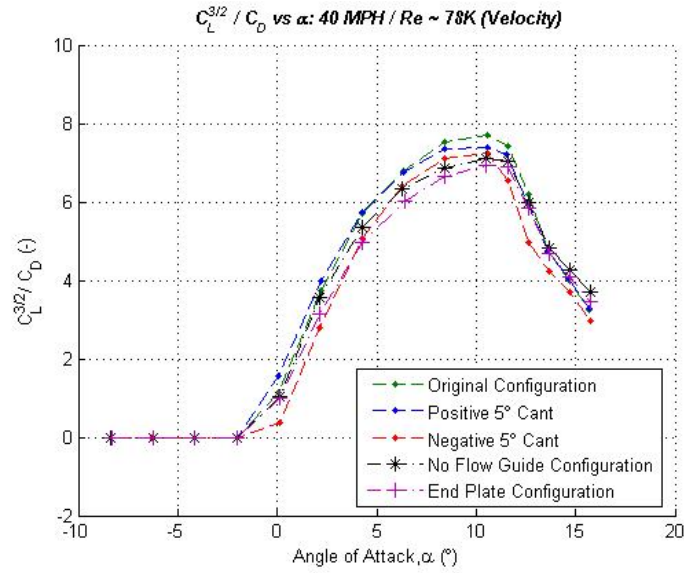


Figure 106: $C_L^{3/2}/C_D$ – Max Endurance vs. Angle of Attack – $Re \sim 78K$ / 40MPH

4.3.3.4 Effective Aspect Ratio

The effective aspect ratio, eAR , has been calculated for all five models at a $Re \approx 78K$. This data can be seen in Table 27. The induced drag coefficient and lift coefficient values were taken at L/D_{max} for all five configurations. The effective aspect ratio is highest for the Original Configuration at a $Re \approx 78K$.

Table 27: Comparison of Aspect Ratio for the Five Models – $Re \sim 78K$

| Model Configuration | Re (-) | eAR |
|---------------------|--------|------|
| Original | 78K | 3.85 |
| +5° Cant | 78K | 3.55 |
| -5° Cant | 78K | 3.36 |
| Endplate | 78K | 3.00 |
| No Flow Guide | 78K | 3.01 |

4.3.4 $Re \approx 120K$ / 60 MPH

4.3.4.1 Summary

The data results of the five model configurations, which were presented in Section 4.2 at a Reynolds number of 120K (60 mph or 26.82 m/s), are compared to gauge the differences in aerodynamic performance of the models. The models that were included in the test were: the Original Configuration Model, the + 5° Cant Configuration Model, the – 5° Cant Configuration Model, the Endplate Configuration Model, and the No Flow Guide Configuration Model. The No Flow Guide Configuration Model served as the reference to base all the performance parameters.

A summary of aerodynamic performance comparisons between the five model configurations can be seen in Table 27. A discussion of the performance factors: drag, maximum range, maximum endurance, and effective aspect ratio will be discussed in this section with corresponding figures.

Table 28: Summary of the Aerodynamic Performance Comparison of the Five Models – Re ~ 120K

| Model Configuration | Re (-) | S (in ²) | b (in) | Minimum Drag | | | Zero Lift | Slopes | |
|---------------------|--------|----------------------|--------|---------------------|--------------|--------|-------------------------------|--|--|
| | | | | C _{D0} (-) | α (°) | D (lb) | $\alpha_{0 \text{ Lift}}$ (°) | C _{Lα} (/°) | C _{mα} (/°) |
| Original | 120K | 72.58 | 13.81 | 0.0204 | 0.12 | 0.098 | -1.54 | 0.053 | 0.011 |
| +5° Cant | 120K | 72.56 | 13.81 | 0.0218 | 0.13 | 0.102 | -1.92 | 0.053 | 0.011 |
| -5° Cant | 120K | 72.56 | 13.81 | 0.0201 | 0.11 | 0.095 | -0.88 | 0.054 | 0.011 |
| Endplate | 120K | 58.33 | 11.50 | 0.0251 | 0.11 | 0.099 | -1.40 | 0.055 | 0.013 |
| No Flow Guide | 120K | 58.02 | 11.38 | 0.0195 | 0.11 | 0.077 | -1.58 | 0.052 | 0.012 |

| Model Configuration | Re (-) | S (in ²) | b (in) | Maximum Range | | | | | |
|---------------------|--------|----------------------|--------|------------------------|--------------|--------------------|--------------------|--------|--------|
| | | | | L/D _{max} (-) | α (°) | C _L (-) | C _D (-) | L (lb) | D (lb) |
| Original | 120K | 72.58 | 13.81 | 11.8368 | 6.41 | 0.4240 | 0.0358 | 2.022 | 0.171 |
| +5° Cant | 120K | 72.56 | 13.81 | 11.7204 | 6.33 | 0.4387 | 0.0374 | 2.099 | 0.179 |
| -5° Cant | 120K | 72.56 | 13.81 | 11.9833 | 6.40 | 0.3945 | 0.0329 | 1.883 | 0.157 |
| Endplate | 120K | 58.33 | 11.50 | 10.3918 | 8.41 | 0.5281 | 0.0508 | 2.075 | 0.200 |
| No Flow Guide | 120K | 58.02 | 11.38 | 11.6871 | 6.29 | 0.4145 | 0.0355 | 1.648 | 0.141 |

| Model Configuration | Re (-) | S (in ²) | b (in) | Maximum Endurance | | | | | |
|---------------------|--------|----------------------|--------|--|--------------|--------------------|--------------------|--------|--------|
| | | | | C _L ^(3/2) /C _{Dmax} (-) | α (°) | C _L (-) | C _D (-) | L (lb) | D (lb) |
| Original | 120K | 72.58 | 13.81 | 8.5435 | 10.56 | 0.6003 | 0.0544 | 2.884 | 0.262 |
| +5° Cant | 120K | 72.56 | 13.81 | 8.3031 | 8.45 | 0.5277 | 0.0462 | 2.552 | 0.223 |
| -5° Cant | 120K | 72.56 | 13.81 | 8.3134 | 8.43 | 0.4842 | 0.0405 | 2.320 | 0.194 |
| Endplate | 120K | 58.33 | 11.50 | 7.6841 | 10.53 | 0.6157 | 0.0629 | 2.424 | 0.247 |
| No Flow Guide | 120K | 58.02 | 11.38 | 8.1126 | 10.52 | 0.6086 | 0.0585 | 2.392 | 0.230 |

4.3.4.2 Drag

Figure 107 plots the drag polar, C_D vs. C_L, for the five model configurations at a Reynolds number of 120K. The No Flow Guide Configuration has the lowest value of C_{D0} of all the five configurations. Table 29 compares the induced and parasite drag between all the model configurations. It is interesting to note at a Reynolds number of 120K the Endplate configuration had the most amount of induced drag percentage of the total drag. The – 5°Cant Configuration had the highest lift-to-induced drag of all the models.

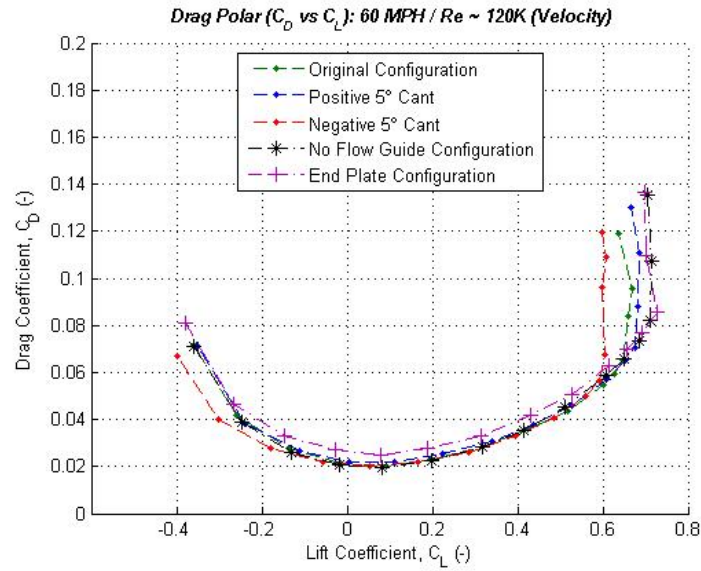


Figure 107: Drag Polar vs. Angle of Attack – Re ~ 120K / 60MPH

Table 29: Comparison of Induced and Parasite Drag of the Five Models – Re ~ 120K

| Model Configuration | Re (-) | L/D _{max} (-) | C _D (-) | C _{Do} (-) | C _{Di} (-) | C _{Di} /C _D (-) | L (lb) | D (lb) | D _{min} (lb) | D _i (lb) | L/D _i (-) |
|---------------------|--------|------------------------|--------------------|---------------------|---------------------|-------------------------------------|--------|--------|-----------------------|---------------------|----------------------|
| Original | 120K | 11.8368 | 0.0358 | 0.0204 | 0.0154 | 43.0% | 2.022 | 0.171 | 0.098 | 0.073 | 27.80 |
| +5° Cant | 120K | 11.7204 | 0.0374 | 0.0218 | 0.0156 | 41.7% | 2.099 | 0.179 | 0.102 | 0.077 | 27.36 |
| -5° Cant | 120K | 11.9833 | 0.0329 | 0.0201 | 0.0128 | 38.9% | 1.883 | 0.157 | 0.095 | 0.062 | 30.38 |
| Endplate | 120K | 10.3918 | 0.0508 | 0.0251 | 0.0257 | 50.6% | 2.075 | 0.200 | 0.099 | 0.100 | 20.65 |
| No Flow Guide | 120K | 11.6871 | 0.0355 | 0.0195 | 0.0159 | 44.9% | 1.648 | 0.141 | 0.077 | 0.064 | 25.64 |

4.3.4.3 Maximum Range and Endurance

A plot of lift-to-drag versus angle of attack for the five model configurations can be seen in Figure 108. A summary of the results is located in Table 28 and the percent change between models can be seen in Table 30. The No Flow Guide Configuration was the reference point for the other configurations. These results will help determine the best configuration for endurance. For a $Re \approx 120K$, the - 5° Cant Configuration has the highest L/D_{max} value due to decreased induced drag. The +5° Cant Configuration and the

-5° Cant Configuration are shifted to either side of the Original Configuration due to the effective angle of attack of the canted flow guides.

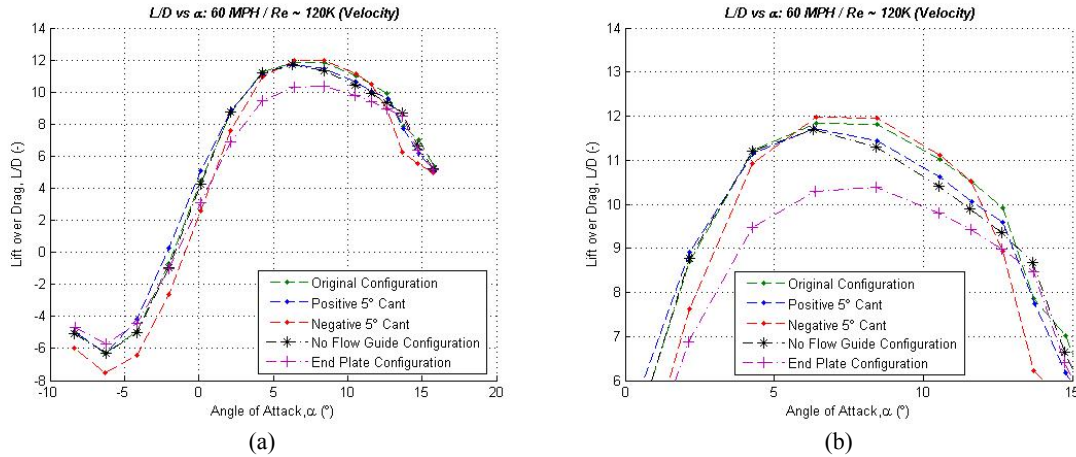


Figure 108: Lift-to-Drag vs. Angle of Attack – Re ~ 120K / 60MPH
(a) Lift-to-Drag vs. Alpha, (b) Lift-to-Drag vs. Alpha – Magnified Section

Table 30: Comparison of L/D_{\max} and $C_L^{3/2}/C_{D\max}$ of the Five Models – Re ~ 120K

| Model Configuration | Re (-) | % Change from No Flow Guide | |
|---------------------|--------|-----------------------------|-------------------------|
| | | L/D_{\max} | $C_L^{(3/2)}/C_{D\max}$ |
| Original | 120K | 1.3% | 5.3% |
| +5° Cant | 120K | 0.3% | 2.3% |
| -5° Cant | 120K | 2.5% | 2.5% |
| Endplate | 120K | -11.1% | -5.3% |
| No Flow Guide | 120K | - | - |

A plot of $C_L^{3/2}/C_D$ versus angle of attack for the five model configurations can be seen in Figure 109. A summary of the results is located in Table 28 and the percent change between models can be seen in Table 30. The No Flow Guide Configuration was the reference point for the other configurations. These results will help determine the best configuration for endurance. For a $Re \approx 120K$, the model with the highest endurance relative to the No Flow Guide Configuration was the Original Configuration due to its relatively low value for induced drag.

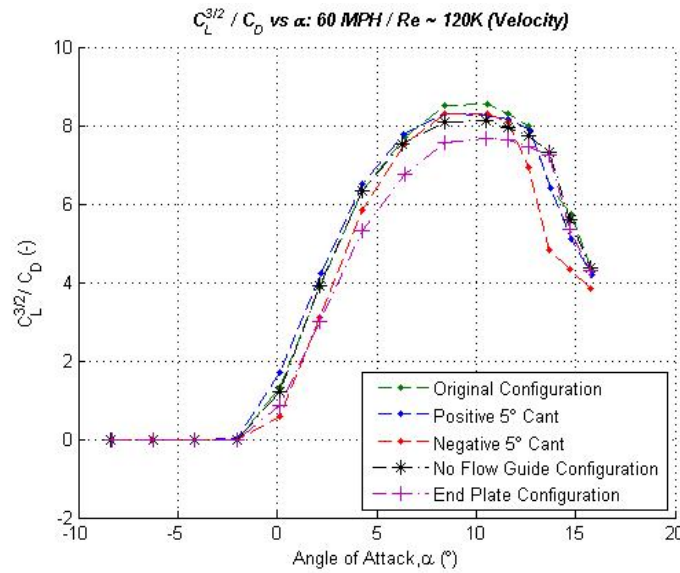


Figure 109: $C_L^{3/2}/C_D$ – Max Endurance vs. Angle of Attack – $Re \sim 120K$ / 60MPH

4.3.4.4 Effective Aspect Ratio

The effective aspect ratio, eAR , has been calculated for all five models at a $Re \approx 120K$. This data can be seen in Table 31. The induced drag coefficient and lift coefficient values were taken at L/D_{max} for all five configurations. The effective aspect ratio is highest for the $+5^\circ$ Cant Configuration at a $Re \approx 120K$.

Table 31: Comparison of Aspect Ratio for the Five Models – $Re \sim 120K$

| Model Configuration | Re (-) | eAR |
|---------------------|--------|------|
| Original | 120K | 3.71 |
| +5° Cant | 120K | 3.92 |
| -5° Cant | 120K | 3.87 |
| Endplate | 120K | 3.45 |
| No Flow Guide | 120K | 3.43 |

4.3.5 Trends

The overall trend of results of the five model configurations, which were presented in this section at Reynolds numbers of 38K, 57K, 78K, and 120K, are presented in Table 32. The models that were included in the test were: the Original Configuration Model, the + 5° Cant Configuration Model, the – 5° Cant Configuration Model, the Endplate Configuration Model, and the No Flow Guide Configuration Model. The No Flow Guide Configuration Model served as the reference to base all the performance parameters. The 24” Houck Configuration Model with and without flow guides was also included for comparison.

Table 32: Aerodynamic Performance Comparison for the Models – Re ~ 38K, 57K, 78K, & 120K

| Model Configuration | Re (-) | % Change from No Flow Guide (per Re #) | | At L/D _{max} | | |
|---------------------|---------|--|--|--------------------------------------|----------------------|------|
| | | L/D _{max} (-) | C _L ^(3/2) /C _{Dmax} (-) | C _{Di} / C _D (-) | L/D _i (-) | eAR |
| Original | 38,000 | -10.1% | -6.3% | 56.0% | 10.92 | 1.64 |
| Original | 57,000 | 3.1% | 9.1% | 38.9% | 23.65 | 3.28 |
| Original | 78,000 | 5.9% | 8.5% | 36.2% | 27.97 | 3.85 |
| Original | 120,000 | 1.3% | 5.3% | 43.0% | 27.80 | 3.71 |
| +5° Cant | 38,000 | -8.1% | -0.4% | 64.6% | 10.31 | 1.57 |
| +5° Cant | 57,000 | 3.1% | 9.1% | 42.5% | 22.85 | 3.15 |
| +5° Cant | 78,000 | 3.7% | 4.1% | 39.6% | 25.35 | 3.55 |
| +5° Cant | 120,000 | 0.3% | 2.3% | 41.7% | 27.36 | 3.92 |
| -5° Cant | 38,000 | -2.8% | 0.5% | 49.7% | 13.64 | 1.87 |
| -5° Cant | 57,000 | 3.2% | 4.4% | 49.5% | 20.60 | 3.04 |
| -5° Cant | 78,000 | 4.6% | 2.1% | 45.9% | 21.59 | 3.36 |
| -5° Cant | 120,000 | 2.5% | 2.5% | 38.9% | 30.38 | 3.87 |
| Endplate | 38,000 | -8.0% | 3.1% | 47.7% | 13.26 | 1.78 |
| Endplate | 57,000 | -4.3% | 1.3% | 42.3% | 20.85 | 2.91 |
| Endplate | 78,000 | -7.6% | -2.5% | 50.7% | 18.31 | 3.00 |
| Endplate | 120,000 | -11.1% | -5.3% | 50.6% | 20.65 | 3.45 |
| No Flow Guide | 38,000 | - | - | 56.0% | 12.11 | 1.61 |
| No Flow Guide | 57,000 | - | - | 42.7% | 20.57 | 2.87 |
| No Flow Guide | 78,000 | - | - | 42.8% | 23.15 | 3.01 |
| No Flow Guide | 120,000 | - | - | 44.9% | 25.64 | 3.43 |
| Original 24" Houck | 80,000 | -2.50% | -12.80% | 36.10% | 17.93 | 1.64 |
| Original 24" Houck | 125,000 | -0.30% | -3.40% | 41.90% | 17.63 | 1.65 |
| NOFG Houck | 80,000 | - | - | 48.90% | 13.63 | 1.68 |
| NOFG Houck | 125,000 | - | - | 41.20% | 17.96 | 1.74 |

The first aerodynamic performance parameter to be discussed is maximum lift-to-drag, L/D_{\max} . This parameter is one of the aerodynamic performance parameters that is used to measure aircraft efficiency (maximum range). The percent change of L/D_{\max} (percent change L/D_{\max}) of all five models for all the tested Reynolds numbers is located in Figure 110.

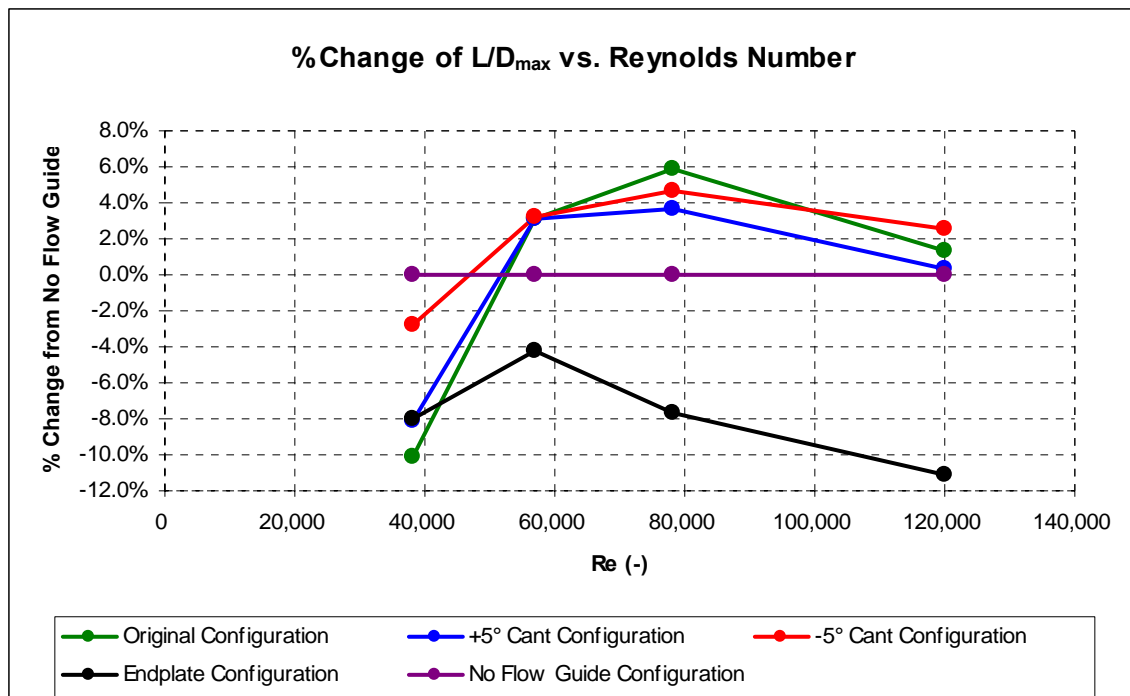


Figure 110: % Change of L/D_{\max} vs. Reynolds Number – Re ~ 38K, 57K, 78K, & 120K

For all Reynolds $\geq 57K$, the Flow Guide Configurations exceed the percent change of L/D_{\max} as compared to the No Flow Guide Configuration. The trend of the percent change L/D_{\max} values of the flow guide configurations compared to the No Flow Guide Configuration is to increase the maximum range over the range of Re $\approx 57K$ to 120K. This performance trend is consistent with the results associated with the 24" Houck Configuration (Table 32). The 24" Houck Configuration had percent change

L/D_{\max} performance trend was increasing over its associated range of $Re \approx 80K$ to $125K$. However, the values of percent change L/D_{\max} were less than the associated No Flow Guide Configuration. The reasons for the increased percent change L/D_{\max} values for the five models, compared to the 24" Houck Configuration, are due to: the model body being less prominent, the trailing edges of the wings were cleaned up, and the balance holder on the model was more streamlined.

The second aerodynamic performance parameter to be discussed is maximum $C_L^{3/2}/C_D$. This parameter is one of the aerodynamic performance parameters that is used to measure aircraft efficiency (maximum endurance). The percent change of $C_L^{3/2}/C_{D\max}$ (percent change $C_L^{3/2}/C_{D\max}$) of all five models for all the tested Reynolds numbers is located in Figure 111. The percent change $C_L^{3/2}/C_{D\max}$ values are located in Table 32.

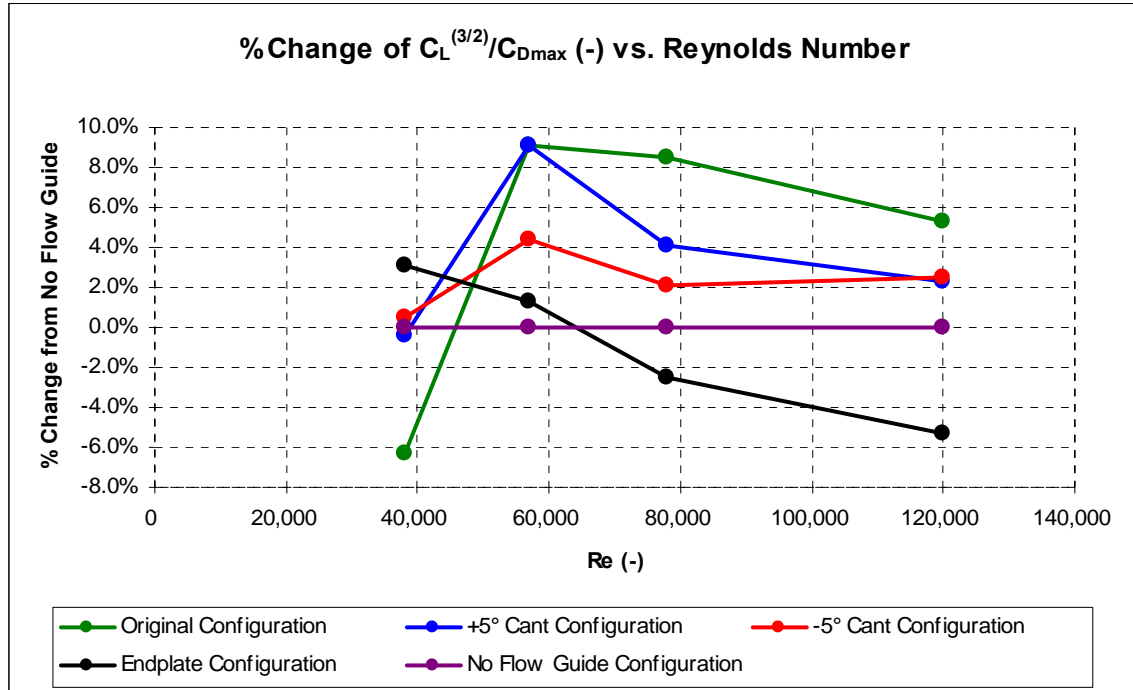


Figure 111: % Change of $C_L^{3/2}/C_{D\max}$ vs. Reynolds Number – $Re \sim 38K, 57K, 78K, \& 120K$

For all Reynolds $\geq 57K$, the Flow Guide Configurations exceed the percent change of $C_L^{3/2}/C_{Dmax}$ as compared to the No Flow Guide Configuration. The trend of the percent change $C_L^{3/2}/C_{Dmax}$ values of the flow guide configurations compared to the No Flow Guide Configuration is to increase the maximum range over the range of $Re \approx 57K$ to $120K$. It is especially noteworthy that the Original Configuration had the best values for the percent change $C_L^{3/2}/C_{Dmax}$ over the range. This performance trend is consistent with the results associated with the 24" Houck Configuration (Table 32). The 24" Houck Configuration had percent change $C_L^{3/2}/C_{Dmax}$ performance trend was increasing over its associated range of $Re \approx 80K$ to $125K$. However, the values of percent change $C_L^{3/2}/C_{Dmax}$ were less than the associated No Flow Guide Configuration. Again, the reasons for the increased percent change $C_L^{3/2}/C_{Dmax}$ values for the five models, compared to the 24" Houck Configuration, are due to: the model body being less prominent, the trailing edges of the wings were cleaned up, and the balance holder on the model was more streamlined.

The average induced drag to total drag (C_{Di}/C_D) at L/D_{max} for the five models tested over the entire range of Reynolds numbers is 45.5%. For each individual model the C_{Di}/C_D is: 43.5% (Original Configuration), 47.1% (+5° Cant Configuration), 46.0% (-5° Cant Configuration), 47.8% (Endplate Configuration), and 46.6% (No Flow Guide Configuration). The percent of C_{Di}/C_D (% C_{Di}/C_D) of all five models for all the tested Reynolds numbers is located in Figure 112. The % C_{Di}/C_D values are located in Table 32.

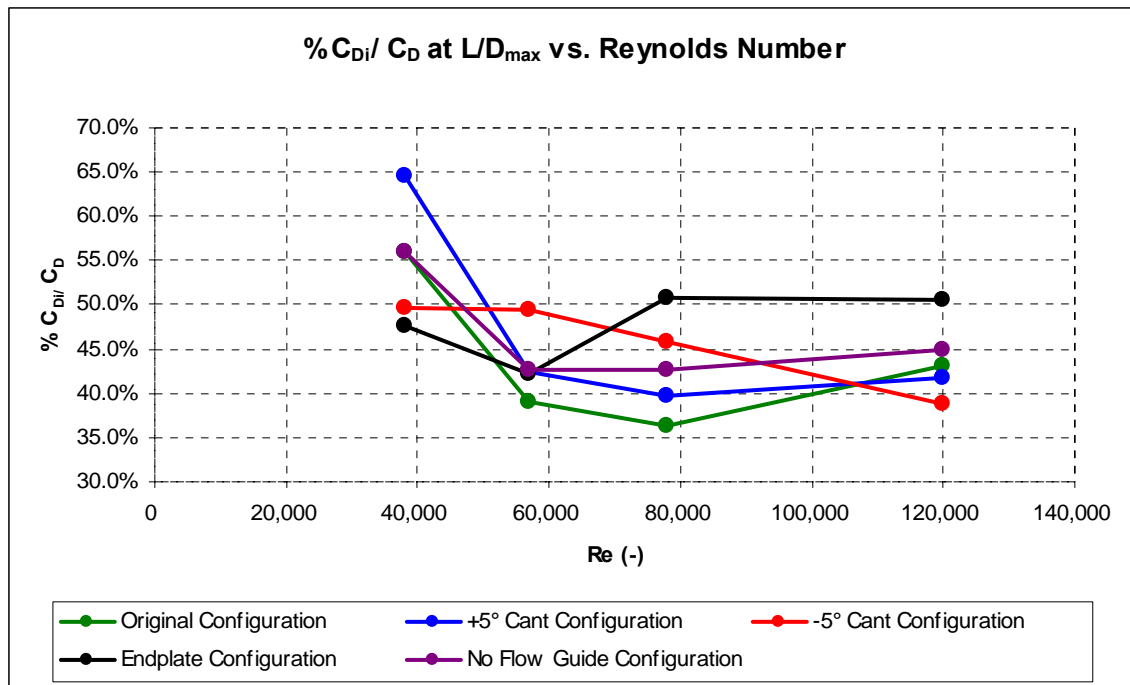


Figure 112: % C_{Di}/C_D vs. Reynolds Number – Re ~ 38K, 57K, 78K, & 120K

Over the range of Re \approx 38K to 120K, the overall trend of the % C_{Di}/C_D values is for the Original Configuration, the +5° Cant Configurations, and eventually the -5° Cant Configuration to reduce the effect of induced drag. This trend is inconsistent with the 24” Houck results. As seen in Table 32, the 24” Houck Configuration increased its induced drag over the range of Re \approx 80K to 125K. The reasons for the decreased % C_{Di}/C_D values for the five models, compared to the 24” Houck Configuration, are due to: the model body being less prominent, the trailing edges of the wings were cleaned up, and the balance holder on the model was more streamlined.

The last aerodynamic performance parameter to be discussed is the span efficiency factor, e . The span efficiency factor is calculated from the effective aspect

ratio, eAR , divided by the aspect ratio, AR (Equation 20). The AR for a monoplane is given in equation 21 and the AR for a biplane is given in equation 22.

$$e = \frac{eAR}{AR} \quad (20)$$

$$AR = \frac{b^2}{S} \quad (21)$$

$$AR = \frac{2 \cdot b^2}{S} \quad (22)$$

where b is the span (in) and S is the planform area of the wing (in^2).

Table 33 lists the span efficiency factor for the five models and the 24" Houck configurations at each Reynolds number.

Table 33: Span Efficiency Comparison for the Models – Re ~ 38K, 57K, 78K, & 120K

| Model Configuration | Re (-) | S (in^2) | b (in) | eAR | Monoplane AR | Monoplane e | Biplane AR | Biplane e |
|---------------------|---------|---------------------|--------|------|--------------|-------------|------------|-----------|
| Original | 38,000 | 72.58 | 13.81 | 1.64 | 2.63 | 0.62 | 5.25 | 0.31 |
| Original | 57,000 | 72.58 | 13.81 | 3.28 | 2.63 | 1.25 | 5.25 | 0.62 |
| Original | 78,000 | 72.58 | 13.81 | 3.85 | 2.63 | 1.47 | 5.25 | 0.73 |
| Original | 120,000 | 72.58 | 13.81 | 3.71 | 2.63 | 1.41 | 5.25 | 0.71 |
| +5° Cant | 38,000 | 72.56 | 13.81 | 1.57 | 2.63 | 0.60 | 5.25 | 0.30 |
| +5° Cant | 57,000 | 72.56 | 13.81 | 3.15 | 2.63 | 1.20 | 5.25 | 0.60 |
| +5° Cant | 78,000 | 72.56 | 13.81 | 3.55 | 2.63 | 1.35 | 5.25 | 0.68 |
| +5° Cant | 120,000 | 72.56 | 13.81 | 3.92 | 2.63 | 1.49 | 5.25 | 0.75 |
| -5° Cant | 38,000 | 72.56 | 13.81 | 1.87 | 2.63 | 0.71 | 5.25 | 0.36 |
| -5° Cant | 57,000 | 72.56 | 13.81 | 3.04 | 2.63 | 1.16 | 5.25 | 0.58 |
| -5° Cant | 78,000 | 72.56 | 13.81 | 3.36 | 2.63 | 1.28 | 5.25 | 0.64 |
| -5° Cant | 120,000 | 72.56 | 13.81 | 3.87 | 2.63 | 1.47 | 5.25 | 0.74 |
| Endplate | 38,000 | 58.33 | 11.50 | 1.78 | 2.27 | 0.79 | 4.53 | 0.39 |
| Endplate | 57,000 | 58.33 | 11.50 | 2.91 | 2.27 | 1.28 | 4.53 | 0.64 |
| Endplate | 78,000 | 58.33 | 11.50 | 3.00 | 2.27 | 1.32 | 4.53 | 0.66 |
| Endplate | 120,000 | 58.33 | 11.50 | 3.45 | 2.27 | 1.52 | 4.53 | 0.76 |
| No Flow Guide | 38,000 | 58.02 | 11.38 | 1.61 | 2.23 | 0.72 | 4.46 | 0.36 |
| No Flow Guide | 57,000 | 58.02 | 11.38 | 2.87 | 2.23 | 1.29 | 4.46 | 0.64 |
| No Flow Guide | 78,000 | 58.02 | 11.38 | 3.01 | 2.23 | 1.35 | 4.46 | 0.67 |
| No Flow Guide | 120,000 | 58.02 | 11.38 | 3.43 | 2.23 | 1.54 | 4.46 | 0.77 |
| Original 24" Houck | 80,000 | 307.00 | 23.58 | 1.64 | 1.81 | 0.90 | 3.62 | 0.45 |
| Original 24" Houck | 125,000 | 307.00 | 23.58 | 1.65 | 1.81 | 0.91 | 3.62 | 0.46 |
| NOFG Houck | 80,000 | 254.00 | 20.33 | 1.68 | 1.63 | 1.03 | 3.25 | 0.52 |
| NOFG Houck | 125,000 | 254.00 | 20.33 | 1.74 | 1.63 | 1.07 | 3.25 | 0.54 |

For a $Re = 38K$, the span efficiency factor is less than one for the monoplane span efficiency factor (all models except for No Flow Guide Houck). However, for all the biplane models, span efficiency factors all the values are less than one. Since the elliptical lift distribution has the least amount of induced drag and therefore an $e = 1$, there cannot be a value that is greater than one. It is interesting to note that e is increasing for all five models as the Reynolds number increases. The e is best, as compared to the five models, at all Reynolds for the No Flow Guide Configuration.

4.4 Neutral Longitudinally Stable $C_{m\alpha}$

4.5.1 Calculation

In order to calculate the neutral longitudinally stable $C_{m\alpha}$, the reference location for the aircraft's center of gravity (x-axis) was varied from the reference measured $X_{cg} = 2.1625"$ ($X_{cmb} = 1.0025"$) to a new measured $X_{cg} = 1.4"$ ($X_{cmb} = 1.765"$). Using the *MATLAB* code and method outlined in Section 3.5.1, the pitching moment coefficient, C_m , was determined.

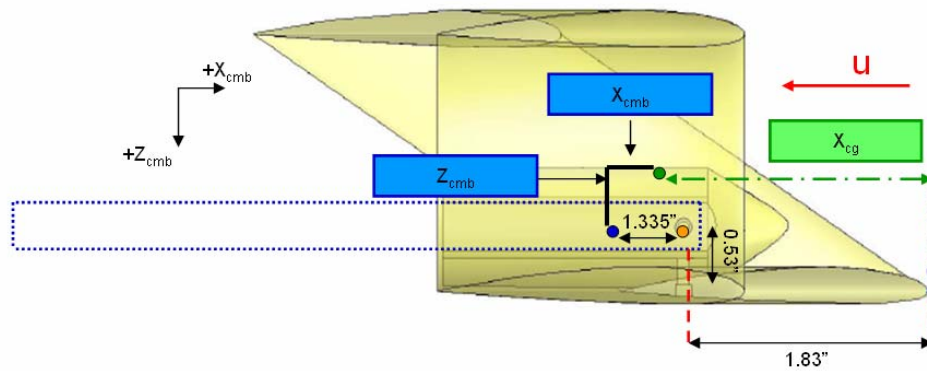


Figure 113: Variation of Aircraft Center of Gravity and Balance Moment Center

The final step to determine $C_{m\alpha}$, was to calculate the slope of the C_m vs. α data over the linear region ($\alpha = -8^\circ$ to 8°).

4.5.2 Results

The results of the $C_{m\alpha}$ calculation described in Section 4.5.1 for the five models at a $Re \approx 120K$ are located in Table 34. The neutral longitudinally stable $C_{m\alpha}$ is located where $C_{m\alpha} = 0$. For the five models it is approximately located at an $X_{cmb} = 1.5750''$ ($X_{cg} = 1.59''$). The range for X_{cg} was chosen so that the region would encompass $C_{m\alpha}$ slopes that are both positive and negative to bound the neutral longitudinal stability $C_{m\alpha}$. Figure 114 shows the graphed C_m curves with their respective linear fits to determine $C_{m\alpha}$ for the Original Configuration Model at a $Re \approx 120K$. The result of $X_{cg} = 1.59''$ suggests that the lower wing produces more lift than the upper wing. Therefore the location of the aircraft's aerodynamic center at the average of the quarter chord of the upper and lower wing produces an aircraft that is longitudinally unstable. Any reference X_{cg} that is less than $1.59''$ (from model nose) will produce a longitudinally stable aircraft.

Table 34: Varying $C_{m\alpha}$ for the Models – $Re \sim 120K$

| Re $\approx 120K$ | $C_{m\alpha}$ (-) | | | | |
|-------------------------------------|-------------------------------------|-------------------------|-------------------------|------------------------|--------------------|
| X_{cmb} (in) | Original Config | + 5° Cant Config | - 5° Cant Config | Endplate Config | NOFG Config |
| 1.0025 | 0.0114 | 0.0113 | 0.0112 | 0.0125 | 0.0115 |
| 1.5750 | 0.0000 | -0.0001 | -0.0003 | 0.0008 | 0.0003 |
| 1.7650 | -0.0038 | -0.0039 | -0.0042 | -0.0031 | -0.0035 |

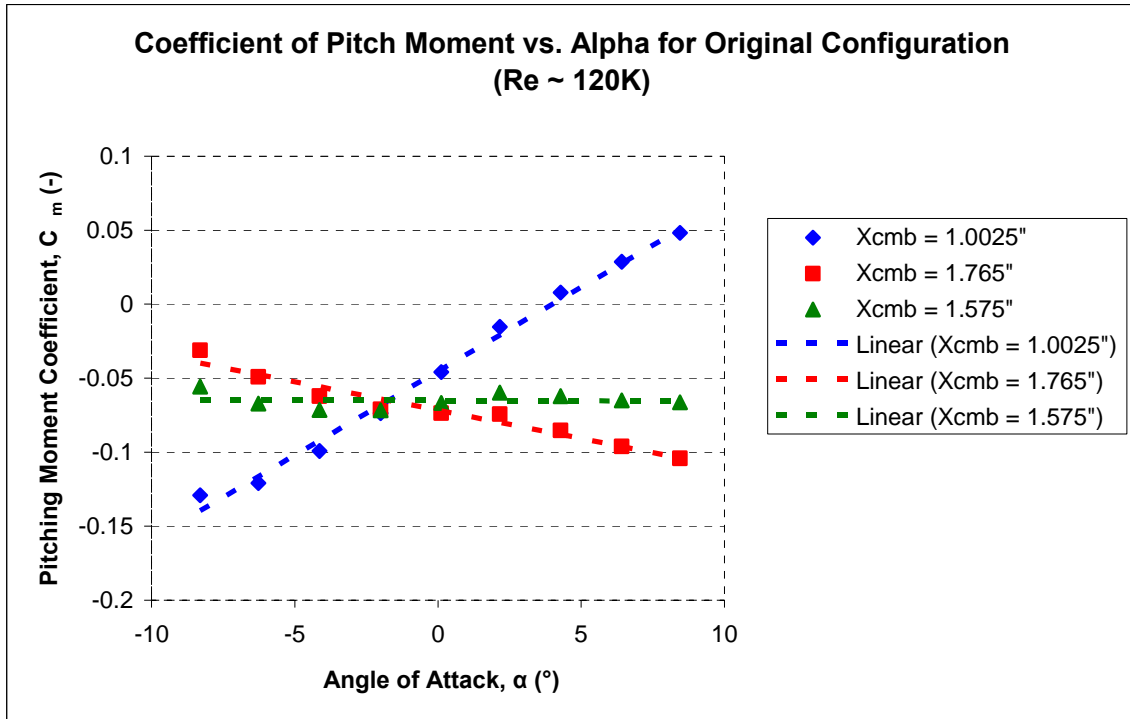


Figure 114: Coefficient of Pitch Moment vs. Alpha to determine the Neutral Longitudinally Stable $C_{m\alpha}$

4.5 Vortex Centroid and Moment Calculations and Results

The vortex moment (rad-mm/s) in the y-direction and the y-coordinate of the vortex centroid were calculated from the Hot-Wire analysis data of the 24" Houck Configuration documented in Walker's thesis (30). The vortex moment was calculated for the 24" Houck Configuration (with and without flow guides) at an $\alpha \approx 4.13^\circ$ and a $Re \approx 125K$. The vorticity data was extracted from *Tecplot*, which was used to plot the vorticity in Figure 115.

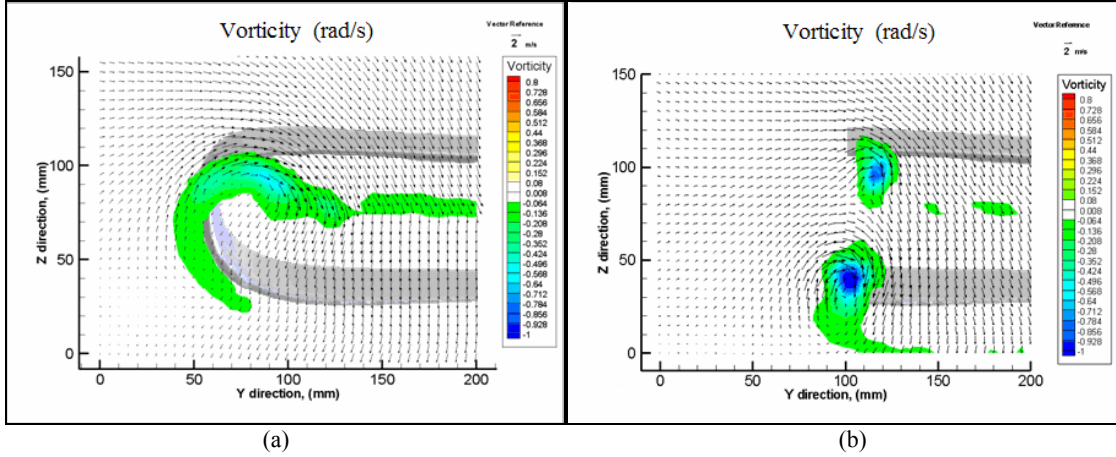


Figure 115: Hot-Wire Vorticity Analysis – $Re \sim 125K$ & $\alpha = 4.13^\circ$ (reproduced from Reference 30)
 (a) Houck 24" Vorticity with v & w vectors shown, (b) Houck 24" No Flow Guides Vorticity with v & w vectors shown

Once this data was extracted through a manual method involving multiple file conversions, a *MATLAB* code was used to reduce the data (App D). The first step in the reduction of the data was to filter out the positive vorticity noise. The next step was to sum the vorticity values at each y-direction coordinate. Once that was accomplished, the vortex moment could be found by multiplying the sum of the vortices at that y-coordinate (mm) by the y-coordinate value (Equation 23). The total vortex moment is the sum each vortex moment (Equation 24).

$$\Omega_{x \text{ y-moment}} = \left(\sum \omega_{x y_i} \right) \cdot y_i \quad (23)$$

$$\Omega_{\text{total-x y-moment}} = \sum \Omega_{x \text{ y-moment}_i} \quad (24)$$

where $\Omega_{x \text{ y-moment}}$ is the vortex moment in the y-direction (rad-mm/s), $\omega_{x y_i}$ is the vorticity value at the y-coordinate, y_i is the y-coordinate, $\Omega_{\text{total-x y-moment}}$ (rad-mm/s) is the total vortex moment for the entire grid. Finite wing theory suggests that, for a given lift per unit span, the circulation of the trailing vortex system should be equal for the two cases.

An outward displacement of the streamwise vortex system is consistent with a reduction of induced drag.

Once the total vortex moment was calculated, the next step was to divide the total vortex moment by the total vorticity of the entire grid to get the y-coordinate centroid location (Equation 25).

$$y_{\text{vortex centroid}} = \frac{\Omega_{\text{total-x,y-moment}}}{\omega_{\text{total}}} \quad (25)$$

where $y_{\text{vortex centroid}}$ is the y-coordinate of the vortex centroid from the mid-span (mm), $\Omega_{\text{total-x,y-moment}}$ (rad-mm/s) is the total vortex moment for the entire grid, and ω_{total} is the total vorticity of the grid (rad/s).

The results for $y_{\text{vortex centroid ND}}$ and $y_{\text{vortex centroid}}$ calculations are located in Table 35 and they are plotted on Figure 116.

Table 35: Vortex Centroid Calculations – Re ~ 120K

| Model Configuration | Lift (lbs) | Drag (lbs) | $y_{\text{vortex centroid}}$ (mm) |
|---------------------|------------|------------|-----------------------------------|
| 24" Houck | 0.609 | 0.094 | 250.8449 |
| 24" Houck NOFG | 0.586 | 0.088 | 238.2817 |

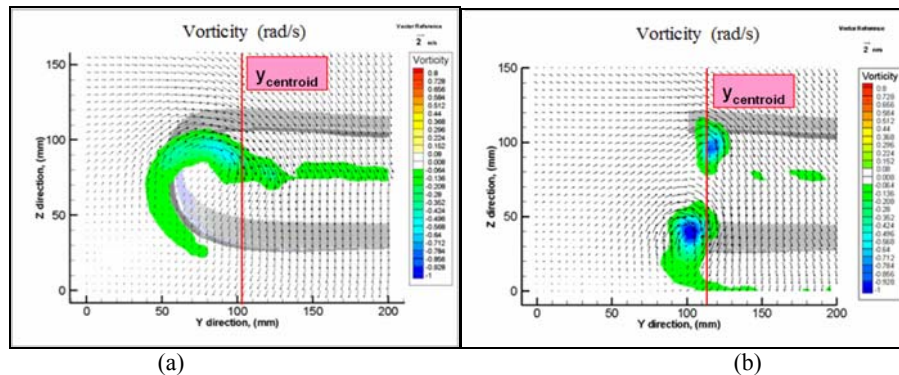


Figure 116: Y-coordinate Centroid on Hot-Wire Vorticity Analysis – Re ~ 125K & $\alpha = 4.13^\circ$ (reproduced from Reference 31)

(a) Houck 24" Vorticity with v & w vectors shown, (b) Houck 24" No Flow Guides Vorticity with v & w vectors shown

From these results, the y-coordinate of the vortex centroid of the No Flow Guide 24" Houck has a greater value than the flow guide case. This result suggests the Flow Guide 24" model is able to displace the vortex centroid farther out than the No Flow Guide model. Lift-to-drag for the two cases are $L/D = 6.5$ for the Flow Guide model and $L/D = 6.67$ for the No Flow Guide model (30).

V. Conclusions and Recommendations

5.1 Conclusions of Research

The purpose of this study was to investigate the aerodynamic performance of Claim 14 and 17 in the Houck Lifting Foil Patent (16) that relates to the design of the flow guides. It has been shown that three of the five models (Original Configuration, +5° Cant, and -5° Cant) that were constructed for use in this study followed the description outlined in the claim (curved, variable camber, etc.). The other two models (Endplate and No Flow Guide Configurations) were built as references for comparison.

When compared to the No Flow Guide Configuration Model, the Original Configuration Model was shown to have a 10.1% decrease in L/D_{\max} at $Re \approx 38K$, a 3.1% increase at $Re \approx 57K$, a 5.9% increase at $Re \approx 78K$, and a 1.3% increase at $Re \approx 120K$. It has also been shown to have a 6.3% decrease in $C_L^{(3/2)}/C_D$ at $Re = 38K$, a 9.1% increase at $Re = 57K$, a 8.5% increase at $Re = 78K$, and a 5.3% increase at $Re = 120K$. For both cases, maximizing range and endurance, the performance of the Original Configuration Model increased to become a positive parameter; but towards the higher Reynolds number, the trend of performance increase diminished. Further testing is needed to determine if the trend would cause a performance gap in these parameters.

When compared to the No Flow Guide Configuration Model, the +5° Cant Model was shown to have an 8.1% decrease in L/D_{\max} at $Re \approx 38K$, a 3.1% increase at $Re \approx 57K$, a 3.7% increase at $Re \approx 78K$, and a 0.3% increase at $Re \approx 120K$. It has also been shown to have a 0.4% decrease in $C_L^{(3/2)}/C_D$ at $Re = 38K$, a 9.1% increase at $Re = 57K$, a 4.1% increase at $Re = 78K$, and a 2.3% increase at $Re = 120K$. For both cases,

maximizing range and endurance, the performance of the +5° Cant Configuration Model increased to become a positive parameter; but towards the higher Reynolds number, the trend of performance increase diminished. Further testing is needed to determine if the trend would cause a performance gap in these parameters. As compared to the Original Flow Guide Configuration Model, the +5° Cant Configuration Model was less efficient at the higher Reynolds numbers proving the variation in flow guide geometry was a performance factor. Further testing of the geometrical variation of the flow guides is needed to determine its effects.

When compared to the No Flow Guide Configuration Model, the -5° Cant Model was shown to have a 2.8% decrease in L/D_{\max} at $Re \approx 38K$, a 3.2% increase at $Re \approx 57K$, a 4.6% increase at $Re \approx 78K$, and a 2.5% increase at $Re \approx 120K$. It has also been shown to have a 0.5% increase in $C_L^{(3/2)}/C_D$ at $Re = 38K$, a 4.4% increase at $Re = 57K$, a 2.1% increase at $Re = 78K$, and a 2.5% increase at $Re = 120K$. For both cases, maximizing range and endurance, the positive performance of the -5° Cant Configuration Model increased; but towards the higher Reynolds number, the trend of performance increase diminished. As compared to the Original Flow Guide Configuration Model, the -5° Cant Configuration Model was more efficient at the lower Reynolds number proving the variation in flow guide geometry was a performance factor. Further testing of the geometrical variation of the flow guides is needed to determine its effects.

The aerodynamic efficiency, measured by L/D_{\max} , of the flow guide configurations over the range of $Re \approx 57K$ to $120K$ were about 2-5% better than the No Flow Guide Configuration. At a Reynolds number of $38K$, the increase in skin friction

drag outweighed any possible reduction of induced drag for the flow guide configurations. The baseline value for the aerodynamic efficiency for the addition of winglets on a low-aspect-ratio delta wing is about 6.96% for a Reynolds number of 1,900K (27:38). The addition of flow guides does provide a comparable efficiency increase as compared to the addition of winglets on a low-aspect-ratio delta wing configuration.

When compared to the No Flow Guide Configuration Model, the Endplate Configuration Model was shown to have an 8.0% decrease in L/D_{\max} at $Re \approx 38K$, a 4.3% decrease at $Re \approx 57K$, a 7.6% decrease at $Re \approx 78K$, and a 11.1% decrease at $Re \approx 120K$. It has also been shown to have a 3.1% increase in $C_L^{(3/2)}/C_D$ at $Re = 38K$, a 1.3% increase at $Re = 57K$, a 2.5% decrease at $Re = 78K$, and a 5.3% decrease at $Re = 120K$. For both cases, maximizing range and endurance, the Endplate Configuration Model had a trend of decreasing performance to an over performance gap at the higher Reynolds numbers. Further testing of endplate geometry, possibly adding an airfoil shape to the endplate cross-section, is needed to determine its effects.

The tested error analysis was conducted on the Original Configuration Model at all Reynolds numbers. The percent error of lift-to-drag for the Original Configuration Model is nominally the same for all the models. This error analysis provided a confidence interval of approximately 99.9% due to a sample size of 22 points. At each model's given L/D_{\max} there is an approximate worst error of 4.23% and realistic error of 3.36% for $Re \approx 38K$, an approximate worst error of 1.96% and realistic error of 1.96% for $Re \approx 57K$, an approximate worst error of 1.30% and realistic error of 1.24% for $Re \approx 78K$, and an

approximate worst error of 0.64% and realistic error of 0.58% for $Re \approx 120K$. For the L/D_{max} comparison to the No Flow Guide Configuration the comparison errors are as follows: approximate worst error of 8.46% and realistic error of 6.72% for $Re \approx 38K$, an approximate worst error of 3.92% and realistic error of 3.92% for $Re \approx 57K$, an approximate worst error of 2.60% and realistic error of 2.28% for $Re \approx 78K$, and an approximate worst error of 1.28% and realistic error of 1.16% for $Re \approx 120K$.

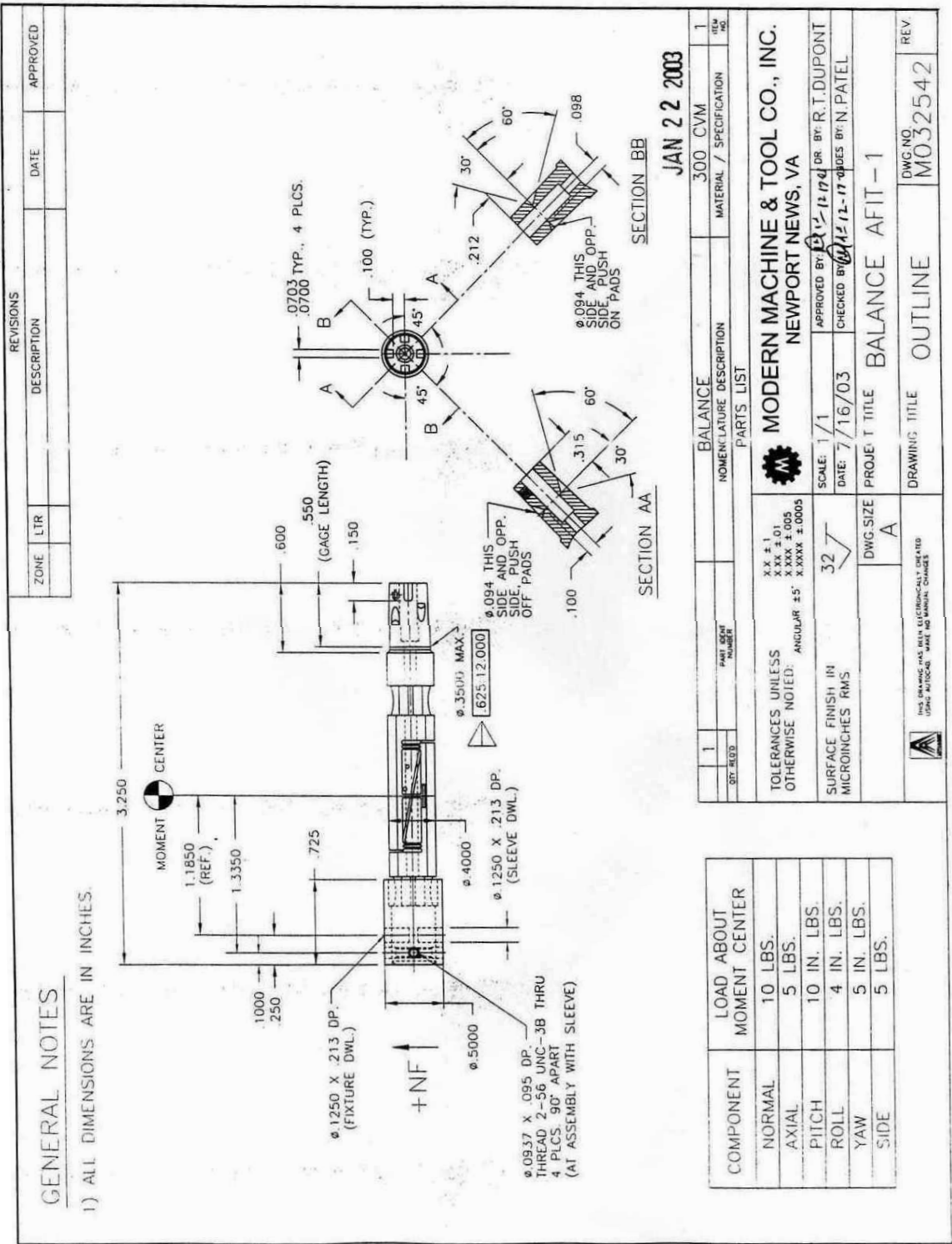
It has been shown in Section 4.3 that the effective aspect ratios, eAR, of the three flow guide configuration models (Original Configuration, +5° Cant, and -5° Cant) were greater than the No Flow Guide Configuration Model's effective aspect ratio at Reynolds numbers higher than 38K. From previous thesis research, it has been proven that the flow guides are successful in combining the upper and lower wing-tip vortices into one single vortex (31: 101). The effect of the combination of the vortices with the use of flow guides on an aerodynamic model as compared to an identical aerodynamic model without flow guides is an improvement in aerodynamic efficiency over a certain range of velocities. However, further investigation of the flow guide configuration will need to be conducted to determine the successful implementation of this configuration on other aircraft designs.

5.2 Recommendations for Future Research

It is recommended that there be continued testing of the flow guide configuration that is part of Houck Lifting Foil concept in order to better understand the design and its aerodynamic influence. CFD and experimental wind tunnel testing is suggested. CFD analysis should be utilized to explore geometric flow guide designs, in order to optimize design before experimental testing, and to compare data with experimental results.

Experimentally, more variable geometric flow guides with varying camber need to be utilized in order to validate patent claims and to further optimize the design. Also, a more aerodynamic baseline model should be designed to decrease the influence of aerodynamic parameters that conflict with the flow guide design. This baseline model should utilize the same wingspan and planform area as the models with flow guides.

Appendix A: 10 lb Balance Dimensions



Appendix B: *MATLAB* 10 lb Balance Code

```
%*****
%*****
%*****      Lt. Gebbie & Capt Anthony DeLuca      *****
%*****  Adapted for the Balance AFIT 1 by Lt. Rivera Parga *****
%*****  re-adapted by Troy Leveron, ENS, USNR      *****
%*****  Calculation of Lift, Drag, Moments           *****
%*****  FLEX WING, Prop OFF, ALPHA SWEEPS          *****
%*****
%*****  re-adapted by 1Lt Michael Walker, ENY, USAF *****
%*****  re-adapted by ENS Dermot Killian, ENY, USN *****
%*****
%This Code will transfer measured Forces and Moments on the AFIT 1 balance to Wind
%(earth) centered frame of reference by correcting for tare effects, balance
%interactions, and wind tunnel irregularities, then gives a file with all the
%corrected data

clear; clc; close all;
format long
%#####
%      INPUT DECK
%FIRST FILL THE FOLLOWING INFORMATION (modified by D. Killian on 17 Apr, 2007)

Masskg=0.346;      %kgs - Mass of Original Configuration Model (0.7628lbs)

T_room = mean([74.2]) + 459.67;      %deg R  ****Room Temperature on 23 Apr 2007****
P_barro = mean(28.9723) * 0.4911541;  %Psi  ****Pressure on 23 Apr 2007****

load killian_origcfg2_tare_a_n8to15.txt;      %tarefile tare.txt - CHANGE FOR EACH TEST RUN
TareFile = killian_origcfg2_tare_a_n8to15(:,1:9);

load killian_60m_origcfg2_a_n8to15.txt;      %datafile .txt - CHANGE FOR EACH TEST RUN
DataFile = killian_60m_origcfg2_a_n8to15(:,1:9);

%Offset distances from the Mounting Block to the Model C.G.,%(inches)
Y_cmb = 0;
X_cmb = 1.0025;      %inches (from origin @ balance center w/ + forward)
Z_cmb = -0.53;      %inches (from origin @ balance center w/ + down)

% Queried for the Solid body blockage corrections due to wing and fuselage

Body_Volume = 17.78/(12^3);      %(ft^3): SOLIDWORKS Original Model
Wing_Area = 72.58/(12^2);      %(ft^2): SOLIDWORKS Original Model
c_bar = 2.55/12;      % (ft): SOLIDWORKS Original Model
span = 13.808/12;      % (ft): SOLIDWORKS Original Model
root_chord = 2.55/12;      % (ft): SOLIDWORKS Original Model
%*****
% Queried for the Pitching Moment Correction (NOT USED FOR HOUCK MODEL)

% l_t = 9/12;      % ft = length from tail MAC to aircraft CG
% Span_t =(4+(6/16)) / 12;      % ft = horizontal span
% Tail_Area = (9.42962435) / 144;      % ft^2 = horizontal tail area
%*****
```

```

%#####
%II.- Room Conditions and Model Specifics :
%   UNITS are in Ft, Sec, lbm, Psf, Rankine, fps
%#####

Mass = (Masskg * 1000) * 0.0022046;           %lbm (24 in Houck Model)
Gas_Const = 1716;                             %ft-lbf/Slug-R
Density = (P_barro * 144)/(1716 * T_room);     %lbm/ft^3 or lbf-s^2/ft^4
Root_Chord = root_chord;                      %ft
Span = span;                                  %ft
Aspect_Ratio = Span^2 / Wing_Area;
Kinematic_Viscosity = .372e-6;                %slug/ft-s
Speed_of_Sound = sqrt(1.4 * T_room * Gas_Const); %fps

%#####
%III.- Solid body blockage corrections due to wing and fuselage
%#####

K_1 = 0.9;
K_3 = 0.93;
delta = 0.1177;
Tau_1 = 0.83125;                             % from page XXX in text - Figure XX
X_Section = (31/12)*(44/12);                  %ft^2
Wing_Volume = Body_Volume;                    %ft^3

Epsilon_sb_w = (K_1*Tau_1*Wing_Volume) / X_Section^(3/2);
Epsilon_sb_b = (K_3*Tau_1*Body_Volume) / X_Section^(3/2);
Epsilon_tot = Epsilon_sb_w + Epsilon_sb_b;
%Epsilon_tot = Epsilon_sb_w ;

%#####
% III.- Load the static tare data for the alpha sweep w/o the wind ,
%   separate each force from the file, and fit a 4th order poly
%   as an x-y plot (AoA vs.Force) for each of the 6 force sensors.
%#####

FILE=TareFile(:,:);                          % Pulls in tare data file

j=1;
k=1;
L=length(FILE);

for i=1:L                                     %Run for all data points # of rows
    if i~=L                                  %if current row is not last row, go to next
        NEXT=i+1;                          %set next equal to the value of the next row
        VALUE2=FILE(NEXT,1);               %set value2 as next row column 1
    else if i==L                             %unless the it is the last value
        VALUE2=50;                         %value2 set to 50 to end the sequence
    end
    A(j,:)=FILE(i,:);                      %set row j of A equal to row i of FILE
    VALUE1=FILE(i,1);                      %set value1 equal to row i column 1 of FILE
    if VALUE1==VALUE2                      %if value1 equals value2, go to next row
        j=j+1;
    end
end

```

```

else if VALUE1~=VALUE2           %if value1 and value2 are different check
    if length(A(:,1))<5           %if less than 5 values, ignored due to angle change
        j=1;
        clear A;
    else if length(A(:,1))>5       %if more than 5 values
        C=length(A(:,1));         %find length of A
        for m=1:9                 %Average all rows of the like values in A
            B(k,m)=mean(A(4:C,m)); %disregarding first 3 for vibrations
        end
        j=1;
        k=k+1;
        clear A
    end
end

end
end
end

if B(k-1,1)<B((k-2),1)
    B=B(1:(k-2),:)
end

tare=[B];

%_____End of inserted code
[row,col] = size(tare);

for k = 1:row;

    theta_tare(k,,:) = tare(k,1).*(pi/180);
    NF_tare(k,,:)    = tare(k,4);
    PM_tare(k,,:)    = tare(k,5);
    AF_tare(k,,:)    = tare(k,6);
    SF_tare(k,,:)    = tare(k,7);
    YM_tare(k,,:)    = tare(k,8);
    RM_tare(k,,:)    = tare(k,9);

end

NF_poly = polyfit(theta_tare,NF_tare,4);
PM_poly = polyfit(theta_tare,PM_tare,4);
AF_poly = polyfit(theta_tare,AF_tare,4);
SF_poly = polyfit(theta_tare,SF_tare,4);
YM_poly = polyfit(theta_tare,YM_tare,4);
RM_poly = polyfit(theta_tare,RM_tare,4);

```

```

#####
%IV.- Load the specific test run files,
#####

clear('AA','B','C','L')
%_____

FILE=DataFile(:,:);          % Pulls in test data file

j=1;
k=1;
L=length(FILE);

for i=1:L                      %Run for all data points # of rows
    if i~=L                    %if current row is not last row, go to next
        NEXT=i+1;              %set next equal to the value of the next row
        VALUE2=FILE(NEXT,1);    %set value2 as next row column 1
    else if i==L                %unless the it is the last value
        VALUE2=50;              %value2 set to 50 to end the sequence
    end
    end
    A(j,:)=FILE(i,:);          %set row j of A equal to row i of FILE
    VALUE1=FILE(i,1);           %set value1 equal to row i column 1 of FILE
    if VALUE1==VALUE2            %if value1 equals value2, go to next row
        j=j+1;
    else if VALUE1~=VALUE2        %if value1 and value2 are different check
        if length(A(:,1))<5      %if less than 5 values, ignored due to angle change
            j=1;
            clear A;
        else if length(A(:,1))>5 %if more than 5 values
            C=length(A(:,1));      %find length of A
            for m=1:9               %Average all rows of the like values in A
                B(k,m)=mean(A(4:C,m)); %disregarding first 3 for vibrations
            end
            j=1;
            k=k+1;
            clear A;
        end
    end
end
end
end
end

% if B(k-1,1)<B((k-2),1)
%   B=B(1:(k-2),:)
% end

sample_data=[B];

%_____End of inserted code

[row2,col2] = size(sample_data);
for i = 1:row2;

```

%Angles of the model during test runs (Roll, Pitch {AoA}, Yaw {Beta}):

```
phi = 0;
theta(i,:) = sample_data(i,1) .* (pi/180)-(0*pi/180); %radians
si(i,:) = sample_data(i,2) .* (pi/180); %radians
Wind_Speed(i,:) = sample_data(i,3) .* (5280/3600); %fps
```

%Flight Parameters (Re#, Ma#, Dynamic Pressure):

```
q = (.5 * Density) .* Wind_Speed.^2; %lbf/ft^2
q_Corrected = q .* (1 + Epsilon_tot)^2; %lbf/ft^2
Wind_Speed_Corrected = Wind_Speed .* (1 + Epsilon_tot); %fps
Mach_Number = Wind_Speed_Corrected ./ Speed_of_Sound; %NonDimensional
Reynolds_Number = ((Density * Root_Chord) .* Wind_Speed_Corrected) ./ Kinematic_Viscosity; %NonDimensional
Flight_Parameters = [Mach_Number Reynolds_Number q_Corrected]
```

%individual forces and moments for each sensor:

%NEW NOTATION

```
NF_test(i,:,:) = sample_data(i,4);
PM_test(i,:,:) = sample_data(i,5);
AF_test(i,:,:) = sample_data(i,6);
SF_test(i,:,:) = sample_data(i,7);
YM_test(i,:,:) = sample_data(i,8);
RM_test(i,:,:) = sample_data(i,9);
```

```
%#####
%V.- Subtract the effect of the static
% weight with the tare polynomials above
%#####
```

%Evaluating the actual test theta angle (AoA) in the tare polynomial to
%determine the tare values for the angles tested in each run.

```
NF_eval = polyval(NF_poly,theta);
PM_eval = polyval(PM_poly,theta);
AF_eval = polyval(AF_poly,theta);
SF_eval = polyval(SF_poly,theta);
YM_eval = polyval(YM_poly,theta);
RM_eval = polyval(RM_poly,theta);
```

%The Time-Averaged (raw) forces and momentums NF,AF,SF,PM,YM AND RM measurd in the wind
%tunnel (body axis) with the tare effect of the weight subtracted off.

```
NF_resolved = NF_test - (NF_eval);
PM_resolved = PM_test - (PM_eval);
AF_resolved = AF_test - (AF_eval); % check this 8-17-04
SF_resolved = SF_test - (SF_eval);
YM_resolved = YM_test - (YM_eval);
RM_resolved = RM_test - (RM_eval);
```

```
Forces_minus_tare = [NF_resolved, AF_resolved, PM_resolved, RM_resolved, YM_resolved,  
SF_resolved];
```

```

#####
%VI.- CORRECT FORCES AND MOMENTS FOR BALANCE INTERATIONS (body axis)
#####

%USING THE REDUCTION EQUATIONS
%LET US SET A MAXIMUN NUMBER OF INTERATIONS (FOR AVOIDING AN INFINIT LOOP)
MAXIT=100;
%SET THE LIMIT FOR THE DIFFERENCE BETWEEN INTERATIONS(CRITERIA FOR FINISH
THE INTERATIONS)
LIMIT= 10E-14;

%MATCHING EACH NAME WITH THE DATA
% Prof. Reeder added :i
MNF=NF_resolved(i);
MAF=AF_resolved(i);
MPM=PM_resolved(i);
MRM=RM_resolved(i);
MYM=YM_resolved(i);
MSF=SF_resolved(i);

%INPUT OF THE CONSTANTS VALUES FROM THE MATRIX FOR SENSITIVITIES AND
INTERATIONS
K=[0 -1.3567E-03 -3.8021E-03 -4.2814E-03 -1.6966E-03 1.7567E-03 ...
5.3167E-05 -1.3867E-04 -5.5629E-05 3.5181E-05 1.0601E-05 -2.5271E-04...
5.6693E-05 -1.9537E-04 1.7908E-05 -3.6606E-05 -4.9934E-05 4.1205E-05...
2.5648E-05 -1.9289E-05 8.9661E-05 -1.9594E-05 -4.9859E-04 -1.1599E-03...
5.7163E-05 8.9798E-05 -7.8591E-05 9.3187E-03 0 -3.8421E-03 3.5740E-03...
9.7714E-05 -2.7776E-03 -1.3552E-04 5.1538E-04 2.2082E-04 -1.2706E-05...
-2.3637E-05 1.3686E-05 1.1085E-04 -3.6557E-06 4.9876E-06 8.1085E-06...
3.7381E-05 1.2791E-04 -9.4527E-06 -2.3083E-06 -1.2046E-06 7.8161E-04...
-1.1997E-03 -3.0560E-05 -6.6202E-05 3.7227E-04 -2.1469E-04 4.8386E-03...
-3.7387E-03 0 -1.8479E-02 3.9077E-03 9.9165E-04 -1.4825E-05 -1.4830E-06...
6.0845E-05 8.0667E-05 1.8547E-05 -5.0212E-05 1.0539E-04 -2.2676E-04...
4.3793E-05 -1.0456E-05 -8.1186E-06 -2.1653E-05 -3.3070E-05 1.7280E-05...
-7.4509E-05 -3.4399E-05 -8.2999E-04 -6.7962E-04 4.0521E-05 -5.1604E-05...
9.1132E-06 -5.7360E-03 -2.2213E-04 9.9131E-04 0 -9.5790E-03 6.7114E-03...
3.6824E-05 1.0056E-04 -3.7105E-05 -9.0295E-05 -7.4580E-05 1.4814E-04...
7.2634E-05 -8.4778E-06 6.3486E-05 5.6328E-05 -1.3617E-04 2.2196E-05...
1.3606E-05 -3.6689E-05 8.3283E-05 1.1865E-04 1.8544E-05 -1.9831E-05...
1.7894E-05 -6.8164E-05 -7.0892E-05 1.2378E-03 1.6961E-03 -6.5102E-03...
-9.3202E-03 0 5.1349E-03 1.3612E-05 -1.3175E-04 7.2442E-06 5.6705E-04...
-1.4723E-05 -4.8656E-05 -1.4282E-04 5.9711E-05 5.9046E-05 -3.6490E-04...
7.4881E-05 5.4601E-06 1.0129E-03 -1.3867E-04 8.1617E-05 6.6053E-05...
-1.3417E-05 9.0025E-05 -4.5362E-05 -4.4672E-06 9.5087E-05 -3.4077E-02...
7.9142E-04 1.6667E-03 -6.6512E-03 8.1538E-03 0 -1.4185E-05 7.3209E-05...
-2.5849E-05 1.2325E-03 -4.1696E-05 4.6266E-05 8.6146E-05 2.1436E-05...
5.0874E-05 -3.2738E-04 2.2218E-04 8.6478E-06 7.3395E-04 -4.1453E-05...
3.5719E-05 2.5313E-05 1.5182E-04 3.6007E-05 -2.8844E-05 8.9741E-05...
-7.3257E-05];

```

%COMPUTE THE UNCORRECTED FORCES AND MOMENTS BY
 %CONSIDERING THAT THE PRIME SENSITIVITY CONSTANTS ARE ALREADY APLIED:

NF1=MNF;
 AF1=MAF;
 PM1=MPM;
 RM1=MRM;
 YM1=MYM;
 SF1=MSF;

%FOR THE FIRST INTERACTION LET US INITIALIZE THE VALUES OF FORCES AND
 %MOMENTS WITH THE VALUES OF THE UNCORRECTED FORCES AND MOMENTS

NF(1)=NF1;
 AF(1)=AF1;
 PM(1)=PM1;
 RM(1)=RM1;
 YM(1)=YM1;
 SF(1)=SF1;

%DOING THE INTERACTION EQUATIONS:

for n=2:MAXIT;

NF(n)=NF1-((K(2)*AF(n-1))+(K(3)*PM(n-1))+(K(4)*RM(n-1))+(K(5)*YM(n-1))+(K(6)*SF(n-1)))+(K(7)*NF(n-1)^2)+...
 (K(8)*(NF(n-1)*AF(n-1)))+(K(9)*(NF(n-1)*PM(n-1)))+(K(10)*(NF(n-1)*RM(n-1)))+(K(11)*(NF(n-1)*YM(n-1)))+...
 (K(12)*(NF(n-1)*SF(n-1)))+(K(13)*(AF(n-1)^2))+(K(14)*(AF(n-1)*PM(n-1)))+(K(15)*(AF(n-1)*RM(n-1)))+...
 (K(16)*(AF(n-1)*YM(n-1)))+(K(17)*(AF(n-1)*SF(n-1)))+(K(18)*(PM(n-1)^2))+(K(19)*(PM(n-1)*RM(n-1)))+...
 (K(20)*(PM(n-1)*YM(n-1)))+(K(21)*(PM(n-1)*SF(n-1)))+(K(22)*(RM(n-1)^2))+(K(23)*(RM(n-1)*YM(n-1)))+...
 (K(24)*(RM(n-1)*SF(n-1)))+(K(25)*(YM(n-1)^2))+(K(26)*(YM(n-1)*SF(n-1)))+(K(27)*(SF(n-1)^2)));

AF(n)=AF1-((K(28)*NF(n-1))+(K(30)*PM(n-1))+(K(31)*RM(n-1))+(K(32)*YM(n-1))+(K(33)*SF(n-1)))+(K(34)*NF(n-1)^2)+...
 (K(35)*(NF(n-1)*AF(n-1)))+(K(36)*(NF(n-1)*PM(n-1)))+(K(37)*(NF(n-1)*RM(n-1)))+(K(38)*(NF(n-1)*YM(n-1)))+...
 (K(39)*(NF(n-1)*SF(n-1)))+(K(40)*(AF(n-1)^2))+(K(41)*(AF(n-1)*PM(n-1)))+(K(42)*(AF(n-1)*RM(n-1)))+...
 (K(43)*(AF(n-1)*YM(n-1)))+(K(44)*(AF(n-1)*SF(n-1)))+(K(45)*(PM(n-1)^2))+(K(46)*(PM(n-1)*RM(n-1)))+...
 (K(47)*(PM(n-1)*YM(n-1)))+(K(48)*(PM(n-1)*SF(n-1)))+(K(49)*(RM(n-1)^2))+(K(50)*(RM(n-1)*YM(n-1)))+...
 (K(51)*(RM(n-1)*SF(n-1)))+(K(52)*(YM(n-1)^2))+(K(53)*(YM(n-1)*SF(n-1)))+(K(54)*(SF(n-1)^2)));

PM(n)=PM1-((K(55)*NF(n-1))+(K(56)*AF(n-1))+(K(58)*RM(n-1))+(K(59)*YM(n-1))+(K(60)*SF(n-1)))+(K(61)*NF(n-1)^2)+...
 (K(62)*(NF(n-1)*AF(n-1)))+(K(63)*(NF(n-1)*PM(n-1)))+(K(64)*(NF(n-1)*RM(n-1)))+(K(65)*(NF(n-1)*YM(n-1)))+...

$$\begin{aligned}
& (K(66)*(NF(n-1)*SF(n-1)))+(K(67)*(AF(n-1)^2))+(K(68)*(AF(n-1)*PM(n-1)))+(K(69)*(AF(n-1)*RM(n-1)))+... \\
& (K(70)*(AF(n-1)*YM(n-1)))+(K(71)*(AF(n-1)*SF(n-1)))+(K(72)*(PM(n-1)^2))+(K(73)*(PM(n-1)*RM(n-1)))+... \\
& (K(74)*(PM(n-1)*YM(n-1)))+(K(75)*(PM(n-1)*SF(n-1)))+(K(76)*(RM(n-1)^2))+(K(77)*(RM(n-1)*YM(n-1)))+... \\
& (K(78)*(RM(n-1)*SF(n-1)))+(K(79)*(YM(n-1)^2))+(K(80)*(YM(n-1)*SF(n-1)))+(K(81)*(SF(n-1)^2));
\end{aligned}$$

$$\begin{aligned}
RM(n)=RM1- & ((K(82)*NF(n-1))+(K(83)*AF(n-1))+(K(84)*PM(n-1))+(K(86)*YM(n-1))+(K(87)*SF(n-1)))+(K(88)*NF(n-1)^2)+... \\
& (K(89)*(NF(n-1)*AF(n-1)))+(K(90)*(NF(n-1)*PM(n-1)))+(K(91)*(NF(n-1)*RM(n-1)))+(K(92)*(NF(n-1)*YM(n-1)))+... \\
& (K(93)*(NF(n-1)*SF(n-1)))+(K(94)*(AF(n-1)^2))+(K(95)*(AF(n-1)*PM(n-1)))+(K(96)*(AF(n-1)*RM(n-1)))+... \\
& (K(97)*(AF(n-1)*YM(n-1)))+(K(98)*(AF(n-1)*SF(n-1)))+(K(99)*(PM(n-1)^2))+(K(100)*(PM(n-1)*RM(n-1)))+... \\
& (K(101)*(PM(n-1)*YM(n-1)))+(K(102)*(PM(n-1)*SF(n-1)))+(K(103)*(RM(n-1)^2))+(K(104)*(RM(n-1)*YM(n-1)))+... \\
& (K(105)*(RM(n-1)*SF(n-1)))+(K(106)*(YM(n-1)^2))+(K(107)*(YM(n-1)*SF(n-1)))+(K(108)*(SF(n-1)^2));
\end{aligned}$$

$$\begin{aligned}
YM(n)=YM1- & ((K(109)*NF(n-1))+(K(110)*AF(n-1))+(K(111)*PM(n-1))+(K(112)*RM(n-1)))+(K(114)*SF(n-1))+(K(115)*NF(n-1)^2)+... \\
& (K(116)*(NF(n-1)*AF(n-1)))+(K(117)*(NF(n-1)*PM(n-1)))+(K(118)*(NF(n-1)*RM(n-1)))+(K(119)*(NF(n-1)*YM(n-1)))+... \\
& (K(120)*(NF(n-1)*SF(n-1)))+(K(121)*(AF(n-1)^2))+(K(122)*(AF(n-1)*PM(n-1)))+(K(123)*(AF(n-1)*RM(n-1)))+... \\
& (K(124)*(AF(n-1)*YM(n-1)))+(K(125)*(AF(n-1)*SF(n-1)))+(K(126)*(PM(n-1)^2))+(K(127)*(PM(n-1)*RM(n-1)))+... \\
& (K(128)*(PM(n-1)*YM(n-1)))+(K(129)*(PM(n-1)*SF(n-1)))+(K(130)*(RM(n-1)^2))+(K(131)*(RM(n-1)*YM(n-1)))+... \\
& (K(132)*(RM(n-1)*SF(n-1)))+(K(133)*(YM(n-1)^2))+(K(134)*(YM(n-1)*SF(n-1)))+(K(135)*(SF(n-1)^2));
\end{aligned}$$

$$\begin{aligned}
SF(n)=SF1- & ((K(136)*NF(n-1))+(K(137)*AF(n-1))+(K(138)*PM(n-1))+(K(139)*RM(n-1)))+(K(140)*YM(n-1))+(K(142)*NF(n-1)^2)+... \\
& (K(143)*(NF(n-1)*AF(n-1)))+(K(144)*(NF(n-1)*PM(n-1)))+(K(145)*(NF(n-1)*RM(n-1)))+(K(146)*(NF(n-1)*YM(n-1)))+... \\
& (K(147)*(NF(n-1)*SF(n-1)))+(K(148)*(AF(n-1)^2))+(K(149)*(AF(n-1)*PM(n-1)))+(K(150)*(AF(n-1)*RM(n-1)))+... \\
& (K(151)*(AF(n-1)*YM(n-1)))+(K(152)*(AF(n-1)*SF(n-1)))+(K(153)*(PM(n-1)^2))+(K(154)*(PM(n-1)*RM(n-1)))+... \\
& (K(155)*(PM(n-1)*YM(n-1)))+(K(156)*(PM(n-1)*SF(n-1)))+(K(157)*(RM(n-1)^2))+(K(158)*(RM(n-1)*YM(n-1)))+... \\
& (K(159)*(RM(n-1)*SF(n-1)))+(K(160)*(YM(n-1)^2))+(K(161)*(YM(n-1)*SF(n-1)))+(K(162)*(SF(n-1)^2));
\end{aligned}$$

```
% SET THE LIMIT FOR THE DIFFERENCE BETWEEN ITERATIONS(CRITERIA FOR FINISH
THE ITERATIONS)
```

```
DIFFNF(n)=abs(NF(n)-NF(n-1));
DIFFAF(n)=abs(AF(n)-AF(n-1));
DIFFPM(n)=abs(PM(n)-PM(n-1));
DIFFRM(n)=abs(RM(n)-RM(n-1));
DIFFYM(n)=abs(YM(n)-YM(n-1));
DIFFSF(n)=abs(SF(n)-SF(n-1));
```

```
if DIFFNF(n)&DIFFAF(n)&DIFFPM(n)&DIFFRM(n)&DIFFYM(n)&DIFFSF(n) < LIMIT
break
```

```
end
```

```
end
```

```
%disp('THE FINAL VALUES ARE (NF,AF,PM,RM,YM,SF):')
Corrected_Data(:,i)=[NF(n);AF(n);PM(n);RM(n);YM(n);SF(n)];
```

```
%disp('THE FINAL DIFFERENCE BETWEEN ITERATIONS ARE(FOR NF,AF,PM,RM,YM,SF) :')
%FINAL_DIFFERENCE=[DIFFNF(n),DIFFAF(n),DIFFPM(n),DIFFRM(n),DIFFYM(n),DIFFSF(n)]
```

```
%disp('THE NUMBER OF ITERATIONS USED WAS:')
%n
```

```
%#####
%VII.- Calculation of the Axial, Side, & Normal Forces from the corrected balance
%   forces in the Body Axis reference frame
%#####
```

```
Forces_b(:,i)=[Corrected_Data(2,i); Corrected_Data(6,i); Corrected_Data(1,i)];
```

```
%Calculation of the Drag, Side, & Lift Forces in the Wind Axis reference
%frame
```

```
Forces_w=[Forces_b(1,:).*cos(theta').*cos(si')+Forces_b(2,:).*sin(si')+Forces_b(3,:).*sin(theta').*cos(si');
%in radians
-Forces_b(1,:).*sin(si').*cos(theta')+Forces_b(2,:).*cos(si')-Forces_b(3,:).*sin(theta').*sin(si');
-Forces_b(1,:).*sin(theta')+Forces_b(3,:).*cos(theta')];
```

```
%First entry is the moments calculated by the balance or direct calculation
%in the Body Reference Frame. Balance measures Roll (l), Yaw is about the
%z-axis (n), and Pitch is about the y-axis (m). Distances from strain
%gages to C.G. are in INCHES. Moments are in-lbf. See pp. 236-238 of
%Barlow et. al., 3rd ed.
```

```
m = Corrected_Data(3,i);
n = Corrected_Data(5,i);
l = Corrected_Data(4,i);
```

```
Moments_b(:,i)=[l; m; n];
```

%Second entry is the conversion from the "Balance Centeric" moments to the
%Wind Reference monments with respect to the Balance Center (bc)

```
Moments_w_bc = [Moments_b(1,:).*cos(theta').*cos(si')-  
Moments_b(2,:).*sin(si')+Moments_b(3,:).*sin(theta').*cos(si');
```

```
Moments_b(1,:).*sin(si').*cos(theta')+Moments_b(2,:).*cos(si')+Moments_b(3,:).*sin(theta').*sin(si');  
-Moments_b(1,:).*sin(theta')+Moments_b(3,:).*cos(theta')];
```

%Finally, the balance centered moments are converted to moments about the
%Model's Center of Mass (cm) or Center of Gravity (CG)

```
cgdist=sqrt((X_cmb)^2+(Z_cmb)^2); %Obtaining the direct distance between the  
%center of the balance and the center of mass  
w=atan(-Z_cmb/X_cmb); %Obtaining the angle between cgdist and the x axes at zero angle of attack
```

```
X_cm(i,:)= cos(theta(i,:)+w)*cos(si(i,:))*(cgdist);  
Y_cm(i,:)= Y_cmb + X_cm(i,:)*tan(si(i,:)); % appropriate for very small y_cmb and reasonable si  
Z_cm(i,:)= -sin(theta(i,:)+w)*(cgdist);
```

```
Moments_w_cg_u = [Moments_w_bc(1,:) + Z_cm(i,:)*Forces_w(2,:) + Forces_w(3,)* Y_cm(i,:);  
Moments_w_bc(2,:) - Forces_w(3,)* X_cm(i,:) + Forces_w(1,)* Z_cm(i,:);  
Moments_w_bc(3,:) - Forces_w(1,)* Y_cm(i,:) - Forces_w(2,)* X_cm(i,:)];
```

```
%#####
```

%VIII.- Calculation of the actual Lift and Drage nondimensional Coefficients, uncorrected for tunnel
effects, (Cl

% and Cd)

```
%#####
```

```
C_D_u = Forces_w(1,:) ./ (q_Corrected' .* Wing_Area);  
C_Y_u = Forces_w(2,:) ./ (q_Corrected' .* Wing_Area);  
C_L_u = Forces_w(3,:) ./ (q_Corrected' .* Wing_Area); %Keuthe & Chow pg 178  
Coefficients = [C_L_u; C_D_u; C_Y_u];  
Ave_Cl = mean(Coefficients(:,1));  
Ave_Cd = mean(Coefficients(:,2));
```

end

```
%#####
```

%IX Drag Coefficient Correction

```
%#####
```

```
C_D_o = min(Coefficients(:,2));  
C_L_u_sqrd = Coefficients(:,1).^2;  
Delta_C_D_w = ((delta * Wing_Area) / X_Section) .* C_L_u_sqrd;  
C_D_Corrected = C_D_u' + Delta_C_D_w;
```

```

%#####
%X.- Angle of Attack due to upwash Correction
%#####

alpha_before = sample_data(:,1);
alpha=[alpha_before]-[0]; %18APR05 change to 5 for sting block angle, then back to 0 for Aero 517 SU
2005 *****
Delta_alpha_w = ((delta * Wing_Area) / X_Section) .* (57.3 * C_L_u);
alpha_Corrected = alpha + Delta_alpha_w';

%#####
%XI.- Pitching Moment Correction
%#####

% tau2 = 0.65;
c_bar = c_bar; % ft = Mean Chord of wing
% V_bar = 0 / (Wing_Area * c_bar); % Horizontal tail volume ratio
% eta_t = 1.0;
% epsilon_o = 0;
% i_t = pi/4; % radians
% i_w = 0;
% Aspect_Ratio_t = Span_t^2 / Tail_Area;
%
% D_epsilon_D_alpha = ((2 .* C_L_u) ./ (pi* Aspect_Ratio_t))';
% epsilon = epsilon_o + (D_epsilon_D_alpha .* alpha_Corrected);
% alpha_t = alpha_Corrected - i_w - epsilon + i_t;
% C_L_alpha_t = 0 %((0.1* Aspect_Ratio) / (Aspect_Ratio_t + 2)) * 0.8;
% D_Cm_cg_t_D_alpha_t = -C_L_alpha_t * V_bar * eta_t;
% Delta_C_m_cg_t = ((D_Cm_cg_t_D_alpha_t) * (delta*tau2) * (Wing_Area / X_Section) .* (C_L_u *
57.3))';

Cl_w_cg = Moments_w_cg_u(1,:) ./ (q_Corrected' .* (Wing_Area * Span*12));
Cm_w_cg_u = Moments_w_cg_u(2,:) ./ (q_Corrected' .* (Wing_Area * c_bar*12));
Cn_w_cg = Moments_w_cg_u(3,:) ./ (q_Corrected' .* (Wing_Area * Span*12));

Cm_w_cg_corrected = Cm_w_cg_u %'-Delta_C_m_cg_t'; %no tail
Corrected_Moment_Coefficients = [Cl_w_cg' Cm_w_cg_corrected' Cn_w_cg'];

%OBTAINING THE MOMENT COEFFICIENTS CORRECTED ABOUT THE CENTER OF THE
%BALANCE

Cl_w_bc = Moments_w_bc(1,:) ./ (q_Corrected' .* (Wing_Area * Span*12));
Cm_w_bc_u = Moments_w_bc(2,:) ./ (q_Corrected' .* (Wing_Area * c_bar*12));
Cn_w_bc = Moments_w_bc(3,:) ./ (q_Corrected' .* (Wing_Area * Span*12));

Cm_w_bc_corrected = Cm_w_bc_u ; %no tail
Corrected_Moment_Coefficients_bc = [Cl_w_bc' Cm_w_bc_corrected' Cn_w_bc'];

```

```

#####
%XII.- OUTPUT VARIABLES FORMATING
#####

alpha = sample_data(:,1);

% fprintf(' Mach Number Reynolds Number Dynamic Pressure(Psf)\r')
% % Flight_Parameters
% fprintf(' \r');
% fprintf(' Loads are in lbf and arranged [D S L] across the top and increments of alpha down the side \r')
% Forces_w'
% fprintf(' \r')
% fprintf(' Moments are in in-lbf and arranged [L M N] down the side and increments of alpha along the
top \r')
% % Moments_w_cg_u
% fprintf(' \r')
% fprintf(' Cl_u Cd_u CY_u \r');
% % Coefficients
% fprintf(' \r')
% fprintf(' Del_CD_w CD_u CD_Corrected \r');
% Compare_CD = [Delta_C_D_w C_D_u' C_D_Corrected]
% fprintf(' \r')
% fprintf(' Del_alpha_w alpha_g alpha_Corrected \r');
% Compare_alpha = [Delta_alpha_w' alpha alpha_Corrected ]
% fprintf(' \r')
% fprintf(' Cl_cg_wind Cm_cg_corrected_w Cn_cg_wind \r');
% % Corrected_Moment_Coefficients
% fprintf(' \r')
% fprintf(' M# Re# q_c Uoo alpha_c C_L C_D_c Cl_cg_w
Cm_cg_c_w Cn_cg_w C_Y \r');
YY=[Flight_Parameters (Wind_Speed_Corrected.*(3600/5280)) alpha_Corrected C_L_u' C_D_Corrected
Corrected_Moment_Coefficients C_Y_u' NF_resolved AF_resolved]
% XX=['M#', 'Re#', 'q_c', 'Uoo', 'alpha_c', 'C_L', 'C_D_c', 'Cl_cg_w', 'Cm_cg_c_w', 'Cn_cg_w', 'C_Y_u'];

% ZZ=[XX; YY];
% wk1write('output.xls',YY,2,1)

% Max_Cl = max(Coefficients(:,1))

% LET US SAVE TOTAL DATA IN A EXTERNAL FILE

dlmwrite('output_killian_origcfg_23APR07_60m_a_n8to15',YY,'t')

```

Appendix C: Aerodynamic Data of the Five Model Configurations

The following data was taken in the AFIT low-speed wind tunnel using the 10lb balance and resolved using the *MATLAB* code found in Appendix B.

Table 36: Original Configuration at 20 mph: Alpha Sweep

| Original Configuration at 20 mph: Alpha Sweep - 17th April 2007, $T_{room} = 71.0^\circ \text{ F}$, $P_{baro} = 14.15 \text{ psi}$, $S = 72.58 \text{ in}^2$, $b = 13.808 \text{ in}$ | | | | | | | | | | |
|--|--------|------------------------------|---------|----------------------------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | $q \text{ (lb/ft}^2\text{)}$ | V (mph) | $\alpha \text{ (}^\circ\text{)}$ | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0253 | 36499 | 0.9123 | 19.47 | -8.41 | -0.190 | 0.015 | -0.4074 | 0.0946 | -0.1412 | -4.44 |
| 0.0253 | 36570 | 0.9158 | 19.51 | -6.29 | -0.149 | 0.012 | -0.3197 | 0.0614 | -0.1261 | -5.54 |
| 0.0257 | 37114 | 0.9433 | 19.80 | -4.16 | -0.096 | 0.012 | -0.2012 | 0.0400 | -0.0952 | -6.06 |
| 0.0253 | 36512 | 0.9129 | 19.48 | -2.03 | -0.040 | 0.014 | -0.0876 | 0.0327 | -0.0714 | -3.24 |
| 0.0250 | 36018 | 0.8884 | 19.21 | 0.02 | 0.020 | 0.016 | 0.0442 | 0.0356 | -0.0576 | 1.76 |
| 0.0253 | 36539 | 0.9143 | 19.49 | 2.14 | 0.073 | 0.016 | 0.1569 | 0.0384 | -0.0354 | 5.40 |
| 0.0254 | 36707 | 0.9227 | 19.58 | 4.27 | 0.129 | 0.013 | 0.2748 | 0.0464 | -0.0139 | 6.47 |
| 0.0261 | 37686 | 0.9726 | 20.10 | 6.30 | 0.167 | 0.011 | 0.3385 | 0.0571 | 0.0125 | 6.92 |
| 0.0255 | 36849 | 0.9298 | 19.66 | 8.43 | 0.219 | 0.004 | 0.4631 | 0.0744 | 0.0388 | 6.25 |
| 0.0248 | 35775 | 0.8765 | 19.08 | 10.55 | 0.251 | -0.001 | 0.5625 | 0.0995 | 0.0500 | 5.86 |
| 0.0247 | 35644 | 0.8700 | 19.01 | 11.61 | 0.268 | -0.003 | 0.6044 | 0.1135 | 0.0647 | 5.55 |
| 0.0253 | 36479 | 0.9113 | 19.46 | 12.66 | 0.287 | -0.006 | 0.6158 | 0.1213 | 0.0719 | 5.13 |
| 0.0255 | 36810 | 0.9279 | 19.64 | 13.61 | 0.293 | -0.004 | 0.6137 | 0.1375 | 0.0485 | 4.56 |
| 0.0250 | 36054 | 0.8902 | 19.23 | 14.66 | 0.285 | -0.001 | 0.6186 | 0.1559 | 0.0556 | 4.19 |
| 0.0251 | 36178 | 0.8963 | 19.30 | 15.69 | 0.276 | 0.003 | 0.5910 | 0.1688 | 0.0617 | 3.73 |

Table 37: Original Configuration at 30 mph: Alpha Sweep

| Original Configuration at 30 mph: Alpha Sweep - 17th April 2007, $T_{room} = 71.0^\circ \text{ F}$, $P_{baro} = 14.15 \text{ psi}$, $S = 72.58 \text{ in}^2$, $b = 13.808 \text{ in}$ | | | | | | | | | | |
|--|--------|------------------------------|---------|----------------------------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | $q \text{ (lb/ft}^2\text{)}$ | V (mph) | $\alpha \text{ (}^\circ\text{)}$ | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0395 | 56773 | 2.2175 | 30.43 | -8.38 | -0.441 | 0.032 | -0.3984 | 0.0896 | -0.1430 | -4.45 |
| 0.0398 | 57241 | 2.2542 | 30.68 | -6.26 | -0.342 | 0.024 | -0.3063 | 0.0559 | -0.1257 | -5.48 |
| 0.0396 | 56928 | 2.2296 | 30.51 | -4.14 | -0.208 | 0.027 | -0.1920 | 0.0375 | -0.1025 | -5.12 |
| 0.0397 | 56976 | 2.2333 | 30.53 | -2.02 | -0.052 | 0.031 | -0.0533 | 0.0270 | -0.0870 | -1.97 |
| 0.0395 | 56777 | 2.2178 | 30.43 | 0.11 | 0.096 | 0.034 | 0.0705 | 0.0268 | -0.0677 | 2.63 |
| 0.0397 | 57034 | 2.2379 | 30.57 | 2.15 | 0.261 | 0.029 | 0.2054 | 0.0317 | -0.0493 | 6.48 |
| 0.0401 | 57621 | 2.2842 | 30.88 | 4.27 | 0.388 | 0.018 | 0.3188 | 0.0387 | -0.0252 | 8.24 |
| 0.0400 | 57478 | 2.2728 | 30.80 | 6.30 | 0.503 | 0.000 | 0.4248 | 0.0468 | 0.0034 | 9.08 |
| 0.0401 | 57640 | 2.2857 | 30.89 | 8.41 | 0.607 | -0.022 | 0.5103 | 0.0576 | 0.0268 | 8.86 |
| 0.0401 | 57563 | 2.2796 | 30.85 | 10.52 | 0.700 | -0.049 | 0.5981 | 0.0726 | 0.0437 | 8.24 |
| 0.0402 | 57797 | 2.2982 | 30.97 | 11.57 | 0.732 | -0.054 | 0.6260 | 0.0872 | 0.0355 | 7.18 |
| 0.0400 | 57530 | 2.2770 | 30.83 | 12.63 | 0.762 | -0.051 | 0.6718 | 0.1034 | 0.0357 | 6.50 |
| 0.0398 | 57245 | 2.2545 | 30.68 | 13.67 | 0.731 | -0.036 | 0.6714 | 0.1251 | 0.0158 | 5.37 |
| 0.0401 | 57583 | 2.2812 | 30.86 | 14.71 | 0.700 | -0.019 | 0.6421 | 0.1374 | 0.0026 | 4.67 |
| 0.0402 | 57729 | 2.2928 | 30.94 | 15.74 | 0.664 | -0.004 | 0.6113 | 0.1552 | -0.0005 | 3.94 |

Table 38: Original Configuration at 40 mph: Alpha Sweep

| Original Configuration at 40 mph: Alpha Sweep - 17th April 2007, $T_{room} = 71.0^{\circ} F$, $P_{baro} = 14.15$ psi, $S = 72.58$ in ² , $b = 13.808$ in | | | | | | | | | | |
|--|--------|-------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb/ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0549 | 78867 | 4.2791 | 42.27 | -8.37 | -0.791 | 0.049 | -0.3754 | 0.0815 | -0.1339 | -4.61 |
| 0.0544 | 78128 | 4.1994 | 41.87 | -6.25 | -0.586 | 0.037 | -0.2815 | 0.0503 | -0.1252 | -5.60 |
| 0.0535 | 76895 | 4.0679 | 41.21 | -4.13 | -0.331 | 0.045 | -0.1619 | 0.0338 | -0.1111 | -4.79 |
| 0.0532 | 76509 | 4.0271 | 41.00 | -2.01 | -0.064 | 0.053 | -0.0410 | 0.0256 | -0.0894 | -1.60 |
| 0.0543 | 78089 | 4.1951 | 41.85 | 0.11 | 0.196 | 0.055 | 0.0842 | 0.0233 | -0.0618 | 3.61 |
| 0.0545 | 78324 | 4.2205 | 41.97 | 2.15 | 0.469 | 0.045 | 0.2121 | 0.0273 | -0.0382 | 7.77 |
| 0.0539 | 77401 | 4.1216 | 41.48 | 4.27 | 0.694 | 0.022 | 0.3212 | 0.0339 | -0.0147 | 9.47 |
| 0.0545 | 78284 | 4.2162 | 41.95 | 6.29 | 0.897 | -0.009 | 0.4052 | 0.0407 | 0.0105 | 9.96 |
| 0.0547 | 78637 | 4.2543 | 42.14 | 8.40 | 1.089 | -0.052 | 0.4966 | 0.0511 | 0.0306 | 9.72 |
| 0.0544 | 78151 | 4.2018 | 41.88 | 10.52 | 1.263 | -0.101 | 0.5962 | 0.0648 | 0.0480 | 9.20 |
| 0.0544 | 78108 | 4.1972 | 41.86 | 11.58 | 1.342 | -0.123 | 0.6420 | 0.0731 | 0.0536 | 8.78 |
| 0.0542 | 77825 | 4.1668 | 41.71 | 12.63 | 1.394 | -0.121 | 0.6771 | 0.0934 | 0.0425 | 7.25 |
| 0.0543 | 78069 | 4.1931 | 41.84 | 13.67 | 1.358 | -0.090 | 0.6796 | 0.1163 | 0.0173 | 5.84 |
| 0.0539 | 77437 | 4.1254 | 41.50 | 14.72 | 1.325 | -0.076 | 0.6779 | 0.1309 | -0.0001 | 5.18 |
| 0.0537 | 77179 | 4.0979 | 41.36 | 15.75 | 1.290 | -0.047 | 0.6434 | 0.1394 | -0.0128 | 4.62 |

Table 39: Original Configuration at 60 mph: Alpha Sweep

| Original Configuration at 60 mph: Alpha Sweep - 23rd April 2007, $T_{room} = 74.2^{\circ} F$, $P_{baro} = 28.9723$ inHg, $S = 72.58$ in ² , $b = 13.808$ in | | | | | | | | | | |
|---|--------|-------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb/ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0825 | 120370 | 9.8340 | 63.64 | -8.36 | -1.762 | 0.088 | -0.3585 | 0.0711 | -0.1470 | -5.04 |
| 0.0824 | 120190 | 9.8043 | 63.54 | -6.24 | -1.238 | 0.060 | -0.2453 | 0.0388 | -0.1330 | -6.32 |
| 0.0823 | 120000 | 9.7731 | 63.44 | -4.12 | -0.649 | 0.085 | -0.1313 | 0.0261 | -0.1105 | -5.03 |
| 0.0820 | 119590 | 9.7068 | 63.23 | -2.01 | -0.073 | 0.103 | -0.0193 | 0.0208 | -0.0850 | -0.93 |
| 0.0822 | 119850 | 9.7493 | 63.36 | 0.11 | 0.434 | 0.102 | 0.0827 | 0.0195 | -0.0543 | 4.24 |
| 0.0822 | 119850 | 9.7488 | 63.36 | 2.14 | 0.970 | 0.082 | 0.1982 | 0.0226 | -0.0259 | 8.77 |
| 0.0818 | 119270 | 9.6548 | 63.06 | 4.27 | 1.527 | 0.031 | 0.3193 | 0.0285 | -0.0040 | 11.20 |
| 0.0827 | 120570 | 9.8663 | 63.74 | 6.29 | 2.020 | -0.044 | 0.4145 | 0.0355 | 0.0163 | 11.68 |
| 0.0829 | 120900 | 9.9207 | 63.92 | 8.41 | 2.481 | -0.143 | 0.5100 | 0.0451 | 0.0349 | 11.31 |
| 0.0822 | 119880 | 9.7538 | 63.38 | 10.52 | 2.870 | -0.255 | 0.6086 | 0.0585 | 0.0483 | 10.40 |
| 0.0824 | 120140 | 9.7952 | 63.51 | 11.58 | 3.041 | -0.313 | 0.6487 | 0.0656 | 0.0526 | 9.89 |
| 0.0826 | 120450 | 9.8468 | 63.68 | 12.63 | 3.186 | -0.370 | 0.6841 | 0.0731 | 0.0550 | 9.36 |
| 0.0828 | 120700 | 9.8880 | 63.81 | 13.68 | 3.233 | -0.349 | 0.7119 | 0.0820 | 0.0544 | 8.68 |
| 0.0822 | 119820 | 9.7442 | 63.35 | 14.73 | 3.234 | -0.357 | 0.7131 | 0.1074 | 0.0306 | 6.64 |
| 0.0820 | 119570 | 9.7031 | 63.21 | 15.77 | 3.115 | -0.267 | 0.7049 | 0.1354 | 0.0067 | 5.21 |

Table 40: +5° Cant Configuration at 20 mph: Alpha Sweep

| +5° Cant Configuration at 20 mph: Alpha Sweep - 17th April 2007, $T_{room} = 71.0^{\circ} F$, $P_{baro} = 14.15$ psi, $S = 72.56$ in ² , $b = 13.806$ in | | | | | | | | | | |
|--|--------|-------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb/ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0252 | 36329 | 0.9038 | 19.38 | -8.40 | -0.175 | 0.040 | -0.3846 | 0.0878 | -0.1391 | -4.38 |
| 0.0250 | 36011 | 0.8881 | 19.21 | -6.28 | -0.135 | 0.026 | -0.3012 | 0.0576 | -0.1278 | -5.22 |
| 0.0254 | 36706 | 0.9226 | 19.58 | -4.15 | -0.086 | 0.017 | -0.1851 | 0.0363 | -0.0934 | -5.10 |
| 0.0260 | 37570 | 0.9666 | 20.04 | -2.02 | -0.029 | 0.014 | -0.0599 | 0.0278 | -0.0633 | -2.15 |
| 0.0253 | 36510 | 0.9128 | 19.48 | 0.02 | 0.030 | 0.015 | 0.0653 | 0.0321 | -0.0534 | 2.03 |
| 0.0250 | 36107 | 0.8928 | 19.26 | 2.16 | 0.085 | 0.017 | 0.1895 | 0.0389 | -0.0371 | 4.88 |
| 0.0254 | 36634 | 0.9190 | 19.54 | 4.28 | 0.137 | 0.022 | 0.2968 | 0.0480 | -0.0126 | 6.18 |
| 0.0257 | 37125 | 0.9439 | 19.80 | 6.31 | 0.181 | 0.029 | 0.3801 | 0.0620 | 0.0147 | 6.13 |
| 0.0255 | 36729 | 0.9238 | 19.59 | 8.44 | 0.233 | 0.037 | 0.5007 | 0.0787 | 0.0444 | 6.37 |
| 0.0256 | 36909 | 0.9329 | 19.69 | 10.55 | 0.261 | 0.045 | 0.5562 | 0.0965 | 0.0547 | 5.77 |
| 0.0258 | 37189 | 0.9471 | 19.84 | 11.51 | 0.280 | 0.052 | 0.5866 | 0.1093 | 0.0622 | 5.37 |
| 0.0259 | 37385 | 0.9571 | 19.94 | 12.57 | 0.294 | 0.059 | 0.6106 | 0.1217 | 0.0651 | 5.02 |
| 0.0253 | 36533 | 0.9140 | 19.49 | 13.62 | 0.292 | 0.066 | 0.6347 | 0.1435 | 0.0495 | 4.42 |
| 0.0246 | 35515 | 0.8637 | 18.95 | 14.67 | 0.284 | 0.072 | 0.6524 | 0.1653 | 0.0551 | 3.95 |
| 0.0251 | 36255 | 0.9001 | 19.34 | 15.70 | 0.277 | 0.079 | 0.6110 | 0.1739 | 0.0610 | 3.51 |

Table 41: +5° Cant Configuration at 30 mph: Alpha Sweep

| +5° Cant Configuration at 30 mph: Alpha Sweep - 17th April 2007, T _{room} = 71.0° F, P _{baro} = 14.15 psi, S = 72.56 in ² , b = 13.806 in | | | | | | | | | | |
|--|--------|-------------------------|---------|--------------|---------|---------|--------------------|--------------------|--------------------|---------|
| Mach (-) | Re (-) | q (lb/ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C _L (-) | C _D (-) | C _m (-) | L/D (-) |
| 0.0402 | 57980 | 2.3021 | 30.93 | -8.39 | -0.417 | 0.095 | -0.3593 | 0.0823 | -0.1261 | -4.37 |
| 0.0398 | 57410 | 2.2570 | 30.62 | -6.27 | -0.317 | 0.059 | -0.2787 | 0.0522 | -0.1147 | -5.34 |
| 0.0400 | 57711 | 2.2807 | 30.78 | -4.14 | -0.182 | 0.041 | -0.1586 | 0.0355 | -0.0920 | -4.47 |
| 0.0406 | 58649 | 2.3555 | 31.29 | -2.01 | -0.047 | 0.033 | -0.0400 | 0.0277 | -0.0700 | -1.45 |
| 0.0410 | 59109 | 2.3926 | 31.53 | 0.03 | 0.116 | 0.033 | 0.0961 | 0.0278 | -0.0563 | 3.46 |
| 0.0408 | 58889 | 2.3748 | 31.41 | 2.17 | 0.276 | 0.038 | 0.2303 | 0.0320 | -0.0379 | 7.20 |
| 0.0404 | 58267 | 2.3249 | 31.08 | 4.30 | 0.409 | 0.047 | 0.3489 | 0.0398 | -0.0135 | 8.77 |
| 0.0401 | 57867 | 2.2931 | 30.87 | 6.34 | 0.520 | 0.056 | 0.4503 | 0.0481 | 0.0140 | 9.35 |
| 0.0398 | 57422 | 2.2579 | 30.63 | 8.46 | 0.622 | 0.067 | 0.5468 | 0.0588 | 0.0395 | 9.30 |
| 0.0394 | 56916 | 2.2183 | 30.36 | 10.58 | 0.715 | 0.082 | 0.6395 | 0.0736 | 0.0612 | 8.69 |
| 0.0401 | 57851 | 2.2919 | 30.86 | 11.53 | 0.740 | 0.096 | 0.6407 | 0.0834 | 0.0548 | 7.69 |
| 0.0409 | 59009 | 2.3845 | 31.48 | 12.58 | 0.770 | 0.120 | 0.6411 | 0.0995 | 0.0415 | 6.44 |
| 0.0411 | 59373 | 2.4140 | 31.67 | 13.61 | 0.742 | 0.140 | 0.6101 | 0.1155 | 0.0213 | 5.28 |
| 0.0403 | 58109 | 2.3123 | 31.00 | 14.65 | 0.699 | 0.161 | 0.6002 | 0.1379 | 0.0271 | 4.35 |
| 0.0404 | 58299 | 2.3274 | 31.10 | 15.68 | 0.651 | 0.178 | 0.5552 | 0.1516 | 0.0417 | 3.66 |

Table 42: +5° Cant Configuration at 40 mph: Alpha Sweep

| +5° Cant Configuration at 40 mph: Alpha Sweep - 17th April 2007, T _{room} = 71.0° F, P _{baro} = 14.15 psi, S = 72.56 in ² , b = 13.806 in | | | | | | | | | | |
|--|--------|-------------------------|---------|--------------|---------|---------|--------------------|--------------------|--------------------|---------|
| Mach (-) | Re (-) | q (lb/ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C _L (-) | C _D (-) | C _m (-) | L/D (-) |
| 0.0542 | 78227 | 4.1906 | 41.73 | -8.39 | -0.745 | 0.162 | -0.3530 | 0.0768 | -0.1266 | -4.59 |
| 0.0543 | 78384 | 4.2075 | 41.81 | -6.27 | -0.541 | 0.097 | -0.2552 | 0.0456 | -0.1114 | -5.60 |
| 0.0542 | 78178 | 4.1853 | 41.70 | -4.14 | -0.288 | 0.068 | -0.1365 | 0.0324 | -0.0929 | -4.22 |
| 0.0544 | 78456 | 4.2151 | 41.85 | -2.00 | -0.017 | 0.053 | -0.0078 | 0.0250 | -0.0734 | -0.31 |
| 0.0546 | 78746 | 4.2464 | 42.01 | 0.04 | 0.247 | 0.054 | 0.1153 | 0.0253 | -0.0474 | 4.55 |
| 0.0546 | 78851 | 4.2577 | 42.06 | 2.17 | 0.498 | 0.060 | 0.2320 | 0.0282 | -0.0202 | 8.24 |
| 0.0553 | 79758 | 4.3563 | 42.55 | 4.29 | 0.734 | 0.074 | 0.3343 | 0.0337 | -0.0028 | 9.91 |
| 0.0549 | 79189 | 4.2943 | 42.24 | 6.33 | 0.927 | 0.090 | 0.4284 | 0.0415 | 0.0209 | 10.33 |
| 0.0543 | 78294 | 4.1978 | 41.76 | 8.45 | 1.120 | 0.111 | 0.5294 | 0.0523 | 0.0424 | 10.12 |
| 0.0548 | 79044 | 4.2785 | 42.16 | 10.56 | 1.287 | 0.134 | 0.5971 | 0.0624 | 0.0577 | 9.58 |
| 0.0548 | 79026 | 4.2767 | 42.16 | 11.53 | 1.363 | 0.150 | 0.6323 | 0.0697 | 0.0627 | 9.07 |
| 0.0552 | 79620 | 4.3411 | 42.47 | 12.58 | 1.409 | 0.189 | 0.6441 | 0.0866 | 0.0484 | 7.44 |
| 0.0550 | 79337 | 4.3103 | 42.32 | 13.62 | 1.392 | 0.234 | 0.6408 | 0.1076 | 0.0217 | 5.96 |
| 0.0547 | 78989 | 4.2726 | 42.14 | 14.66 | 1.351 | 0.265 | 0.6274 | 0.1231 | 0.0157 | 5.10 |
| 0.0549 | 79289 | 4.3052 | 42.30 | 15.69 | 1.297 | 0.306 | 0.5978 | 0.1410 | 0.0146 | 4.24 |

Table 43: +5° Cant Configuration at 60 mph: Alpha Sweep

| +5° Cant Configuration at 60 mph: Alpha Sweep - 23rd April 2007, $T_{room} = 74.8^{\circ} F$, $P_{baro} = 28.9373$ inHg, $S = 72.58$ in ² , $b = 13.808$ in | | | | | | | | | | |
|---|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0811 | 117080 | 9.4124 | 62.62 | -8.39 | -1.666 | 0.337 | -0.3513 | 0.0712 | -0.1326 | -4.94 |
| 0.0809 | 116790 | 9.3667 | 62.47 | -6.26 | -1.139 | 0.181 | -0.2413 | 0.0384 | -0.1184 | -6.28 |
| 0.0807 | 116570 | 9.3302 | 62.35 | -4.13 | -0.525 | 0.125 | -0.1117 | 0.0266 | -0.0992 | -4.20 |
| 0.0807 | 116640 | 9.3413 | 62.39 | -2.00 | 0.028 | 0.103 | 0.0059 | 0.0219 | -0.0735 | 0.27 |
| 0.0806 | 116490 | 9.3178 | 62.31 | 0.13 | 0.525 | 0.102 | 0.1117 | 0.0218 | -0.0448 | 5.12 |
| 0.0807 | 116500 | 9.3194 | 62.31 | 2.17 | 1.053 | 0.118 | 0.2243 | 0.0252 | -0.0148 | 8.92 |
| 0.0812 | 117280 | 9.4444 | 62.73 | 4.30 | 1.623 | 0.145 | 0.3410 | 0.0306 | 0.0069 | 11.16 |
| 0.0814 | 117610 | 9.4984 | 62.91 | 6.33 | 2.099 | 0.179 | 0.4387 | 0.0374 | 0.0283 | 11.72 |
| 0.0819 | 118230 | 9.5985 | 63.24 | 8.45 | 2.552 | 0.223 | 0.5277 | 0.0462 | 0.0468 | 11.43 |
| 0.0819 | 118240 | 9.5993 | 63.24 | 10.57 | 2.937 | 0.277 | 0.6072 | 0.0572 | 0.0597 | 10.61 |
| 0.0811 | 117090 | 9.4138 | 62.63 | 11.63 | 3.105 | 0.309 | 0.6546 | 0.0650 | 0.0642 | 10.06 |
| 0.0817 | 118050 | 9.5686 | 63.14 | 12.68 | 3.251 | 0.339 | 0.6743 | 0.0703 | 0.0653 | 9.60 |
| 0.0821 | 118550 | 9.6503 | 63.41 | 13.72 | 3.313 | 0.428 | 0.6814 | 0.0880 | 0.0502 | 7.75 |
| 0.0812 | 117270 | 9.4429 | 62.72 | 14.77 | 3.263 | 0.528 | 0.6858 | 0.1110 | 0.0311 | 6.18 |
| 0.0810 | 117040 | 9.4066 | 62.60 | 15.80 | 3.159 | 0.617 | 0.6664 | 0.1301 | 0.0187 | 5.12 |

Table 44: -5° Cant Configuration at 20 mph: Alpha Sweep

| -5° Cant Configuration at 20 mph: Alpha Sweep - 18th April 2007, $T_{room} = 69.9^{\circ} F$, $P_{baro} = 14.10$ psi, $S = 72.56$ in ² , $b = 13.806$ in | | | | | | | | | | |
|--|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0254 | 36561 | 0.9167 | 19.53 | -8.41 | -0.194 | 0.042 | -0.4204 | 0.0910 | -0.1418 | -4.62 |
| 0.0259 | 37305 | 0.9544 | 19.93 | -6.29 | -0.157 | 0.028 | -0.3271 | 0.0587 | -0.1154 | -5.57 |
| 0.0255 | 36702 | 0.9238 | 19.61 | -4.17 | -0.108 | 0.018 | -0.2313 | 0.0397 | -0.0955 | -5.82 |
| 0.0245 | 35271 | 0.8532 | 18.84 | -2.05 | -0.060 | 0.014 | -0.1393 | 0.0330 | -0.0734 | -4.22 |
| 0.0246 | 35446 | 0.8617 | 18.94 | 0.00 | -0.001 | 0.014 | -0.0027 | 0.0324 | -0.0525 | -0.08 |
| 0.0245 | 35204 | 0.8499 | 18.81 | 2.13 | 0.056 | 0.016 | 0.1298 | 0.0374 | -0.0387 | 3.47 |
| 0.0246 | 35349 | 0.8569 | 18.88 | 4.27 | 0.111 | 0.019 | 0.2562 | 0.0442 | -0.0180 | 5.80 |
| 0.0254 | 36546 | 0.9160 | 19.52 | 6.30 | 0.159 | 0.026 | 0.3437 | 0.0556 | 0.0087 | 6.18 |
| 0.0262 | 37711 | 0.9753 | 20.15 | 8.42 | 0.213 | 0.032 | 0.4335 | 0.0644 | 0.0392 | 6.73 |
| 0.0253 | 36456 | 0.9114 | 19.48 | 10.46 | 0.249 | 0.040 | 0.5422 | 0.0878 | 0.0537 | 6.18 |
| 0.0249 | 35828 | 0.8803 | 19.14 | 11.52 | 0.266 | 0.047 | 0.5987 | 0.1053 | 0.0577 | 5.68 |
| 0.0247 | 35506 | 0.8646 | 18.97 | 12.57 | 0.273 | 0.054 | 0.6256 | 0.1248 | 0.0494 | 5.01 |
| 0.0252 | 36322 | 0.9048 | 19.40 | 13.60 | 0.271 | 0.061 | 0.5937 | 0.1331 | 0.0333 | 4.46 |
| 0.0253 | 36406 | 0.9090 | 19.45 | 14.64 | 0.265 | 0.067 | 0.5796 | 0.1466 | 0.0368 | 3.95 |
| 0.0249 | 35776 | 0.8778 | 19.11 | 15.68 | 0.250 | 0.073 | 0.5653 | 0.1657 | 0.0516 | 3.41 |

Table 45: -5° Cant Configuration at 30 mph: Alpha Sweep

| -5° Cant Configuration at 30 mph: Alpha Sweep - 18th April 2007, $T_{room} = 69.9^{\circ} F$, $P_{baro} = 14.10$ psi, $S = 72.56$ in ² , $b = 13.806$ in | | | | | | | | | | |
|--|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0396 | 57000 | 2.2282 | 30.45 | -8.41 | -0.462 | 0.094 | -0.4115 | 0.0840 | -0.1367 | -4.90 |
| 0.0398 | 57259 | 2.2485 | 30.59 | -6.29 | -0.374 | 0.062 | -0.3302 | 0.0545 | -0.1162 | -6.06 |
| 0.0401 | 57786 | 2.2900 | 30.87 | -4.17 | -0.265 | 0.044 | -0.2297 | 0.0380 | -0.0863 | -6.05 |
| 0.0406 | 58408 | 2.3396 | 31.20 | -2.04 | -0.125 | 0.034 | -0.1060 | 0.0286 | -0.0677 | -3.71 |
| 0.0406 | 58378 | 2.3372 | 31.19 | 0.01 | 0.027 | 0.032 | 0.0231 | 0.0273 | -0.0532 | 0.85 |
| 0.0399 | 57460 | 2.2643 | 30.70 | 2.15 | 0.186 | 0.035 | 0.1627 | 0.0306 | -0.0392 | 5.32 |
| 0.0397 | 57095 | 2.2356 | 30.50 | 4.28 | 0.330 | 0.042 | 0.2929 | 0.0374 | -0.0149 | 7.83 |
| 0.0394 | 56668 | 2.2023 | 30.27 | 6.32 | 0.448 | 0.050 | 0.4037 | 0.0452 | 0.0129 | 8.93 |
| 0.0390 | 56171 | 2.1639 | 30.01 | 8.44 | 0.551 | 0.059 | 0.5054 | 0.0540 | 0.0415 | 9.36 |
| 0.0393 | 56513 | 2.1903 | 30.19 | 10.56 | 0.640 | 0.073 | 0.5801 | 0.0664 | 0.0592 | 8.73 |
| 0.0404 | 58088 | 2.3141 | 31.03 | 11.60 | 0.669 | 0.090 | 0.5738 | 0.0773 | 0.0485 | 7.42 |
| 0.0407 | 58534 | 2.3497 | 31.27 | 12.64 | 0.677 | 0.112 | 0.5720 | 0.0950 | 0.0261 | 6.02 |
| 0.0402 | 57876 | 2.2971 | 30.92 | 13.68 | 0.666 | 0.127 | 0.5751 | 0.1093 | 0.0191 | 5.26 |
| 0.0400 | 57563 | 2.2724 | 30.75 | 14.73 | 0.650 | 0.146 | 0.5679 | 0.1277 | 0.0150 | 4.45 |
| 0.0400 | 57531 | 2.2698 | 30.73 | 15.76 | 0.614 | 0.166 | 0.5370 | 0.1448 | 0.0215 | 3.71 |

Table 46: -5° Cant Configuration at 40 mph: Alpha Sweep

| -5° Cant Configuration at 40 mph: Alpha Sweep - 18th April 2007, T _{room} = 69.9° F, P _{hvac} = 14.10 psi, S = 72.56 in ² , b = 13.806 in | | | | | | | | | | |
|--|--------|---------------------------------------|---------|-------|---------|---------|--------------------|--------------------|--------------------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C _L (-) | C _D (-) | C _m (-) | L/D (-) |
| 0.0540 | 77783 | 4.1492 | 41.55 | -8.40 | -0.839 | 0.159 | -0.4011 | 0.0762 | -0.1343 | -5.27 |
| 0.0542 | 78093 | 4.1824 | 41.72 | -6.29 | -0.662 | 0.100 | -0.3141 | 0.0474 | -0.1116 | -6.63 |
| 0.0537 | 77340 | 4.1021 | 41.32 | -4.17 | -0.450 | 0.072 | -0.2179 | 0.0349 | -0.0890 | -6.25 |
| 0.0535 | 77020 | 4.0682 | 41.15 | -2.03 | -0.180 | 0.054 | -0.0878 | 0.0263 | -0.0729 | -3.34 |
| 0.0536 | 77216 | 4.0889 | 41.25 | 0.10 | 0.089 | 0.050 | 0.0431 | 0.0241 | -0.0499 | 1.79 |
| 0.0538 | 77455 | 4.1143 | 41.38 | 2.15 | 0.369 | 0.056 | 0.1779 | 0.0268 | -0.0235 | 6.63 |
| 0.0541 | 77861 | 4.1575 | 41.59 | 4.28 | 0.610 | 0.065 | 0.2912 | 0.0310 | -0.0029 | 9.39 |
| 0.0544 | 78326 | 4.2074 | 41.84 | 6.31 | 0.808 | 0.078 | 0.3811 | 0.0367 | 0.0217 | 10.40 |
| 0.0548 | 78961 | 4.2758 | 42.18 | 8.43 | 1.000 | 0.096 | 0.4643 | 0.0445 | 0.0423 | 10.43 |
| 0.0545 | 78470 | 4.2228 | 41.92 | 10.55 | 1.167 | 0.119 | 0.5486 | 0.0560 | 0.0583 | 9.79 |
| 0.0545 | 78528 | 4.2291 | 41.95 | 11.60 | 1.230 | 0.142 | 0.5772 | 0.0668 | 0.0578 | 8.64 |
| 0.0548 | 78827 | 4.2614 | 42.11 | 12.64 | 1.253 | 0.192 | 0.5837 | 0.0895 | 0.0324 | 6.52 |
| 0.0554 | 79717 | 4.3581 | 42.59 | 13.68 | 1.229 | 0.217 | 0.5597 | 0.0990 | 0.0188 | 5.66 |
| 0.0546 | 78550 | 4.2314 | 41.96 | 14.73 | 1.208 | 0.246 | 0.5665 | 0.1154 | 0.0162 | 4.91 |
| 0.0543 | 78124 | 4.1857 | 41.74 | 15.76 | 1.155 | 0.288 | 0.5478 | 0.1364 | 0.0096 | 4.02 |

Table 47: -5° Cant Configuration at 60 mph: Alpha Sweep

| -5° Cant Configuration at 60 mph: Alpha Sweep - 23rd April 2007, T _{room} = 74.8° F, P _{hvac} = 28.9373 inHg, S = 72.58 in ² , b = 13.808 in | | | | | | | | | | |
|---|--------|---------------------------------------|---------|-------|---------|---------|--------------------|--------------------|--------------------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C _L (-) | C _D (-) | C _m (-) | L/D (-) |
| 0.0813 | 117480 | 9.4773 | 62.84 | -8.40 | -1.907 | 0.320 | -0.3994 | 0.0670 | -0.1361 | -5.97 |
| 0.0816 | 117900 | 9.5446 | 63.06 | -6.28 | -1.447 | 0.192 | -0.3008 | 0.0400 | -0.1123 | -7.53 |
| 0.0816 | 117860 | 9.5383 | 63.04 | -4.15 | -0.855 | 0.134 | -0.1780 | 0.0278 | -0.0932 | -6.40 |
| 0.0812 | 117240 | 9.4386 | 62.71 | -2.02 | -0.271 | 0.104 | -0.0570 | 0.0218 | -0.0710 | -2.62 |
| 0.0809 | 116920 | 9.3871 | 62.54 | 0.11 | 0.248 | 0.095 | 0.0524 | 0.0201 | -0.0439 | 2.61 |
| 0.0818 | 118110 | 9.5787 | 63.17 | 2.15 | 0.805 | 0.106 | 0.1667 | 0.0219 | -0.0135 | 7.62 |
| 0.0818 | 118200 | 9.5927 | 63.22 | 4.28 | 1.384 | 0.127 | 0.2863 | 0.0262 | 0.0090 | 10.93 |
| 0.0813 | 117460 | 9.4732 | 62.83 | 6.40 | 1.883 | 0.157 | 0.3945 | 0.0329 | 0.0286 | 11.98 |
| 0.0815 | 117680 | 9.5093 | 62.95 | 8.43 | 2.320 | 0.194 | 0.4842 | 0.0405 | 0.0466 | 11.95 |
| 0.0816 | 117860 | 9.5384 | 63.04 | 10.55 | 2.684 | 0.242 | 0.5585 | 0.0503 | 0.0610 | 11.11 |
| 0.0817 | 117980 | 9.5580 | 63.11 | 11.60 | 2.851 | 0.271 | 0.5920 | 0.0563 | 0.0658 | 10.52 |
| 0.0826 | 119370 | 9.7840 | 63.85 | 12.65 | 2.975 | 0.333 | 0.6034 | 0.0676 | 0.0614 | 8.93 |
| 0.0821 | 118580 | 9.6547 | 63.42 | 13.69 | 2.911 | 0.468 | 0.5983 | 0.0962 | 0.0294 | 6.22 |
| 0.0813 | 117460 | 9.4735 | 62.83 | 14.74 | 2.896 | 0.521 | 0.6066 | 0.1092 | 0.0228 | 5.56 |
| 0.0814 | 117610 | 9.4977 | 62.91 | 15.78 | 2.859 | 0.573 | 0.5973 | 0.1198 | 0.0219 | 4.99 |

Table 48: Endplate Configuration at 20 mph: Alpha Sweep

| Endplate Configuration at 20 mph: Alpha Sweep - 20th April 2007, T _{room} = 72.6° F, P _{hvac} = 29.1564 inHg, S = 58.33 in ² , b = 11.5 in | | | | | | | | | | |
|---|--------|---------------------------------------|---------|-------|---------|---------|--------------------|--------------------|--------------------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C _L (-) | C _D (-) | C _m (-) | L/D (-) |
| 0.0253 | 36869 | 0.9226 | 19.49 | -8.38 | -0.157 | 0.038 | -0.4210 | 0.1007 | -0.1516 | -4.18 |
| 0.0253 | 36879 | 0.9231 | 19.50 | -6.27 | -0.122 | 0.025 | -0.3265 | 0.0660 | -0.1347 | -4.95 |
| 0.0251 | 36602 | 0.9093 | 19.35 | -4.15 | -0.078 | 0.016 | -0.2123 | 0.0446 | -0.1073 | -4.76 |
| 0.0248 | 36158 | 0.8873 | 19.12 | -2.03 | -0.033 | 0.013 | -0.0905 | 0.0350 | -0.0763 | -2.59 |
| 0.0249 | 36320 | 0.8953 | 19.20 | 0.10 | 0.016 | 0.012 | 0.0449 | 0.0344 | -0.0560 | 1.31 |
| 0.0254 | 37073 | 0.9328 | 19.60 | 2.14 | 0.067 | 0.015 | 0.1781 | 0.0405 | -0.0362 | 4.40 |
| 0.0255 | 37246 | 0.9415 | 19.69 | 4.26 | 0.109 | 0.019 | 0.2861 | 0.0492 | -0.0133 | 5.82 |
| 0.0250 | 36451 | 0.9018 | 19.27 | 6.38 | 0.153 | 0.024 | 0.4194 | 0.0658 | 0.0100 | 6.37 |
| 0.0250 | 36488 | 0.9036 | 19.29 | 8.41 | 0.192 | 0.031 | 0.5258 | 0.0852 | 0.0423 | 6.17 |
| 0.0248 | 36164 | 0.8876 | 19.12 | 10.53 | 0.225 | 0.038 | 0.6246 | 0.1058 | 0.0616 | 5.90 |
| 0.0251 | 36641 | 0.9112 | 19.37 | 11.58 | 0.238 | 0.044 | 0.6454 | 0.1197 | 0.0592 | 5.39 |
| 0.0250 | 36434 | 0.9009 | 19.26 | 12.63 | 0.252 | 0.050 | 0.6908 | 0.1376 | 0.0660 | 5.02 |
| 0.0247 | 36088 | 0.8839 | 19.08 | 13.68 | 0.254 | 0.057 | 0.7107 | 0.1593 | 0.0527 | 4.46 |
| 0.0250 | 36471 | 0.9027 | 19.28 | 14.72 | 0.252 | 0.063 | 0.6896 | 0.1718 | 0.0378 | 4.01 |
| 0.0251 | 36585 | 0.9084 | 19.34 | 15.76 | 0.245 | 0.069 | 0.6654 | 0.1862 | 0.0412 | 3.57 |

Table 49: Endplate Configuration at 30 mph: Alpha Sweep

| Endplate Configuration at 30 mph: Alpha Sweep - 20th April 2007, $T_{room} = 72.6^{\circ} F$, $P_{baro} = 29.1564$ inHg, $S = 58.33$ in ² , $b = 11.5$ in | | | | | | | | | | |
|---|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0400 | 58326 | 2.3088 | 30.84 | -8.38 | -0.371 | 0.086 | -0.3970 | 0.0924 | -0.1397 | -4.30 |
| 0.0401 | 58493 | 2.3221 | 30.92 | -6.26 | -0.290 | 0.056 | -0.3082 | 0.0591 | -0.1242 | -5.21 |
| 0.0405 | 59020 | 2.3641 | 31.20 | -4.14 | -0.174 | 0.038 | -0.1813 | 0.0398 | -0.0992 | -4.56 |
| 0.0405 | 59011 | 2.3634 | 31.20 | -2.01 | -0.041 | 0.028 | -0.0433 | 0.0297 | -0.0847 | -1.46 |
| 0.0403 | 58813 | 2.3475 | 31.09 | 0.11 | 0.076 | 0.028 | 0.0799 | 0.0296 | -0.0631 | 2.70 |
| 0.0401 | 58508 | 2.3233 | 30.93 | 2.15 | 0.205 | 0.034 | 0.2184 | 0.0359 | -0.0430 | 6.08 |
| 0.0399 | 58140 | 2.2942 | 30.74 | 4.27 | 0.320 | 0.041 | 0.3446 | 0.0441 | -0.0171 | 7.81 |
| 0.0401 | 58473 | 2.3205 | 30.91 | 6.39 | 0.419 | 0.048 | 0.4453 | 0.0513 | 0.0131 | 8.68 |
| 0.0406 | 59247 | 2.3823 | 31.32 | 8.41 | 0.503 | 0.058 | 0.5218 | 0.0601 | 0.0399 | 8.68 |
| 0.0407 | 59428 | 2.3969 | 31.42 | 10.52 | 0.587 | 0.071 | 0.6051 | 0.0729 | 0.0602 | 8.30 |
| 0.0409 | 59599 | 2.4108 | 31.51 | 11.57 | 0.617 | 0.084 | 0.6321 | 0.0863 | 0.0544 | 7.32 |
| 0.0401 | 58525 | 2.3246 | 30.94 | 12.63 | 0.650 | 0.101 | 0.6909 | 0.1076 | 0.0487 | 6.42 |
| 0.0401 | 58549 | 2.3266 | 30.95 | 13.67 | 0.633 | 0.120 | 0.6720 | 0.1270 | 0.0210 | 5.29 |
| 0.0407 | 59368 | 2.3921 | 31.39 | 14.70 | 0.593 | 0.136 | 0.6121 | 0.1408 | 0.0144 | 4.35 |
| 0.0406 | 59181 | 2.3770 | 31.29 | 15.74 | 0.584 | 0.153 | 0.6065 | 0.1592 | 0.0069 | 3.81 |

Table 50: Endplate Configuration at 40 mph: Alpha Sweep

| Endplate Configuration at 40 mph: Alpha Sweep - 20th April 2007, $T_{room} = 72.6^{\circ} F$, $P_{baro} = 29.1564$ inHg, $S = 58.33$ in ² , $b = 11.5$ in | | | | | | | | | | |
|---|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0548 | 79936 | 4.3367 | 42.26 | -8.29 | -0.676 | 0.151 | -0.3850 | 0.0861 | -0.1333 | -4.47 |
| 0.0543 | 79240 | 4.2615 | 41.89 | -6.26 | -0.500 | 0.095 | -0.2897 | 0.0549 | -0.1259 | -5.28 |
| 0.0542 | 79064 | 4.2426 | 41.80 | -4.13 | -0.278 | 0.065 | -0.1620 | 0.0376 | -0.1069 | -4.31 |
| 0.0545 | 79517 | 4.2913 | 42.04 | -2.01 | -0.056 | 0.050 | -0.0323 | 0.0289 | -0.0852 | -1.12 |
| 0.0547 | 79748 | 4.3163 | 42.16 | 0.11 | 0.159 | 0.049 | 0.0909 | 0.0278 | -0.0578 | 3.27 |
| 0.0542 | 79018 | 4.2376 | 41.78 | 2.15 | 0.375 | 0.056 | 0.2183 | 0.0325 | -0.0288 | 6.72 |
| 0.0542 | 79040 | 4.2400 | 41.79 | 4.27 | 0.573 | 0.067 | 0.3339 | 0.0388 | -0.0076 | 8.61 |
| 0.0541 | 78871 | 4.2219 | 41.70 | 6.38 | 0.734 | 0.080 | 0.4294 | 0.0467 | 0.0199 | 9.19 |
| 0.0544 | 79404 | 4.2791 | 41.98 | 8.41 | 0.901 | 0.098 | 0.5198 | 0.0565 | 0.0444 | 9.20 |
| 0.0547 | 79802 | 4.3222 | 42.19 | 10.52 | 1.062 | 0.119 | 0.6064 | 0.0682 | 0.0638 | 8.89 |
| 0.0542 | 79059 | 4.2421 | 41.80 | 11.58 | 1.135 | 0.134 | 0.6607 | 0.0780 | 0.0705 | 8.47 |
| 0.0541 | 78910 | 4.2261 | 41.72 | 12.64 | 1.186 | 0.169 | 0.6928 | 0.0985 | 0.0564 | 7.03 |
| 0.0547 | 79717 | 4.3129 | 42.14 | 13.67 | 1.184 | 0.208 | 0.6780 | 0.1188 | 0.0240 | 5.71 |
| 0.0545 | 79457 | 4.2849 | 42.01 | 14.71 | 1.143 | 0.227 | 0.6583 | 0.1307 | 0.0059 | 5.04 |
| 0.0539 | 78673 | 4.2008 | 41.59 | 15.75 | 1.100 | 0.256 | 0.6463 | 0.1506 | -0.0011 | 4.29 |

Table 51: Endplate Configuration at 60 mph: Alpha Sweep

| Endplate Configuration at 60 mph: Alpha Sweep - 20th April 2007, $T_{room} = 72.6^{\circ} F$, $P_{baro} = 29.1564$ inHg, $S = 58.33$ in ² , $b = 11.5$ in | | | | | | | | | | |
|---|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0823 | 120030 | 9.7777 | 63.46 | -8.28 | -1.506 | 0.320 | -0.3802 | 0.0809 | -0.1465 | -4.70 |
| 0.0820 | 119580 | 9.7044 | 63.22 | -6.25 | -1.041 | 0.183 | -0.2649 | 0.0466 | -0.1364 | -5.68 |
| 0.0815 | 118820 | 9.5824 | 62.82 | -4.13 | -0.566 | 0.128 | -0.1459 | 0.0330 | -0.1138 | -4.42 |
| 0.0817 | 119120 | 9.6297 | 62.97 | -2.01 | -0.109 | 0.105 | -0.0280 | 0.0269 | -0.0850 | -1.04 |
| 0.0822 | 119860 | 9.7505 | 63.37 | 0.11 | 0.308 | 0.099 | 0.0780 | 0.0251 | -0.0514 | 3.11 |
| 0.0824 | 120210 | 9.8075 | 63.55 | 2.14 | 0.753 | 0.110 | 0.1896 | 0.0276 | -0.0185 | 6.87 |
| 0.0824 | 120150 | 9.7969 | 63.52 | 4.26 | 1.250 | 0.132 | 0.3149 | 0.0333 | 0.0049 | 9.46 |
| 0.0817 | 119180 | 9.6401 | 63.01 | 6.39 | 1.688 | 0.164 | 0.4322 | 0.0420 | 0.0260 | 10.29 |
| 0.0820 | 119560 | 9.7013 | 63.21 | 8.41 | 2.075 | 0.200 | 0.5281 | 0.0508 | 0.0491 | 10.40 |
| 0.0821 | 119660 | 9.7181 | 63.26 | 10.53 | 2.424 | 0.247 | 0.6157 | 0.0629 | 0.0644 | 9.79 |
| 0.0820 | 119660 | 9.7175 | 63.26 | 11.58 | 2.589 | 0.275 | 0.6578 | 0.0698 | 0.0698 | 9.42 |
| 0.0823 | 119960 | 9.7670 | 63.42 | 12.64 | 2.739 | 0.305 | 0.6924 | 0.0772 | 0.0724 | 8.97 |
| 0.0821 | 119690 | 9.7234 | 63.28 | 13.69 | 2.868 | 0.338 | 0.7281 | 0.0859 | 0.0727 | 8.48 |
| 0.0827 | 120560 | 9.8640 | 63.74 | 14.72 | 2.800 | 0.438 | 0.7009 | 0.1096 | 0.0378 | 6.40 |
| 0.0820 | 119550 | 9.7005 | 63.21 | 15.77 | 2.746 | 0.535 | 0.6989 | 0.1363 | 0.0130 | 5.13 |

Table 52: No Flow Guide Configuration at 20 mph: Alpha Sweep

| No Flow Guide Configuration at 20 mph: Alpha Sweep - 18th April 2007, $T_{room} = 71.2^{\circ} F$, $P_{baro} = 14.09$ psi, $S = 58.02$ in ² , $b = 11.38$ in | | | | | | | | | | |
|--|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0244 | 35066 | 0.8460 | 18.79 | -8.39 | -0.150 | 0.034 | -0.4396 | 0.0989 | -0.1624 | -4.44 |
| 0.0248 | 35700 | 0.8768 | 19.13 | -6.27 | -0.117 | 0.021 | -0.3300 | 0.0596 | -0.1385 | -5.54 |
| 0.0250 | 35934 | 0.8883 | 19.26 | -4.15 | -0.077 | 0.013 | -0.2144 | 0.0354 | -0.1037 | -6.05 |
| 0.0245 | 35262 | 0.8554 | 18.90 | -2.03 | -0.031 | 0.009 | -0.0889 | 0.0274 | -0.0759 | -3.25 |
| 0.0246 | 35349 | 0.8597 | 18.94 | 0.10 | 0.016 | 0.009 | 0.0458 | 0.0260 | -0.0566 | 1.76 |
| 0.0248 | 35673 | 0.8755 | 19.12 | 2.14 | 0.065 | 0.012 | 0.1832 | 0.0339 | -0.0405 | 5.40 |
| 0.0251 | 36012 | 0.8922 | 19.30 | 4.25 | 0.100 | 0.016 | 0.2795 | 0.0432 | -0.0142 | 6.47 |
| 0.0250 | 35856 | 0.8845 | 19.22 | 6.29 | 0.146 | 0.021 | 0.4085 | 0.0590 | 0.0044 | 6.93 |
| 0.0249 | 35755 | 0.8795 | 19.16 | 8.41 | 0.178 | 0.028 | 0.5026 | 0.0804 | 0.0250 | 6.25 |
| 0.0250 | 35881 | 0.8857 | 19.23 | 10.52 | 0.213 | 0.036 | 0.5960 | 0.1017 | 0.0377 | 5.86 |
| 0.0248 | 35638 | 0.8738 | 19.10 | 11.58 | 0.229 | 0.041 | 0.6516 | 0.1173 | 0.0486 | 5.55 |
| 0.0252 | 36174 | 0.9002 | 19.39 | 12.63 | 0.244 | 0.048 | 0.6719 | 0.1311 | 0.0523 | 5.13 |
| 0.0250 | 35963 | 0.8898 | 19.27 | 13.67 | 0.245 | 0.054 | 0.6845 | 0.1502 | 0.0389 | 4.56 |
| 0.0246 | 35414 | 0.8628 | 18.98 | 14.73 | 0.249 | 0.059 | 0.7162 | 0.1711 | 0.0304 | 4.19 |
| 0.0246 | 35418 | 0.8630 | 18.98 | 15.76 | 0.241 | 0.065 | 0.6930 | 0.1856 | 0.0331 | 3.74 |

Table 53: No Flow Guide Configuration at 30 mph: Alpha Sweep

| No Flow Guide Configuration at 30 mph: Alpha Sweep - 18th April 2007, $T_{room} = 71.2^{\circ} F$, $P_{baro} = 14.09$ psi, $S = 58.02$ in ² , $b = 11.38$ in | | | | | | | | | | |
|--|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0395 | 56773 | 2.2175 | 30.43 | -8.38 | -0.356 | 0.080 | -0.3984 | 0.0896 | -0.1430 | -4.45 |
| 0.0398 | 57241 | 2.2542 | 30.68 | -6.26 | -0.278 | 0.051 | -0.3063 | 0.0559 | -0.1257 | -5.48 |
| 0.0396 | 56928 | 2.2296 | 30.51 | -4.14 | -0.172 | 0.034 | -0.1920 | 0.0375 | -0.1025 | -5.12 |
| 0.0397 | 56976 | 2.2333 | 30.53 | -2.02 | -0.048 | 0.024 | -0.0533 | 0.0270 | -0.0870 | -1.97 |
| 0.0395 | 56777 | 2.2178 | 30.43 | 0.11 | 0.063 | 0.024 | 0.0705 | 0.0268 | -0.0677 | 2.63 |
| 0.0397 | 57034 | 2.2379 | 30.57 | 2.15 | 0.185 | 0.029 | 0.2054 | 0.0317 | -0.0493 | 6.47 |
| 0.0401 | 57621 | 2.2842 | 30.88 | 4.27 | 0.293 | 0.036 | 0.3188 | 0.0387 | -0.0252 | 8.24 |
| 0.0400 | 57478 | 2.2728 | 30.80 | 6.30 | 0.389 | 0.043 | 0.4248 | 0.0468 | 0.0034 | 9.07 |
| 0.0401 | 57640 | 2.2857 | 30.89 | 8.41 | 0.470 | 0.053 | 0.5103 | 0.0576 | 0.0268 | 8.85 |
| 0.0401 | 57563 | 2.2796 | 30.85 | 10.52 | 0.549 | 0.067 | 0.5981 | 0.0726 | 0.0437 | 8.24 |
| 0.0402 | 57797 | 2.2982 | 30.97 | 11.57 | 0.580 | 0.081 | 0.6260 | 0.0872 | 0.0355 | 7.18 |
| 0.0400 | 57530 | 2.2770 | 30.83 | 12.63 | 0.616 | 0.095 | 0.6718 | 0.1034 | 0.0357 | 6.50 |
| 0.0398 | 57245 | 2.2545 | 30.68 | 13.67 | 0.610 | 0.114 | 0.6714 | 0.1251 | 0.0158 | 5.37 |
| 0.0401 | 57583 | 2.2812 | 30.86 | 14.71 | 0.590 | 0.126 | 0.6421 | 0.1374 | 0.0026 | 4.67 |
| 0.0402 | 57729 | 2.2928 | 30.94 | 15.74 | 0.565 | 0.143 | 0.6113 | 0.1552 | -0.0005 | 3.94 |

Table 54: No Flow Guide Configuration at 40 mph: Alpha Sweep

| No Flow Guide Configuration at 40 mph: Alpha Sweep - 18th April 2007, $T_{room} = 71.2^{\circ} F$, $P_{baro} = 14.09$ psi, $S = 58.02$ in ² , $b = 11.38$ in | | | | | | | | | | |
|--|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0549 | 78867 | 4.2791 | 42.27 | -8.37 | -0.647 | 0.141 | -0.3754 | 0.0815 | -0.1339 | -4.61 |
| 0.0544 | 78128 | 4.1994 | 41.87 | -6.25 | -0.476 | 0.085 | -0.2815 | 0.0503 | -0.1252 | -5.60 |
| 0.0535 | 76895 | 4.0679 | 41.21 | -4.13 | -0.265 | 0.055 | -0.1619 | 0.0338 | -0.1111 | -4.79 |
| 0.0532 | 76509 | 4.0271 | 41.00 | -2.01 | -0.066 | 0.042 | -0.0410 | 0.0256 | -0.0894 | -1.60 |
| 0.0543 | 78089 | 4.1951 | 41.85 | 0.11 | 0.142 | 0.039 | 0.0842 | 0.0233 | -0.0618 | 3.62 |
| 0.0545 | 78324 | 4.2205 | 41.97 | 2.15 | 0.361 | 0.047 | 0.2121 | 0.0273 | -0.0382 | 7.76 |
| 0.0539 | 77401 | 4.1216 | 41.48 | 4.27 | 0.533 | 0.056 | 0.3212 | 0.0339 | -0.0147 | 9.46 |
| 0.0545 | 78284 | 4.2162 | 41.95 | 6.29 | 0.688 | 0.069 | 0.4052 | 0.0407 | 0.0105 | 9.96 |
| 0.0547 | 78637 | 4.2543 | 42.14 | 8.40 | 0.851 | 0.088 | 0.4966 | 0.0511 | 0.0306 | 9.71 |
| 0.0544 | 78151 | 4.2018 | 41.88 | 10.52 | 1.009 | 0.110 | 0.5962 | 0.0648 | 0.0480 | 9.20 |
| 0.0544 | 78108 | 4.1972 | 41.86 | 11.58 | 1.086 | 0.124 | 0.6420 | 0.0731 | 0.0536 | 8.78 |
| 0.0542 | 77825 | 4.1668 | 41.71 | 12.63 | 1.137 | 0.157 | 0.6771 | 0.0934 | 0.0425 | 7.25 |
| 0.0543 | 78069 | 4.1931 | 41.84 | 13.67 | 1.148 | 0.196 | 0.6796 | 0.1163 | 0.0173 | 5.84 |
| 0.0539 | 77437 | 4.1254 | 41.50 | 14.72 | 1.127 | 0.218 | 0.6779 | 0.1309 | -0.0001 | 5.18 |
| 0.0537 | 77179 | 4.0979 | 41.36 | 15.75 | 1.062 | 0.230 | 0.6434 | 0.1394 | -0.0128 | 4.62 |

Table 55: No Flow Guide Configuration at 60 mph: Alpha Sweep

| No Flow Guide Configuration at 60 mph: Alpha Sweep - 20th April 2007, $T_{room} = 71.9^{\circ} F$, $P_{baro} = 29.1699$ inHg, $S = 58.02$ in ² , $b = 11.38$ in | | | | | | | | | | |
|---|--------|---------------------------------------|---------|--------------|---------|---------|-----------|-----------|-----------|---------|
| Mach (-) | Re (-) | q (lb _f /ft ²) | V (mph) | α (°) | L (lbs) | D (lbs) | C_L (-) | C_D (-) | C_m (-) | L/D (-) |
| 0.0825 | 120370 | 9.8340 | 63.64 | -8.36 | -1.421 | 0.282 | -0.3585 | 0.0711 | -0.1470 | -5.04 |
| 0.0824 | 120190 | 9.8043 | 63.54 | -6.24 | -0.969 | 0.153 | -0.2453 | 0.0388 | -0.1330 | -6.32 |
| 0.0823 | 120000 | 9.7731 | 63.44 | -4.12 | -0.517 | 0.103 | -0.1313 | 0.0261 | -0.1105 | -5.02 |
| 0.0820 | 119590 | 9.7068 | 63.23 | -2.01 | -0.076 | 0.082 | -0.0193 | 0.0208 | -0.0850 | -0.93 |
| 0.0822 | 119850 | 9.7493 | 63.36 | 0.11 | 0.325 | 0.077 | 0.0827 | 0.0195 | -0.0543 | 4.23 |
| 0.0822 | 119850 | 9.7488 | 63.36 | 2.14 | 0.779 | 0.089 | 0.1982 | 0.0226 | -0.0259 | 8.77 |
| 0.0818 | 119270 | 9.6548 | 63.06 | 4.27 | 1.242 | 0.111 | 0.3193 | 0.0285 | -0.0040 | 11.21 |
| 0.0827 | 120570 | 9.8663 | 63.74 | 6.29 | 1.648 | 0.141 | 0.4145 | 0.0355 | 0.0163 | 11.69 |
| 0.0829 | 120900 | 9.9207 | 63.92 | 8.41 | 2.039 | 0.180 | 0.5100 | 0.0451 | 0.0349 | 11.30 |
| 0.0822 | 119880 | 9.7538 | 63.38 | 10.52 | 2.392 | 0.230 | 0.6086 | 0.0585 | 0.0483 | 10.40 |
| 0.0824 | 120140 | 9.7952 | 63.51 | 11.58 | 2.560 | 0.259 | 0.6487 | 0.0656 | 0.0526 | 9.89 |
| 0.0826 | 120450 | 9.8468 | 63.68 | 12.63 | 2.714 | 0.290 | 0.6841 | 0.0731 | 0.0550 | 9.36 |
| 0.0828 | 120700 | 9.8880 | 63.81 | 13.68 | 2.836 | 0.327 | 0.7119 | 0.0820 | 0.0544 | 8.68 |
| 0.0822 | 119820 | 9.7442 | 63.35 | 14.73 | 2.800 | 0.422 | 0.7131 | 0.1074 | 0.0306 | 6.64 |
| 0.0820 | 119570 | 9.7031 | 63.21 | 15.77 | 2.756 | 0.529 | 0.7049 | 0.1354 | 0.0067 | 5.21 |

Appendix D: MATLAB Code for Vortex Centroid Calculations

```
clear all
%clc

%6 inch offset converted to mm%
offset = 25.4*6;

%offset = 0;

%Wingspan converted to mm
b = 23.58*25.4;

%Reading the Excel Sheet from the 4deg aoa tecplot%
A = xlsread('vorticity new good Houck 4aoa.xls');

%Calibrating the y so it can be used for moment calculation
y_excel = A(:,1);
y_calibrated = abs(y_excel-200);
y = offset+y_calibrated;
z = A(:,2);
w_x_unf = A(:,10);

%Loop to filter out positive vorticity
for(i = 1:max(size(w_x_unf)))
    if(w_x_unf(i) > 0)
        w_x(i,1) = 0;
    else
        w_x(i,1) = w_x_unf(i);
    end
end

%w_x = w_x_unf;
TABLE(:,1) = y;
TABLE(:,2) = w_x;

%Loop to sum vorticity for each y coordinate%
i = 1;
j = 1;
w_x_new(i,1) = w_x(i);

for(i = 2:max(size(w_x)))
    if(y(i) == y(i-1))
        w_x_new(i,1) = w_x(i) + w_x_new(i-1,1);
        if(i < max(size(w_x)))
            if(y(i) ~= y(i+1))
                omega(j,1) = y(i);
                omega(j,2) = w_x_new(i);
                w_x_new(i,1) = 0;
                j=j+1;
            end
        elseif(i == max(size(w_x)))
            omega(j,1) = y(i);
```

```

                                omega(j,2) = w_x_new(i);
                                end
                                else
                                w_x_new(i,1) = 0;
                                end
                                end

                                %Loop to calculate total moment%
                                for(k = 1:max(size(omega)))
                                y_moment(k,1) = omega(k,1)*omega(k,2);
                                end

                                y_moment_tot = sum(y_moment);
                                y_tot = 200;
                                w_x_tot = sum(w_x)
                                y_bar_FG = y_moment_tot/(w_x_tot)
                                half_span = b/2;
                                y_non_dim_FG = y_bar_FG/half_span

                                %y_bar_FG =

                                %250.7439

                                %y_non_dim_FG =

                                %0.8373

```

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Vita.

Dermot Killian was born in Portland, Maine. He graduated from Cheverus High School, in Portland, Maine in 2002. He went on to earn a Bachelors degree in Mechanical Engineering from the United States Naval Academy in Annapolis, Maryland from 2002 to 2006. Following graduation, he was commissioned as an Officer in the United States Navy. In the Summer of 2006 he began attending the Air Force Institute of Technology at Wright Patterson Air Force Base, Ohio for completion of his Masters Degree in Aeronautical Engineering. After graduation in Summer 2007, he will be stationed in NAS Pensacola to start student naval aviator training and work towards his wings of gold.

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| 13. SUPPLEMENTARY NOTES | | | | | |
| 14. ABSTRACT <p>In an effort to explore efficient wing designs for UAV's, the Air Force is investigating the patented Houck Aircraft Configuration, which is a joined-wing aircraft with curved flow guides of varying camber connecting the upper and lower wingtips. Models were drawn in three-dimensions using Solidworks® with upper and lower wings drawn as identical NACA 2412 airfoil sections for all models. A variety of airfoil sections between the upper and lower wingtips were drawn and rotated to achieve a combination of cant and angle of attack variation. Subsequently, a solid part was lofted through these sections and merged with the upper and lower wings. Each model was built by a rapid prototype machine. A six-component balance in the AFIT low-speed wind tunnel provided measurements yielding the aerodynamic data of each model. Comparisons are made to the same basic planform area without flow guides and to a case where the wingtips are joined with a flat plate. At a Reynolds number of 38K, the increase in skin friction drag outweighed any possible reduction of induced drag. However for Reynolds numbers in the 57K to 120K range, improvements in L/D_{max} of about 2-5% over the no flow guide case were measured.</p> | | | | | |
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